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Visual Servoing of Mobile Robots using Non-Central Catadioptric Cameras

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Abstract

This paper presents novel contributions on image-based control of a mobile robot using a general catadioptric camera model. A catadioptric camera is usually made up by a combination of a conventional camera and a curved mirror resulting on an omnidirectional sensor capable of providing 360° panoramic views of a scene. Modeling such cameras has been subject of significant research interest in the computer vision community leading to a deeper understanding of the image properties and also to different models for different types of configurations. Visual servoing applications using catadioptric cameras have essentially been using central cameras and the corresponding unified projection model. So far only in a few cases more general models have been used. In this paper we address the problem of visual servoing using so-called radial model. The radial model can be applied to many camera configurations and in particular to non-central catadioptric systems with mirrors that are symmetric around an axis coinciding with the optical axis. In this case, we show that the radial model can be used with a non-central catadioptric camera to allow effective image-based visual servoing (IBVS) of a mobile robot. Using this model, which is valid for a large set of catadioptric cameras (central or non-central), new visual features are proposed to control the degrees of freedom of a mobile robot moving on a plane. In addition to several simulation results, a set of experiments was carried out on Robot Operating System (ROS)based platform which validates the applicability, effectiveness and robustness of the proposed method for imaged-based control of a non-holonomic robot.

Keywords: Visual servoing, non-central cameras, mobile robot.

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1. Introduction

Vision-based servoing approaches are versatile and effective methods to control robot motion by using camera observations. In practice, when a conventional camera is used there is no guarantee that the features remain in the camera's field of view (FOV). In order to overcome the problem of keeping the features in the camera's FOV, several methods have been developed namely: based on path planning [1], zoom adjustment [2], switching control [3]. Simpler and differing approaches use omnidirectional vision sensors to increase the FOV using mirrors. Wide-angle cameras include catadioptric systems that combine mirrors and conventional cameras to create omnidirectional images providing 360° panoramic views of a scene, or dioptric fish-eye lenses [4, 5]. Lately they have been subject of an increasing interest from robotics researchers [6], [7], [8], [9], [10].

Having a single viewpoint in omnidirectional imaging systems is very practical [4], [11]. Such systems have a single center of projection, in such way that every image point measures the irradiance of the light passing through the same viewpoint. One can model a central imaging system as two consecutive projections: spherical and perspective. Gever and Daniilidis in [12] derived the geometric model of these systems, and called it the unified model. In this model perspective projection corresponds to a special configuration. This formulation has been used by many research works in the area of visual servoing. Tahri et al. in [9] proposed an image-based visual servoing(IBVS) method to control the translational degrees of freedom (DOFs) which is invariant to rotational motion. In [7] an IBVS is proposed. This method is based on the auto-epipolar condition, which occurs when the current and desired catadioptric views undergo a pure translation. The method has been applied to control a holonomic mobile robot. Adaptation of the classical image-based visual servoing to a generalised imaging model was proposed in [13], by modeling the cameras as sets of 3D viewing rays. In [6], the projection of 3-D straight lines in the image plane on a central catadioptric system is used to control a 6DOFs holonomic robot and a non-holonomic mobile robot. Although the existing methods are effective for single viewpoint catadioptric systems, in practice just a few realistic configurations lead to a single-viewpoint catadioptric system, as mentioned in [4].

The problem of modeling the general case of a non-central catadioptric camera is a hard problem and still has only been tackled partially in computer vision. For this reason, iterative approaches are usually applied by some researchers to determine the reflection point on the mirror. Recently, a forward projection model has been proposed for the case of non-central catadioptric cameras consisting on a perspective camera and a rotationally symmetric conic reflector [14]. In the latter work, the optical path from a given 3D point to the given viewpoint is obtained by solving a 6th degree polynomial equation for general conic mirrors. For a spherical mirror, the forward projection equation reduces to a 4th degree polynomial, resulting in a closed form solution. In [15], an analytical forward projection equation for the projection of a 3D point reflected by a quadric mirror into the image plane of a perspective camera, with no restrictions on the camera placement is derived. They show that the equation is a 8th degree polynomial in a single unknown. In absence of an analytical and simple forward model, the determination of some elements like the interaction matrix required for image-based servoing becomes difficult.

Becerra et al. in [16] proposed a method for image-based control of a mobile robot, employing only the angular (bearing) information provided by an omnidirectional camera, where a 1D radial camera model was used. In their work, the 1D trifocal tensor model was computed using the angles of visual features as a tool for the control. In [17] the authors proposed a method to control a mobile robot by exploiting panoramic vision. In this work, the corresponding features between omnidirectional images are employed to define a control strategy which moves a ground robot along a sequence of desired positions. It is assumed that the robot tracks visual features in panoramic views of the environment that it acquires as it moves.

For scene reconstruction or control purposes, a complete knowledge of the projection model is not always required. In [18], a technique to linearly estimate the radial distortion of a wide-angle lens given three views of a real-world plane has been proposed using the radial projection model. Based on [18], linear methods for the estimation of multi-view geometry of 1D radial cameras have been studied in [10] and [19].

In this paper, it will be shown that the simple radial projection model can be sufficient for mobile robot control using a large family of catadioptric cameras. More precisely, the contributions of this paper are:

- An image-based visual servoing method for mobile robots moving on a plane, valid for a large set of catadioptric cameras (including radially symmetric non-central cameras) is proposed.
- Using the radial model, new visual features with decoupling properties are derived.
- An efficient image-based visual servoing approach based on the desired

value of the interaction matrix is proposed. Unlike the existing visual servoing methods, we incorporate the depth of the features (scene points) in the the control task.

• The feasibility and effectiveness of the proposed method have been demonstrated with real experiments using a real robot.

The rest of this paper is organized as follows:

- The proposed radial camera model and its usage for visual servoing are introduced in Section 2.
- The issues related to the selection of adequate visual features from images are discussed in Section 3. A control law which uses the proposed features is introduced in the same section.
- In Section 4 we present our experimental setup and achieved results using ROS platform and real robot.
- Conclusions and future works are presented and discussed in Section 5.

1.1. Notation and symbols

Throughout this article we use the following notations:

- Scalars are typeset in regular lower-case.
- Vectors are denoted by lower-case boldface.
- Matrices are typeset in capital boldface.
- Variables with the * (star) as exponent denote they are computed using the information corresponding to the robot's goal positions.

2. Radial camera model for visual servoing

2.1. Radial camera model

A catadioptric system made up by the combination of a conventional pinhole camera and a rotationally symmetric mirror, shown in Figure 1, is considered. The camera is positioned in such a way as to have its optical axis aligned with the mirror axis. Using the radial projection model, 3D point $\mathbf{p} = (X, Y, Z)$ is reflected

first on a point on the mirror $\mathbf{p}_{\mathbf{r}} = [X_r Y_r, Z_r]$ before being projected onto the image plane as $\widetilde{\mathbf{x}}_m$ (expressed in metric homogeneous coordinates):

$$\widetilde{\mathbf{x}}_m = (x_m, y_m, 1) = \frac{\mathbf{p_r}}{Z_r} \tag{1}$$

Point $\tilde{\mathbf{x}}_m$ is projected into the camera's image plane at $\tilde{\mathbf{x}}_d = (x_d, y_d, 1)$, expressed in pixels and can be obtained from $\tilde{\mathbf{x}}_m$ using:

$$\widetilde{\mathbf{x}}_d = \mathbf{K} \widetilde{\mathbf{x}}_m \tag{2}$$

where **K** is the matrix of the camera intrinsic parameters, f_x and f_y being the focal lengths, μ_x and μ_y are the principle point coordinates (and zero skew) as follows:

$$\mathbf{K} = \begin{bmatrix} f_x & 0 & \mu_x \\ 0 & f_y & \mu_y \\ 0 & 0 & 1 \end{bmatrix}$$
(3)

From the laws of reflection, we have: (a) vector **n**, the center of the projection **c**, the 3D points **p** and **p**_r belonging to the same plane π as shown in Fig. 1, (b) the angle between the incident ray and **n** is equal to the angle between the reflected ray and **n**. In [19] and [10], the intersection of the planes π defined by the image points from multiple views has been used to recover linearly the structure of the scene.

The mirror is rotationally symmetric, and therefore the optical axis also belongs to π . Further, for symmetry reasons, the center of distortion (in our case the center of the image) (\mathbf{c}_{rad}) and the principal point coincide. In this paper, the normalized coordinates of \mathbf{x}_m are used as follows:

$$\mathbf{x}_{\mathbf{n}} = \frac{\mathbf{x}_{\mathbf{m}}}{\parallel \mathbf{x}_{\mathbf{m}} \parallel} \tag{4}$$

so that they belong to the unit circle. Later, x_n will be used in the derivation of the new features and image servoing algorithm.

Note that the computation of $\mathbf{x_n}$ from the image points expressed in pixel only requires the knowledge of the principal point coordinates (which coincides with the distortion center) and the ratio of the focal length parameters. One can prove it as follows: from (4):

$$\begin{cases} x_n = \frac{x_m}{\sqrt{x_m^2 + y_m^2}} \\ y_n = \frac{y_m}{\sqrt{x_m^2 + y_m^2}} \end{cases}$$
(5)

On the other hand, using (2), x_m and y_m can be expressed as follows:

$$\begin{cases} x_m = \frac{x_d - \mu_x}{f_x} \\ y_m = \frac{y_d - \mu_y}{f_y} \end{cases}$$
(6)

In (5) x_m and x_y can be substituted by their expressions from (6) yielding:

$$\begin{cases} x_n = \frac{x_d - \mu_x}{\sqrt{(x_d - \mu_x)^2 + \rho_f^2 (y_d - \mu_y)^2}} \\ y_n = \frac{y_d - \mu_y}{\sqrt{\rho_f^{-2} (x_d - \mu_x)^2 + (y_d - \mu_y)^2}} \end{cases}$$
(7)

where

$$\rho_f = \frac{f_x}{f_y} \tag{8}$$

Equation (7) implies that further than the coordinates of the distortion's center, only the ratio between the two focal lengths needs to be known in order to obtain x_n . Note that the center of the image (center of distortion) can be approximated by estimating the center of the mirror border (assumed to be a circle or an ellipse) [20].

Let $\tilde{\mathbf{x}}_u = (x_u, y_u, 1) = \frac{\mathbf{p}}{Z}$ be the point coordinates (homogeneous) in metric units of the projection of **p** using pinhole model as shown in Fig. 1. Let $\mathbf{x}_u = [x_u, y_u]$ be the non-homogeneous coordinates corresponding to $\tilde{\mathbf{x}}_u$. Since the center of the pin-hole camera and **p** belong to plane π , the point \mathbf{x}_u also belongs to the intersection of this plane with the image plane. Therefore, \mathbf{c}_{rad} , \mathbf{x}_u and \mathbf{x}_m belong

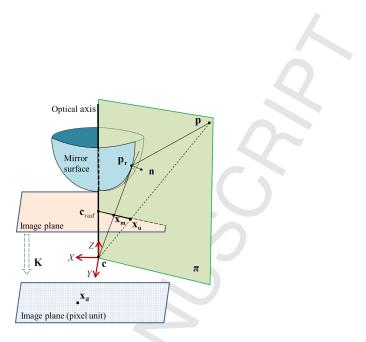


Figure 1: Axial catadioptric system

to the same line. We have then $x_n = \frac{x_u}{\|x_u\|},$ which leads to:

$$\mathbf{x_n} = \begin{bmatrix} x_n \\ y_n \end{bmatrix} = \frac{1}{\sqrt{X^2 + Y^2}} \begin{bmatrix} X \\ Y \end{bmatrix}$$
(9)

Note that $\mathbf{x}_{\mathbf{n}}$ is not defined only if the 3D point belongs to the camera optical axis (which does not happen in the case of the catadioptric camera). In the following $\mathbf{x}_{\mathbf{n}}$ will be used to define new visual features to control the motion of a mobile robot moving on a plane.

2.2. Visual servoing

In visual servoing the time variation \dot{s} of the visual features s can be linearly expressed with respect to the relative camera-object kinematics screw:

$$\dot{\mathbf{s}} = \mathbf{L}_{\mathbf{s}}\tau,\tag{10}$$

where L_s is the interaction matrix related to s. Usually, the control scheme is designed to reach an exponential decoupled decrease of differences on the visual features to their goal value s^{*}. If we consider an eye-in-hand system observing a static object, the corresponding control law is:

$$\tau_c = -\lambda \widehat{\mathbf{L}_{\mathbf{s}}^+}(\mathbf{s} - \mathbf{s}^*), \qquad (11)$$

where $\widehat{\mathbf{L}_s}$ is a model or an approximation of \mathbf{L}_s , $\widehat{\mathbf{L}_s}^+$ the pseudo-inverse of $\widehat{\mathbf{L}_s}$, λ a positive gain tuning the time to convergence, and $\tau_c = (\upsilon_c, \omega_c)$ the camera velocity sent to the low-level robot controller. In practice the matrix $\widehat{\mathbf{L}_s}$ could be chosen as the current value of the interaction matrix \mathbf{L}_s . This choice (except in the case of a singularity) ensures an exponential decrease of the error on features in image. Unfortunately, further to the problem of local minima and singularities, computing the exact current value of the interaction matrix requires the knowledge of the depth information. Determining this information can be time consuming, but also subject to instabilities. In order to avoid these problems, using the depth information of the goal values in \mathbf{L}_s can be an alternative (i.e $\mathbf{L}_s(\mathbf{Z}^*)$). Unfortunately, in that case, the exponential decrease of the features errors in the image will no longer be ensured. Furthermore, if the value of $\widehat{\mathbf{L}_s}$ changes, its pseudo-inverse should also be computed at each iteration, which also can be time consuming if the size of the features vector increases significantly.

In order to avoid computing the depth information and inverting \mathbf{L}_{s} at each time that the velocities have to be computed, a straightforward choice is to use the constant matrix L_{s^*} computed for the goal pose. Using L_{s^*} also permits to avoid the problem of the singularities (except if the desired position corresponds to a singular value of L_{s^*}). Despite the mentioned advantages above, in practice using L_{s*} ensures a local and limited domain of convergence around the desired position as compared to the case where $\mathbf{L}_{\mathbf{s}}$ is used. Furthermore, the behavior of the feature errors in the image as well as in 3D space is neither always predictable nor always satisfactory. Combining L_{s^*} and L_s in a single control law has been studied in [21] and [22] to improve the stability and 3D behavior. Unfortunately, once again, and as far as L_s is involved in the control law, the depth information has to be determined and L_s to be inverted. Actually, the limited domain of convergence and the unpredictable behavior obtained using Ls* results, in large part, from the problem of the tensor frame change. Indeed, L_{s^*} expresses the variations of features as a function of the camera velocities expressed in the goal frame. Therefore, if the current and the goal frames have different orientations, the tensor change of frame has to be taken into account since the velocities are to be applied in the current camera frame. This problem has been highlighted in [23] for instance. More precisely, instead of using the average $\widehat{\mathbf{L}_{s}} = \frac{\mathbf{L}_{s^*} + \mathbf{L}_{s}}{2}$, as proposed in [21], [23] proposed to use $\widehat{\mathbf{L}_{s}} = \frac{\mathbf{L}_{s} + \mathbf{L}_{s} \cdot \mathbf{T}^{-1}}{2}$ after integrating the spatial motion transform T. In this paper we only use the goal value of the interaction matrix in the control law. More precisely, the velocity computed using $L_s = L_{s^*}$ in the control law (11) has to be multiplied by a spatial transformation **T**. A method

to effectively approximate the tensor change of frame in the case of a mobile robot (to avoid reconstructing depth data and inverting $\widehat{\mathbf{L}_s}$ at each iteration of the control loop) will be described next.

3. Visual features selection and control law

In the next paragraph, new visual features are proposed and their corresponding interaction matrices derived. A control law using the goal values of the interaction matrices is also proposed and derived.

3.1. Visual features suitable to control camera translational velocities

In this paragraph, we introduce new visual features which are suitable for the control of the translation component of the camera movement. To do so, we use the inner product between the coordinates of two points \mathbf{x}_{ni} and \mathbf{x}_{nj} in the image:

$$c_{ij} = \mathbf{x}_{\mathbf{n}\,i}^{\top} \mathbf{x}_{\mathbf{n}\,j} \tag{12}$$

Note that at most $N_p(N_p - 1)/2$ of c_{ij} can be defined, N_p being the number of the feature points. By taking the derivative of (12), we obtain:

$$\dot{c}_{ij} = \mathbf{x}_{\mathbf{nj}}^{\dagger} \dot{\mathbf{x}}_{\mathbf{ni}} + \mathbf{x}_{\mathbf{ni}}^{\dagger} \dot{\mathbf{x}}_{\mathbf{nj}}$$
(13)

The interaction matrix corresponding to $\mathbf{x_n}$ can be obtained by taking the derivative of (9):

$$\mathbf{L}_{\mathbf{x}_{\mathbf{n}}} = \begin{bmatrix} \mathbf{L}_{\mathbf{x}_{\mathbf{n}}} \boldsymbol{\upsilon} & \mathbf{L}_{\mathbf{x}_{\mathbf{n}}} \boldsymbol{\omega} \end{bmatrix}$$
(14)

with:

$$\mathbf{L}_{\mathbf{x}_{\mathbf{n}}\boldsymbol{\upsilon}} = \begin{bmatrix} -\frac{(1-x_n^2)}{d} & \frac{x_n y_n}{d} & 0\\ \frac{x_n y_n}{d} & -\frac{(1-y_n^2)}{d} & 0 \end{bmatrix}$$
(15)

and

$$\mathbf{L}_{\mathbf{x}_{\mathbf{n}}\boldsymbol{\omega}} = \begin{bmatrix} -x_n y_n z_n & -(1-x_n^2) z_n & y_n \\ (1-y_n^2) z_n & x_n y_n z_n & -x_n \end{bmatrix}$$
(16)

where $d = \sqrt{X^2 + Y^2}$ and $z_n = Z/d$. By combining (14) and (13), the interaction matrix $\mathbf{L}_{c_{ij}} = [\mathbf{L}_{c_{ij}\omega} \ \mathbf{L}_{c_{ij}\omega}]$ corresponding to c_{ij} can be then obtained by:

$$\mathbf{L}_{c_{ij}\upsilon} = \left[\begin{array}{c} \left(\frac{-1}{d_j} + \frac{c_{ij}}{d_i}\right) \mathbf{x}_{\mathbf{n}\ i}^\top + \left(\frac{-1}{d_i} + \frac{c_{ij}}{d_j}\right) \mathbf{x}_{\mathbf{n}\ j}^\top & 0 \end{array} \right]$$
(17)

and

$$\mathbf{L}_{c_{ij}\boldsymbol{\omega}} = \begin{bmatrix} y_{nj}z_{ij} + y_{ni}z_{ji} & -x_{nj}z_{ij} - x_{ni}z_{ji} & 0 \end{bmatrix}$$
(18)

where $z_{ij} = z_{ni} - c_{ij}z_{nj}$ and $z_{ji} = z_{nj} - c_{ij}z_{ni}$. From (17) and (18), it can be seen that c_{ij} is invariant to the motion around the optical axis (which corresponds to the normal of the plane of motion). We assume that the camera is mounted on the mobile robot so that the translational motion takes place on the plane defined by the vectors **x** and **y** of the camera frame. Therefore, only the first two entries of the matrix $L_{c_{ij}v}$ are useful for the control of the translational motion with respect to the x-axis and the y-axis. In the next paragraph, we explain how to select an adequate feature to control the remaining DOF, namely the rotation around the optical axis.

3.2. Visual features suitable to control camera rotation

In this paragraph, we introduce visual features which are suitable for the control of the rotational component of robot motion. We consider α as a natural feature in the image that can be obtained from points \mathbf{x}_n to control the rotation of the robot on a plane as:

$$\alpha = atan2(y_n, x_n) \tag{19}$$

The time variation of α can then be obtained by:

$$\dot{\alpha} = \frac{x_n \dot{y}_n - y_n \dot{x}_n}{x_n^2 + y_n^2} = x_n \dot{y}_n - y_n \dot{x}_n$$
(20)

By combining (20) and (14), the interaction matrix corresponding to α can be obtained by:

$$\mathbf{L}_{\alpha} = \begin{bmatrix} \frac{y_n}{d} & \frac{-x_n}{d} & 0 & x_n z_n & y_n z_n & -1 \end{bmatrix}$$
(21)

From (21), we can notice the direct link between α and the rotation around the zaxis. For the sake of robustness, all projected points $\mathbf{x_n}$ have to be used. A simple way to do it is by stacking all the angles α_i in a feature vector. A better choice can be combining all the points in a single and unique feature to control the rotation around the z-axis. A straightforward and simple way to use all the rotation angles could be using their average $\alpha_a = \frac{1}{N} \sum_{i=1}^{N} atan2(y_{ni}, x_{ni})$. Such feature is directly related to ω_z . However, the arithmetic average of rotations does not correspond to the real average of rotations, especially when the difference between the rotations considered is large. For instance, for a rotation angle close to π , and due to the effect of noise or due to translational motion, the computed rotation angles can have opposite signs. Therefore, the rotation angle corresponding to their arithmetic mean would have a value close to 0 instead of π or $-\pi$ generating some discontinuities in the estimation of α_a . In this paper, we propose to define a rotation angle α_m for a virtual point whose coordinates are computed as a linear combination of the projections of points on the circle. Let **p**₁ be the point defined by:

$$\mathbf{p_1} = \sum_{i=1}^{N} a_i \mathbf{x_{ni}} \tag{22}$$

From $\mathbf{p_1}$, we define a new point $\mathbf{v_1}$ belonging to the unit circle by:

$$\mathbf{v}_1 = \frac{\mathbf{p}_1}{\parallel \mathbf{p}_1 \parallel} \tag{23}$$

By taking the derivative of (23), the interaction matrix corresponding to v_1 can be obtained by:

$$\mathbf{L}_{\mathbf{v}_{1}} = \frac{\mathbf{I}_{2} - \mathbf{v}_{1} \mathbf{v}_{1}^{\top}}{\parallel \mathbf{p}_{1} \parallel} \sum_{i=1}^{N} a_{i} \mathbf{L}_{\mathbf{x}_{ni}}$$
(24)

Let α_m be the angle defined by:

$$\alpha_m = atan2(v_{1y}, v_{1x}) \tag{25}$$

By taking the derivative of (25), it can be obtained:

$$\dot{\alpha}_m = v_{1x} \dot{v}_{1y} - v_{1y} \dot{v}_{1x} \tag{26}$$

By combining (26) with (24), $L_{\alpha_m \omega_z} = -1$ is obtained. As a result one can conclude that α_m varies linearly with respect to the velocity ω_z .

The parameters a_i have to be determined before defining point \mathbf{v}_1 on the unit circle. More precisely, we have to define a virtual point \mathbf{p}_1^* and next represent it as a linear combination of the desired projected points on the circle \mathbf{x}_{ni}^* . For the sake of simplicity, \mathbf{p}_1^* is chosen to be unitary ($\| \mathbf{p}_1^* \| = 1$ then $\mathbf{v}_1^* = \frac{\mathbf{p}_1^*}{\| \mathbf{p}_1^* \|} = \mathbf{p}_1^*$). Let \mathbf{p}_2^* be also a unit vector perpendicular to \mathbf{p}_1^* . As a result \mathbf{p}_1^* and \mathbf{p}_2^* form a direct orthogonal frame basis $\mathbf{V}^* = [\mathbf{p}_1^*; \mathbf{p}_2^*]$. It is possible to represent any given frame basis \mathbf{V}^* as a linear combination of the coordinates of a set of points. For instance, \mathbf{V}^* could be set as the desired frame of the camera. In any given frame basis \mathbf{V}^* , each projected point onto the circle can be expressed as:

$$\mathbf{x}_{ni}^* = b_{1i} \mathbf{v}_{n1}^* + b_{2i} \mathbf{v}_{n2}^* \tag{27}$$

Let **B** be the $2 \times N$ matrix that defines the coordinates of all the projected points on the new frame basis. We have:

 $\mathbf{X}_{nt}^* = \mathbf{V}^* \, \mathbf{B}$

where $\mathbf{X}_{nt}^* = [\mathbf{x}_{n1}^* \ \mathbf{x}_{n2}^* \dots \mathbf{x}_{nN}^*]$, and $\mathbf{B} = \mathbf{V}^{*\top} \mathbf{X}_{nt}^*$. From (28), \mathbf{V}^* can be represented as a linear combination of \mathbf{X}_{nt}^* by:

$$\mathbf{V}^* = \mathbf{X}_{nt}^* \, \mathbf{B}^+ \tag{29}$$

(28)

 \mathbf{B}^+ is a $N \times 2$ matrix corresponding to the pseudo-inverse of **B**. Therefore, the a_i can be chosen as the first columns of \mathbf{B}^+ .

3.3. Control law

Let $\mathbf{s}_{\mathbf{c}}$ be the feature vector obtained by stacking the features c_{ij} and $\mathbf{s}_{\mathbf{c}}^*$ their goal values. Let $\mathbf{L}_{\mathbf{s}_{\mathbf{c}}}$ be the interaction matrix obtained by stacking the two first entries v_x and v_y of the interaction matrix corresponding to each feature c_{ij} . Only the two first entries are taken into account because we are only concerned with a planar motion and c_{ij} is invariant to the rotation around z-axis. Let us consider that the goal is to move the desired camera position towards the initial one. Therefore, the velocities that have to be applied to the goal position of the camera using its corresponding interaction matrix are obtained from:

$$\begin{cases} \begin{bmatrix} \upsilon_x^* \\ \upsilon_y^* \end{bmatrix} = -\lambda \mathbf{L}_{\mathbf{s}\mathbf{c}^*}^+(\mathbf{s}_{\mathbf{c}}^* - \mathbf{s}_{\mathbf{c}}) \\ \omega_z^* = \lambda (\alpha_m^* - \alpha_m) - L_{\alpha_m \upsilon_x^*} \upsilon_x^* - L_{\alpha_m \upsilon_y^*} \upsilon_y^* \end{cases}$$
(30)

where $\mathbf{L}_{\alpha_{\mathbf{m}}v_{\mathbf{x}^*}}$ and $\mathbf{L}_{\alpha_{\mathbf{m}}v_{\mathbf{y}^*}}$ represent the variation of α_m with respect to the velocities v_x and v_y respectively (Notice that v_x , v_y and ω_z are the only non-zero components of the camera motion). Let us consider the three frames shown in Figure 2-b. Let \mathcal{F}_c and \mathcal{F}_{c^*} represent respectively the current and the goal camera frames and \mathcal{F}_{ci} an intermediate frame that has the same position of the center as \mathcal{F}_{c^*} but the orientation of \mathcal{F}_c . As it can be seen from Figure 2-b, the translational velocity to be applied to the frame \mathcal{F}_c to move it towards its desired position is equal to the negative of the velocities that move \mathcal{F}_{ci} towards \mathcal{F}_c . Therefore, to control the translational motion of the current camera position, it is more adequate to use the interaction matrix corresponding to \mathbf{s}_c computed for the position corresponding to \mathcal{F}_{ci} :

$$\begin{bmatrix} v_x \\ v_y \end{bmatrix} = -\lambda \mathbf{L}_{\mathbf{s}_{\mathbf{c}i}}^+(\mathbf{s}_{\mathbf{c}} - \mathbf{s}_{\mathbf{c}i})$$
(31)

In the case of the projection onto the sphere, it was shown in [9] that two interaction matrices $L_{i_n}^2$ and $L_{i_n}^1$ related to an invariant to the 3D rotation i_n and

computed respectively for two camera poses 1 and 2 separated by a rotational motion are related by equation:

$$\mathbf{L}_{i_{n}}^{2} = \mathbf{L}_{i_{n}}^{1} \,^{1}\mathbf{R}_{2} \tag{32}$$

where ¹**R**₂ is the rotation matrix. Similarly, it can be shown for feature \mathbf{s}_{ci} that if only a rotation is considered between \mathcal{F}_{ci} and \mathcal{F}_{c*} , $\mathbf{L}_{\mathbf{s}_{ci}}$ can be obtained from $\mathbf{L}_{\mathbf{s}_{c*}}$ by:

$$\mathbf{L}_{\mathbf{s}_{\mathbf{c}\mathbf{i}}} = \mathbf{L}_{\mathbf{s}_{\mathbf{c}^{*}}} \mathbf{c}^{*} \mathbf{R}_{\mathbf{i}} \tag{33}$$

where $c^* \mathbf{R}_i$ is the 2-dimensional rotation matrix corresponding to the rotation angle γ between \mathscr{F}_{c*} and \mathscr{F}_{ci} . We continue to prove that c_{ij} will be invariant to any rotation around *z* axis. Based on (12), c_{ij} is a function of \mathbf{x}_{ni} and \mathbf{x}_{nj} :

$$c_{ij} = g(\mathbf{x}_{\mathbf{n}i}, \mathbf{x}_{\mathbf{n}j}) = \mathbf{x}_{\mathbf{n}i}^{\top} \mathbf{x}_{\mathbf{n}j}$$
(34)

Now we apply an arbitrary rotation \mathbf{R} to the inputs of the function g:

$$g(\mathbf{R}\mathbf{x}_{\mathbf{n}\mathbf{i}},\mathbf{R}\mathbf{x}_{\mathbf{n}\mathbf{j}}) = (\mathbf{R}\mathbf{x}_{\mathbf{n}\mathbf{i}})^{\top} \mathbf{R}\mathbf{x}_{\mathbf{n}\mathbf{j}} = \mathbf{x}_{\mathbf{n}\mathbf{i}}^{\top} \mathbf{R}^{\top} \mathbf{R}\mathbf{x}_{\mathbf{n}\mathbf{j}} = \mathbf{x}_{\mathbf{n}\mathbf{i}}^{\top} \mathbf{x}_{\mathbf{n}\mathbf{j}}$$
(35)

Equation (35) shows that $g(\mathbf{R}\mathbf{x_{ni}}, \mathbf{R}\mathbf{x_{nj}})$ is equal to $g(\mathbf{x_{ni}}, \mathbf{x_{nj}})$ and as a result the feature c_{ij} is invariant to any rotation around z axis. Since c_{ij} is invariant to a z-axis rotation one obtains $s_{ci} = \mathbf{s_{c*}}$. By combining this result and (33) in (31), we obtain:

$$\begin{bmatrix} \upsilon_x \\ \upsilon_y \end{bmatrix} = -^{\mathbf{i}} \mathbf{R}_{\mathbf{c}*} \lambda \mathbf{L}_{\mathbf{s}_{\mathbf{c}*}}^+ (\mathbf{s}_{\mathbf{c}} - \mathbf{s}_{\mathbf{c}*})$$
(36)

By combining (36) and (30), we finally obtain:

$$\begin{bmatrix} \upsilon_{x} \\ \upsilon_{y} \end{bmatrix} = -{}^{\mathbf{i}} \mathbf{R}_{\mathbf{c}*} \begin{bmatrix} \upsilon_{x*} \\ \upsilon_{y*} \end{bmatrix}$$
(37)

On the other hand, since and the z-axis has the same orientation in the current and the goal camera poses, we choose $\omega_z = -\omega_{z*}$. In the next section, we explain how to effectively approximate ${}^{i}\mathbf{R}_{c*}$.

4. Experiments

In this section we first present a set of simulations and afterward some results obtained in a real scenario will be presented. For both cases, a differential drive mobile robot is considered as non-holonomic vehicle. The uniform coordinate

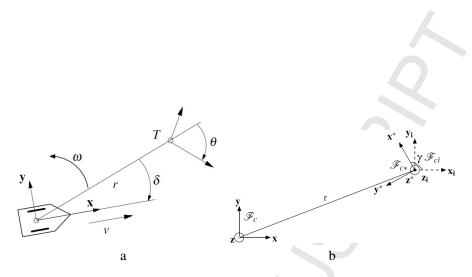


Figure 2: (a) Egocentric polar coordinate system with respect to the observer (b) Camera frame position.

system used as the robot model is shown in Fig. 2-a. The control law proposed in [24] is used to transform the camera velocities into linear and steering velocities to be applied to the mobile robot. More precisely, the steering velocity is defined by:

$$\boldsymbol{\omega} = \frac{\boldsymbol{v}_l}{r} \left[k_2 (\boldsymbol{\delta} - \arctan(-k_1 \boldsymbol{\theta}) + (1 + \frac{k_1}{1 + (k_1 \boldsymbol{\theta})^2}) \sin(\boldsymbol{\delta}) \right]$$
(38)

where k_1 and k_2 are two positive constants, v_l is the linear velocity, r is the distance between the current position of the robot and the goal position, θ is the orientation of the goal T with respect to the line of sight defined between the current and desired position of the robot (T); δ is the orientation of the vehicle heading with respect to the line of sight. To apply the control law (38), it is necessary to represent the parameters v_l , r, θ and δ as a function of the cartesian camera velocities obtained by IBVS. First, the linear velocity can be defined as $v_l = \sqrt{v_x^2 + v_y^2}$. The linear velocity becomes null when the translational motion is null (because of the invariance of the feature s_c). The angle δ can also be estimated as the direction of the velocity to be applied to the current camera pose from $\delta = atan2(v_v, v_x)$ (since the camera is rigidly attached to the robot). The distance from the initial to the desired camera pose can be approximated by $r = \frac{\sqrt{v_x^2 + v_y^2}}{\lambda}$ after removing the time unit. This is equivalent to setting $\frac{v_l}{r} = \lambda$ in (38). Finally, angle θ can be defined as the rotation angle between the initial and goal camera pose. More precisely, we choose $\theta = \frac{\omega_c}{\lambda} - \delta$. Note also that θ as defined in Figure 2-a is equal to γ as defined in Figure 2-b. The rotation matrix ${}^{i}\mathbf{R}_{*}$ is also estimated using $\gamma = \frac{\omega_{z}}{\lambda}$

as a rotation angle.

4.1. Simulation results

In the first set of simulation results, we compare the application of the IBVS described in this paper with the application of the exact 3D parameters θ , *r* and δ in the control law (38). More precisely, four examples of robot parking are considered: all cases start from the same initial pose and have to converge towards four different desired poses obtained after shifting the initial pose by the translational motion defined by [4 4] *meters* but with different orientations corresponding respectively to the angles 0, $\frac{\pi}{2}$, π and $\frac{3\pi}{2}$. The images of the following set of 8 points defined in the 3D environment were used to computed the velocities for IBVS:

$$\mathbf{X}_{\mathbf{0}} = \begin{bmatrix} 15.6 & 15.6 & 7.98 & 5.38 & 9 & 6.62 & 0 & 0 \\ 7.62 & 8.29 & 15.6 & 15.6 & 0 & 0 & 8.15 & 10.32 \\ -0 & 0.86 & 2.52 & 0.32 & 2.07 & 2.14 & 1.30 & 1.79 \end{bmatrix}$$
(39)

In these simulations, the desired depths $r^* = \sqrt{X^{*2} + Y^{*2}}$, required to compute the interaction matrix, are assumed to be known (they could, for example, be estimated using the multiple-view scene reconstruction proposed in [15]). The simulations have been performed using the ISFfMR Integrated Simulation Framework for Mobile Robots [25]. The constants $k_1 = 4$ and $k_2 = 12$ were used in the control law (38) to control the robot using IBVS and the real 3D parameters. Figure 3 shows the trajectories performed by the robot using IBVS and using the real 3D data. From this figure, it can be seen that the trajectories are similar and that IBVS has a performance similar (and as satisfactory) as using the 3D real data. Video 1 (attachment to this paper¹) shows the behavior of the robot along the performed trajectories. The video confirms the similarities between the two trajectories and the good convergence towards the desired robot pose. Only the velocities of the robot along these trajectories differ: the convergence using IBVS is slightly slower than using the 3D real data for this experiment. This due to the fact that the amplitude of the translation estimated using IBVS is smaller than the real one.

In the second set of simulations, a wrong scale for the position of the points is used ($\hat{r^*} = 1.3 r^*$ is used as depth instead of the real values). The same cases of robot parking considered in the first set of simulations are considered here. Figure 4 compares the trajectories performed by the robot using the real value of

¹https://sites.google.com/site/otahri

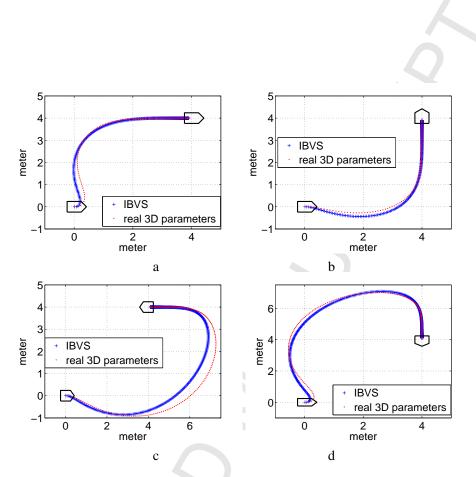


Figure 3: Trajectory performed by the robot using the real 3D parameters and the 3D parameters estimated from an IBVS in the case of four different rotation angles: a) 0*degrees*, b) 90*degrees*, c) 180*degrees*, d) 270*degrees*

 εr^* and $\hat{r^*}$ to computed the desired value of the interaction matrices. From these plots, it can be seen that the errors on the scene scale have negligible influence on the trajectories performed, which means that the curvature defined by the ratio between the steering velocity and the linear velocity $\frac{\omega}{v_l}$ is not very sensitive to the scene scale. Videos² 2 and 3 compare the behavior of the robot motions along the performed trajectories and the point motions in the image using the correct and an erroneous scene scale. The two videos show that the robot converges in all cases, but with different velocities: the convergence using $\hat{r^*} = 1.3 r^*$ to computed

²https://sites.google.com/site/otahri

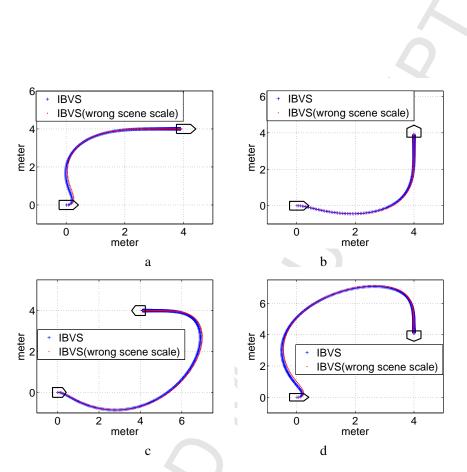


Figure 4: Trajectory performed by the robot using the real 3D parameters and the 3D parameters estimated from an IBVS in the case of four different rotation angles: a) 0*degrees*, b) 90*degrees*, c) 180*degrees*, d) 270*degrees*

the interaction matrices is faster than when using the real depth r^* . This is due to the fact that the scene scale used is bigger than the real one, and therefore the amplitude of the translational motions to be performed are amplified.

4.2. Results using real scenario

Here we present some experiments performed in real scenario by a real robot, using the open-source meta-operating system, ROS [26]. A Pioneer 3-DX [27] has been used as differential drive non-holonomic vehicle. Two different catadioptric systems were used in our servoing experiments, both made up of a hyperbolical mirror (50mm diameter) and a perspective camera (6mm focal length). The specifications of the hyperbolic mirrors are as follows:

	Equation	Parameters
Mirror A	$\frac{X^2}{a^2} - \frac{Y^2}{b^2} = -1$	a = 20.8485, b = 26.8578
Mirror B	$\frac{\tilde{X}^2}{a^2} - \frac{\tilde{Y}^2}{b^2} = -1$	a = 23.6634, b = 27.1301

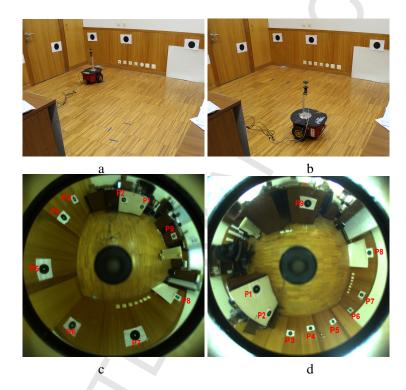


Figure 5: Images of the robot and of images acquired by the robot on its position. (a) and (c): the robot in the goal position and the corresponding image acquired by the robot, respectively. (b) and (d) the robot on an arbitrary initial position and its corresponding image, respectively.

In the first experiment we use mirror A and later it will be substituted by mirror B, while preserving the same configuration. Once the robot is placed on the goal position (Fig. 5-a) in the scene, an image is grabbed as the *goal image* (Fig. 5-c). As seen in the figures, some black circles (here nine circles) were fixed on the walls and used as visual beacons. The centers of these beacons are automatically extracted (using openCV library) and used as our *goal points* for the goal image. The proposed method requires the knowledge of the depths of all the points in

the scene, observed from the goal position, in order to compute the interaction matrices. Therefore in our experiment, the distance (depth) between each of the fixed beacons to the robot are measured manually, while the robot is parked in this position. One can conclude that a coarse measurement is enough and there is no need to have precise depth, as discussed in the simulation part.

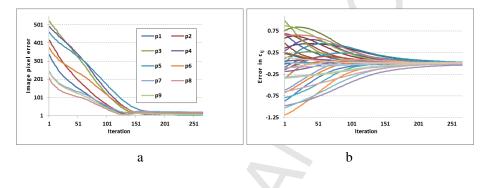


Figure 6: Diagram of errors in terms of points and features during the convergence: Fig. (a) shows the reduction of errors between the nine goal image points and their correspondences in the current image. Using these nine image points, 36 features were defined. The errors between the goal features and current features are plotted in (b).

As already mentioned, one of the advantages of the method proposed in this paper is that the camera does not need to be fully calibrated. In our experiments, ρ_f has been given the value 1 and the center of the image/distortion was computed as the center of the mirror border image. It has as coordinates $\mu_x = 643$, $\mu_y = 535$ (automatically obtained through applying the Hough transform for circle detection defining the mirror border in the image).

The robot is placed on an arbitrary position, the *initial position* (Fig. 5-b). Then the robot moves, so that it can reach the goal position with the goal orientation. After the extraction of features from both goal and initial images, the proposed control law is applied to the robot. In these experiments, $k_1 = 1$, $k_2 = 1$ are used as constant parameters in the control law (38). As expected the robot performs a smooth trajectory, converges and stops nearly on the goal position. Fig. 6-a depicts the errors (distances in pixels) between the goal image points and their corresponding points in the current as a function of servoing iterations. As one can see, the convergence is quite smooth. There is a negligible spacial error (less than 1cm) between the parked and goal position (the behavior of the robot is shown in the video 3). The same behavior is shown in Fig. 6-b where the errors

between the features $(c_{ij}^* - c_{ij})$ are plotted. Note that all 36 available c_{ij} (from 9 tracked features points) are used in this experiment. The velocities of the camera and robot are shown in Fig. 7-a and Fig. 7-b, respectively. Fig. 8 presents the errors in the angle α_m values during servoing.

For the sake of evaluating the robustness of the proposed approach in case of using different mirrors, a new experiment has been carried out: mirror A (the mirror used so far) has been replaced by mirror B. Fig. 9-left and -right respectively show the images taken by mirrors A and B, once the robot is placed on the desire position. In this position, an image is taken while mirror B is mounted. Features are extracted from the newly taken image and kept as the desired features. Then mirror A has been placed back on the robot. Afterwards, the previously presented visual servoing experiment has been repeated. As one can see from the video³ 4, the system's behavior is robust despite of using a goal image taken by other camera.

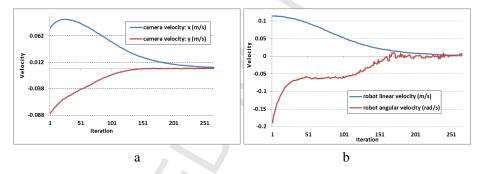


Figure 7: Plots for the velocities during the iterations: (a) Depicts the camera linear velocity. (b) shows the linear and angular components of the velocity of the robot during the convergence.

5. Conclusion

In this paper, we have used the radial camera model to propose a novel IBVS. New features were extracted based on this model and their corresponding interaction matrices were derived. The method does not require a fully calibrated camera. The only calibration parameters that are require are the ratio of the two focal lengths ($\rho_f = \frac{f_x}{f_y}$) and the coordinates of the principal point (μ_x and μ_y). In

³https://sites.google.com/site/otahri/

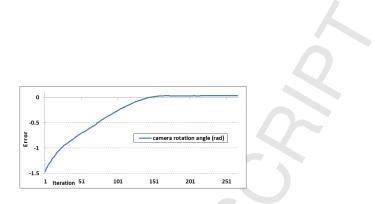


Figure 8: Error in the camera's angle corresponding to α_m in (25).

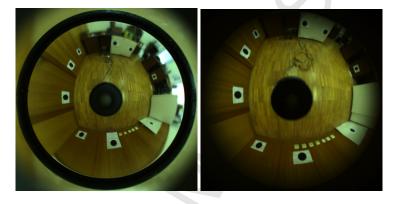


Figure 9: Images acquired by the robot on its goal position using two different mirrors. Left: mirror A, right mirror B.

general, both these parameters can be estimated automatically by using the image of the mirror border (circle or ellipse). Furthermore, only the goal value of the interaction matrix is used to compute the velocities, which allows avoiding the estimation of the depths of the points, as well as the inversion of the interaction matrix, during servoing.

As a result of using a simple radial model, the proposed IBVS method can be applied for a large class of catadioptric cameras, both central and non-central. The proposed method has been implemented using a ROS-based robotic platform. The results obtained show the validity and effectiveness of the proposed approach. Our future work includes extending the method for a 6 *DOFs* robot and the use of global visual features as well as multiple-view geometry in the control law.

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HIGHLIGHTS

- An image-based visual servoing method for mobile robots is proposed.
- Using the radial model, new visual features with decoupling properties are derived.
- Efficient IBVS approach based on desired value of the interaction matrix is proposed.
- Real experiments using a real robot have been carried out (different scenarios).