

Optimization of Highly Noncoplanar Arc Therapy Trajectories: a Dosimetric Approach

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Abstract. The latest generation of linear accelerators allows the use of noncoplanar trajectories in arc therapy which combine the benefits of noncoplanar intensity-modulated radiation therapy (IMRT) treatment plans, such as improved organ sparing, with the benefits of arc therapy treatment plans, such as short treatment times. In this paper, we propose a two-step approach based on dosimetric criteria for the optimization of noncoplanar arc trajectories. In the first step, an initial set of anchor points (noncoplanar beam directions) is computed using a beam angle optimization (BAO) algorithm. In the second step, anchored in the beam directions already calculated, the noncoplanar arc trajectory is defined by iteratively computing additional anchor points considering the same dosimetric criteria used for the noncoplanar BAO. A nasopharyngeal tumor case already treated at the Portuguese Institute of Oncology of Coimbra (IPOC), is used to illustrate the benefits of the proposed optimization approach.

Keywords: radiation therapy, noncoplanar arc therapy, optimization

1 Introduction

In step-and-shoot IMRT, a linear accelerator mounted on a gantry rotates around the patient, stops at fixed beam directions and delivers non-uniform radiation fields. Noncoplanar beam directions are obtained if the couch is allowed to rotate as well. In arc therapy, irradiation is done continuously while the gantry rotates around the patient with the treatment beam always on. One of the most efficient IMRT arc techniques is volumetric modulated arc therapy (VMAT), particularly in terms of dose delivery time [1-3]. VMAT treatment plans typically use coplanar trajectories, considering a fixed couch angle equal to 0° .

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treatment plans, such as short treatment times. Several authors have proposed approaches to optimize highly noncoplanar arc trajectories, mainly resorting to geometrical metrics [5, 6].

In this paper, we propose a two-step approach based on dosimetric criteria for the optimization of noncoplanar arc trajectories. In the first step, an initial set of anchor points (noncoplanar beam directions) is computed taking advantage of the work previously developed in BAO for step-and-shoot IMRT [7–13]. In the second step, anchored in the beam directions already calculated, the noncoplanar arc trajectory is defined by iteratively computing additional anchor points considering the same dosimetric criteria used for the noncoplanar BAO. A nasopharyngeal tumor case already treated at IPOC is used to illustrate the benefits of the proposed approach. The paper is organized as follows. The strategy proposed for noncoplanar arc trajectory optimization is described in the next Section. In Section three we present the computational results. Conclusions and future work are presented in the last Section.

2 Noncoplanar Arc Trajectory Optimization

In this study, simultaneous gantry and couch rotation is considered while the treatment beam is on, leading to a highly noncoplanar arc trajectory. An optimization approach for the noncoplanar arc trajectory of a VMAT plan, called *ncVMAT*, is proposed and compared with the coplanar arc trajectory of a VMAT plan, called *cVMAT*, and with the typically used equispaced step-and-shoot IMRT plan, called *Equi*. The two-step approach proposed combines two optimization problems, the BAO problem and the arc trajectory optimization, that are quite challenging just by themselves. The dosimetric criteria used to guide these two optimization problems is the optimal value of the fluence map optimization (FMO) problem. Formulation and resolution approaches used to address FMO and BAO problems correspond to the ones detailed in Rocha et al. [12].

A clinical nasopharyngeal tumor case treated at IPOC was used to illustrate and test our approach. Nasopharyngeal tumors are complex cases to plan due to the large number of organs-at-risk (OARs) in the neighborhood of the tumor(s). The spinal cord and the brainstem are two of the main OARs considered. They are serial organs, i.e, they are compromised even if only a small part is damaged. Therefore, maximum-doses are prescribed for spinal cord and brainstem, 45 Gy and 54 Gy respectively. The other OARs considered are the parotids (the larger salivary glands) and the oral cavity (that contains the remaining salivary glands). These are parallel organs whose functioning is not much affected if a small part of the organ is damaged. Thus, mean-doses are prescribed for parotids and oral cavity, 26 Gy and 45 Gy respectively. For safety purposes, the tumor volume is enlarged by adding a margin originating a structure called planning target volume (PTV). Two levels of radiation dose are prescribed: a higher radiation dose of 70 Gy is prescribed to the tumor (called PTV_{70}) and a lower radiation dose of 59.4 Gy is prescribed to the lymph nodes (called $PTV_{59.4}$).

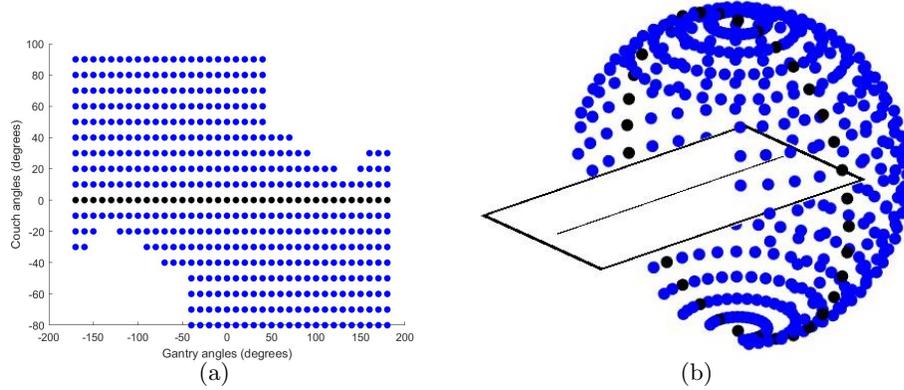


Fig. 1. Candidate beams homogeneously distributed represented in 2D – 1(a) and the corresponding 3D representation – 1(b). Black beams correspond to the coplanar candidate beams (couch fixed at 0°) while blue beams correspond to noncoplanar candidate beams.

The second step, arc trajectory optimization, is now described. A grid with equispaced beams, separated by 10° for both the gantry and the couch, is considered in this second step. After exclusion of infeasible couch-gantry angle pairs due to possible collisions of patient and gantry for a nasopharyngeal tumor case, we end up with 472 candidate beams homogeneously distributed as illustrated in Fig. 1.

The initial anchor points corresponding to the 7-beam noncoplanar BAO solution for the nasopharyngeal tumor case at hand are displayed in red in Fig. 2(a). In order to enhance one of the main features of VMAT, short treatment times, the arc trajectory starts at the leftmost anchor point in Fig. 2(a), visit each anchor point from left to right and ends at the rightmost anchor point in Fig. 2(a), with the gantry always rotating towards the next anchor point while the couch might be halted or moving towards the next anchor point. Considering these gantry/couch movement restrictions, the feasible points when calculating a new anchor point are shown in green in Fig. 2(a).

There are different ways of considering the optimal value of the FMO problem to iteratively add novel anchor points, one by one. In this study we consider the most expensive, in terms of computational time, that adds each one of the green points, one at a time, to the existing set of anchor points and then compute the corresponding optimal FMO value considering these beams. The candidate beam that leads to the minimum optimal FMO value when added to the existing anchor beams will be selected as the next anchor point. In Fig. 2(b) the novel anchor point is displayed. This recently added red point leads to the infeasibility of some green beams due to the gantry/couch movements defined. At the end of each iteration, green candidate beams that became infeasible are removed as illustrated in Fig. 2(b). This iterative procedure ends when 20 anchor points

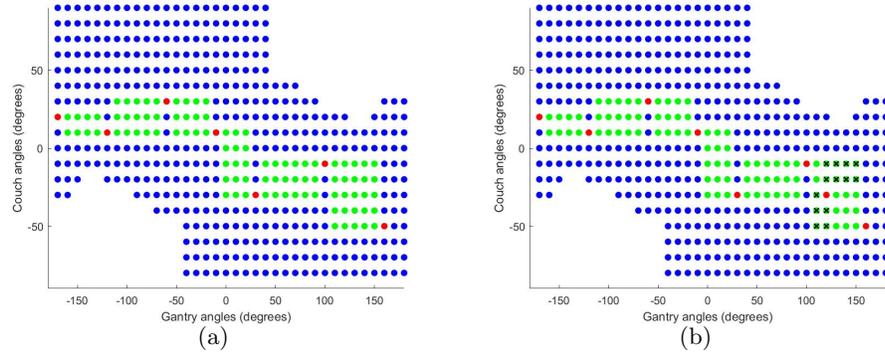


Fig. 2. The 7-beam noncoplanar BAO solution is displayed in red and the feasible points to consider when calculating a new anchor point are displayed in green – 2(a). A novel anchor point is added and green candidate beams that became infeasible are removed – 2(b).

Table 1. Target coverage, conformity and homogeneity obtained by treatment plans.

Target parameters	<i>Equi</i>	<i>cVMAT</i>	<i>ncVMAT</i>
Coverage	0.877	0.882	0.888
PTV_{70} Conformity	0.556	0.523	0.550
Homogeneity	0.880	0.881	0.881
Coverage	0.907	0.911	0.880
$PTV_{59.4}$ Conformity	0.784	0.760	0.841
Homogeneity	0.774	0.773	0.767

are obtained, which is the typical number of anchor points considered in the literature (see, e.g., [14, 15]).

3 Computational Results

Computational tests were conducted on a Dell Precision T5600 with Intel Xeon processor 64GB 1600MHz. The noncoplanar arc trajectory obtained is displayed in Fig. 3. In terms of optimal FMO values, *ncVMAT* clearly outperforms the other treatment plans in terms of optimal FMO value, improving 9.8% the value obtained by *Equi* plan while the improvement of *cVMAT* was 5.5%. For a similar tumor volume coverage, displayed in Table 1, the organ sparing, reported in Table 2, also shows the advantage of the *ncVMAT* treatment plan.

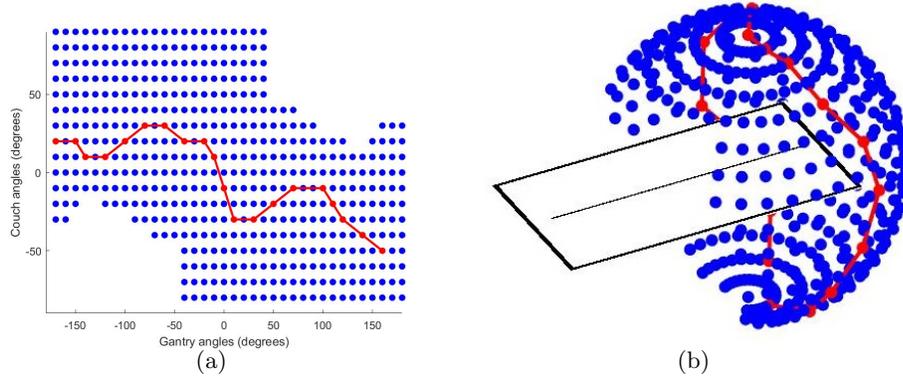


Fig. 3. Trajectory obtained by the noncoplanar arc trajectory optimization approach in 2D – 3(a) and in 3D – 3(b)

Table 2. OARs sparing obtained by treatment plans.

OAR	Mean Dose (Gy)			Max Dose (Gy)		
	<i>Equi</i>	<i>cVMAT</i>	<i>ncVMAT</i>	<i>Equi</i>	<i>cVMAT</i>	<i>ncVMAT</i>
Spinal cord	–	–	–	33.4	29.1	33.1
Brainstem	–	–	–	52.1	49.5	43.4
Right parotid	37.0	34.8	34.5	–	–	–
Left parotid	32.0	29.8	27.6	–	–	–
Oral Cavity	26.2	22.3	22.4	–	–	–

4 Conclusions and Future Work

A dosimetric approach for the optimization of highly noncoplanar arc trajectories was described and tested using a complex nasopharyngeal tumor case already treated at IPOC. For the patient tested, the resulting noncoplanar arc plan, *ncVMAT*, clearly outperforms both the coplanar arc plan, *cVMAT*, and the typically used coplanar equispaced step-and-shoot IMRT plan. Although, for the patient at hand, the overall quality of the treatment is undoubtedly greater considering the noncoplanar arc plan, tests with more patients should be conducted. Moreover, other strategies to accelerate both the noncoplanar BAO procedure and the second step that determines the remaining anchor points should be investigated.

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Conflicts of Interest

None.

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