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ESTUDOS DO GEMF

N.º 9

2007

**PUBLICAÇÃO CO-FINANCIADA PELA  
FUNDAÇÃO PARA A CIÊNCIA E TECNOLOGIA**

Impresso na Secção de Textos da FEUC  
COIMBRA 2007

# Optimal monetary policy with a regime-switching exchange rate in a forward-looking model\*

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## Abstract

We evaluate the macroeconomic performance of different monetary policy rules when there is exchange rate uncertainty. We do this in the context of a non-linear rational expectations model. The exchange rate is allowed to deviate from its fundamental value and the persistence of the deviation is modeled as a Markov switching process. Our results suggest that taking into account the switching nature of the economy is important only in extreme cases.

*JEL Classification:* E52, E58, F41.

*Keywords:* Exchange Rates, Monetary Policy, Markov Switching.

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\*This version: 3/11/2007. The authors are grateful to Luís Aguiar-Conraria, Miguel Portela and other participants at the 13th International Conference of the Society of Computational Economics, Montréal, and at a NIPE Seminar, University of Minho, Braga, Portugal. F. Alexandre and P. Bação are grateful for the hospitality enjoyed at Birkbeck College. The authors acknowledge financial support from Fundação para a Ciência e a Tecnologia, research grant POCI/EGE/56054/2004 (partially funded by FEDER).

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# 1 Introduction

In most respects inflation targetting since 1989 or thereabouts has been a great success. It has achieved both low, stable inflation and steady output growth in most of the countries that practice it. In the United States this fortunate combination of events has been dubbed “The Great Moderation”. The one dark cloud on the horizon has been volatility in the prices of financial and real assets, including stock prices, exchange rates, and housing prices. There is the suspicion that some of these price movements have not been driven by fundamentals. That is, they have been bubbles. They may be contributing to real economic fluctuations. The US stock market rose in the late 1990s in the dot com boom, and may have been sustained by the “Greenspan put”. Subsequently it fell sharply. Housing markets in the United States, the United Kingdom, Spain, Ireland, and other countries have risen markedly in the last few years. In mid to late 2007 the US housing market started to weaken as the sub-prime mortgage market began to collapse, and markets’ fears about the riskiness of opaque securitized mortgage-backed assets caused short-term inter-bank money markets to dry up globally. While the Federal Reserve and the European Central Bank pumped in liquidity, the Bank of England was more restrained, and a distressed British lender, Northern Rock, suffered a bank run, the first in the United Kingdom since 1860. There are fears that a substantial fall in house prices in the US may cause recession and slow down global growth.

Among asset prices, the exchange rate has featured prominently in debates about monetary policy, particularly in economies that target inflation. The exchange rate has a number of direct and indirect effects on inflation and real activity, and it introduces additional channels through which monetary policy can affect the economy, making it a potential policy target. At the same time it is well documented that exchange rates sometimes experience sustained

deviations from their long run equilibrium, followed by sudden corrections. The impact of these “unwarranted” exchange rate movements on macroeconomic performance has been a concern of central bankers and scholars.

As the dollar weakened in 2007 and the Euro rose to \$1.40 and beyond, there were calls from European politicians for the European Central Bank to trim its interest rate policy so as to manage the Euro. The United States continues to call on China to allow further upward adjustment of the Renminbi, in order to foster an orderly adjustment of the so-called “global imbalances”. There have been concerns in the United Kingdom that the pound has become overvalued relative to the dollar and the Euro. Iceland is an example of a very small country whose relatively high interest rates, needed to curb inflation, have attracted large speculative “carry trade” inflows, and whose exchange rate has become greatly overvalued as a result. There has been an ongoing debate over the last ten years as to how should central banks respond to these asset price movements. One widely held view is that an inflation-targetting central bank should not take asset prices into account when setting interest rates except insofar as they help to predict future inflation. This conclusion is reached by Bernanke and Gertler (1999). The opposing view is that central banks should adjust interest rates partly with a view to dampening bubbles in asset prices, on the basis that bubbles should not be allowed to grow large, because a large correction in the future could harm the economy more than a small one now. Representatives of this point of view include Cecchetti et al. (2000), who argue that central banks can improve macroeconomic performance by responding to asset prices as well as to expected inflation and to the output gap. In a similar vein, Ball (1999) shows that an interest rate policy rule that responds only to output and inflation, like a Taylor rule, is not optimal for an open economy. Svensson (2000), using a forward-looking model, concludes that the exchange rate can be a very useful instrument in stabilising Consumer Price Index (CPI)

inflation.

One of the obstacles to using the interest rate to dampen bubbles is that it is empirically very difficult to determine whether or not there is a bubble. Cecchetti et al. (2000) confront this problem and conclude that nevertheless it is worthwhile attempting to respond to movements that are believed to be bubbles. Wollmershäuser (2006) and Zampolli (2006) conclude that reacting to the exchange rate improves macroeconomic stability in models that incorporate exchange rate uncertainty. Wollmershäuser (2006) finds that monetary policy rules that include an exchange rate term are more robust to a high degree of uncertainty concerning the relationship between the nominal exchange rate and the nominal interest rate or other macroeconomic variables. Zampolli (2006) uses a simple backward-looking model of the type defined in Ball (1999) with a regime-switching exchange rate, aimed at capturing the complex behavior of financial markets. Despite these results, this is not a settled question. Batini and Nelson (2000), who model a bubble in the exchange rate as an exogenous process that temporarily shifts it away from its long-run equilibrium, find that responding to the exchange rate does not improve welfare in most cases, and may even lower it. Leitemo and Söderström (2005) analyze the impact of exchange rate uncertainty on the conduct of monetary policy and conclude that policy rules without an exchange rate term, namely a Taylor rule, are optimal for the stabilization of a small open economy. Gilchrist and Saito (2006) show that responding to perceived bubbles can improve performance, but it very much depends on the circumstances. When asset prices are driven also by changes in the rate of productivity growth which are not correctly measured by the policy makers, interventions become less useful and may actually be harmful.

While the theoretical literature has asked whether central banks should direct policy towards asset prices, the empirical question is whether or not they

actually appear to do it. Here again, the evidence is mixed. Some results, such as those of Clarida and Gertler (1997), suggest that central banks indirectly try to influence the exchange rate through movements in the interest rate. Lubik and Schorfheide (2007), who analyze different specifications of the monetary policy reaction function for four small open economies (Australia, Canada, New Zealand and United Kingdom) over the last two decades, conclude that the central banks of Canada and England include the nominal exchange rate in the policy rule, while those of Australia and New Zealand do not. Thus the normative question appears to have some relevance to actual policy.

In view of the continuing debate over the merits of using interest rates to dampen asset price bubbles, the present paper extends the analysis of Zampolli (2006). We follow that paper in allowing for regime-switching in exchange rate movements. This is intended to capture the idea that exchange rates have quiescent periods, when they appear to be driven largely by fundamentals, interspersed with periods when bubbles seem to develop. But the absence of forward-looking behavior in Zampolli (2006) prevents his model from capturing the essential role of expectations in monetary policy and asset markets. Therefore we consider a forward-looking open-economy model of the type used in Svensson (2000) and in Galí and Monacelli (2005).

We assume that the exchange rate may be in one of two states. In one regime it randomly oscillates around its equilibrium, defined by the real interest parity condition. In the other regime the deviations from equilibrium are persistent. We experiment a range of values for the transition probabilities and for the persistence coefficient. We assume that the transition probabilities are exogenous and known to policymakers. We therefore abstract from the issue of imperfect information concerning the process that drives the exchange rate.<sup>1</sup> Uncertainty in this context results from the policymaker not knowing in

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<sup>1</sup>Alexandre and Bação (2005) deal with this issue in the context of equity price

which regime the exchange rate will be in the next period. In other words, the policymaker observes the current state of the exchange rate process and knows the probability of the economy moving to a different state.

We start our analysis by comparing the optimal welfare loss when the policymaker faces no uncertainty about the nature of the shock to the real exchange rate and when policymakers are uncertain about the future state of the economy. Then we analyze the performance of simple policy rules, both with and without an exchange rate term, and evaluate their robustness in dealing with exchange rate uncertainty.

Finally, we evaluate the benefits from taking into account the switching nature of the economy by comparing the performance of time-invariant rules to regime-switching rules.

Section 2 describes our open-economy model and the monetary policy framework. Section 3 evaluates the welfare loss for a set of policy rules under exchange rate uncertainty. Section 4 checks the sensitivity and robustness of the results. Section 5 concludes.

## **2 An open economy with a regime-switching exchange rate**

The exchange rate introduces additional channels for monetary policy through its effects on aggregate demand and inflation. In Ball (1999), the change in the exchange rate affects inflation because it is passed directly into import prices. Following Svensson (2000) and Galí and Monacelli (2005), the inclusion of the exchange rate in our model adds three channels for monetary policy to affect the Consumer Price Index (CPI). First, it can affect inflation with a lag

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misalignments.

through its effect on aggregate demand. Second, the exchange rate can affect domestic inflation, and therefore the CPI, by affecting domestic currency prices of imported intermediate goods and, more indirectly, through its effects on nominal wages that depend on the evolution of the CPI. Finally, the exchange rate affects CPI inflation through its effects on domestic currency prices of imported final goods. Therefore, the model that we describe below tries to capture all these three effects. In our computations we start by calibrating the model using Svensson (2000) values for these parameters. Later we analyze the behavior of the economy using parameter values that correspond to a higher degree of openness. The lag structure of our model is such that it captures the often mentioned fact (see, e.g., Svensson (2000); Ball (1999)) that monetary policy can affect the consumer price index with a shorter lag through the exchange rate channels.

## 2.1 The model

Our stylized system of macroeconomic equations is the following:

$$y_t = E_t y_{t+1} - \alpha_1 (i_t - E_t \pi_{t+1}) + \alpha_2 y_{t-1}^* + \alpha_3 q_t + \varepsilon_t^d, \quad (1)$$

$$\pi_t^d = \beta_1 \pi_{t-1}^d + (1 - \beta_1) \beta E_t \pi_{t+1}^d + \beta_2 y_{t-1} + \beta_3 (q_t - q_{t-1}) + \varepsilon_t^s, \quad (2)$$

$$q_t = E_t q_{t+1} - i_t + E_t \pi_{t+1} + i_t^* - E_t \pi_{t+1}^* + \varepsilon_t^q, \quad (3)$$

$$\pi_t = \pi_t^d + \omega (q_t - q_{t-1}), \quad (4)$$

$$\varepsilon_t^s = \rho^s \varepsilon_{t-1}^s + e_t^s, \quad (5)$$

$$\varepsilon_t^d = \rho^d \varepsilon_{t-1}^d + e_t^d, \quad (6)$$

$$\varepsilon_t^q = \rho_{s_t}^q \varepsilon_{t-1}^q + e_t^q, \quad (7)$$

$$y_t^* = \rho_{y^*} y_{t-1}^* + e_t^{y^*}, \quad (8)$$

$$\pi_t^* = \rho_{\pi^*} \pi_{t-1}^* + e_t^{\pi^*}, \quad (9)$$

$$i_t^* = \rho_{i^*} i_{t-1}^* + \rho_{i^*}' y_t^* + e_t^{i^*}. \quad (10)$$



Eq. (1) is the aggregate demand equation for an open economy of the type used in Svensson (2000). Output depends on its own expected value, on the real interest rate, on the lagged foreign output,  $y_t^*$ , and on the real exchange rate,  $q$ . In this model the real exchange rate affects the aggregate demand because it affects the relative price between domestic and foreign goods: a higher  $q$  means depreciation, that is,  $q_t \equiv s_t + p_t^* - p_t$ , where  $s$  is the price of foreign currency in terms of domestic money,  $p_t^*$  and  $p_t$  are the foreign and domestic price levels, respectively. Additionally, output depends on a demand shock that we assume to follow an AR(1) process, as in Eq. (6). Following Svensson (2000) we set the following values for the coefficients in the aggregate demand equation:  $\alpha_1 = 0.6$ ,  $\alpha_2 = 0.05$  and  $\alpha_3 = 0.04$ .

Eq. (2) is a “hybrid” Phillips curve where  $\pi_t^d$  is domestic inflation. In face of the discussion and evidence provided in Galí and Gertler (1999), we have substituted lagged output for the marginal cost, and we also include some open-economy elements. Following the survey of empirical estimates presented in Rudebusch (2002), we consider the inflation persistence coefficient to be  $\beta_1 = 0.4$ . We set  $\beta = 0.99$  as in Galí and Gertler (1999), and  $\beta_2 = 0.13$  as in Rudebusch (2002). The inclusion of the change in the exchange rate in the domestic inflation equation aims at capturing its effect on domestic currency prices of imported intermediate goods. In our analysis, we follow Svensson (2000) and we set the pass-through parameter, that gives the impact of changes in the exchange rates on domestic inflation,  $\beta_3 = 0.01$ .

In equilibrium the uncovered interest parity condition holds, that is,  $i_t - i_t^* = E_t s_{t+1} - s_t$ . However, we assume that the exchange rate may deviate from its fundamental value due to an exchange-rate risk premium,  $\varepsilon_t^q$ . Using this assumption, Eq. (3) defines the real interest parity condition. Leitemo and Söderström (2005) and Wollmershäuser (2006) study the implications for monetary policy of uncertainty on the exchange rate model. In this paper we

assume there is no uncertainty concerning the exchange rate model. Uncertainty concerning the behavior of the exchange rate comes from a Markov-switching autoregressive coefficient in the exchange-rate risk premium shock.

Eq. (7) specifies the process for the shock in the exchange rate. We assume that the exchange rate may be in one of two states. In state 1,  $\rho_{st}^q > 0$  and therefore the exchange rate deviates persistently from its fundamental value. This state represents times of instability, where the exchange rate is “disconnected” from fundamentals for long periods.<sup>2</sup> In state 2,  $\rho_{st}^q = 0$  and thus the exchange rate is subject to random shocks that disturb it from its fundamental value, but without any persistence. The variance of the exogenous shock  $\varepsilon_t^q$  is the same across regimes, which implies that, as seems reasonable, the variance of  $\varepsilon_t^q$  increases in the first regime, and the higher the persistence the more it increases.

The state of the economy is assumed to evolve as a Markov chain with the following probability transition matrix:

$$P = \begin{bmatrix} p_{11} & p_{12} \\ p_{21} & p_{22} \end{bmatrix}. \quad (11)$$

where  $p_{ij} = 1 - p_{ii}$  (when  $i \neq j$ ) and  $p_{ij}$  is the probability of moving from state  $i$  in the current period to state  $j$  in the next period. In our computations we use the values 0.25, 0.5 and 0.75 for  $p_{ii}$ . In the single state model, we have  $\rho_1^q = \rho_2^q$  and thus the probability transition matrix becomes irrelevant. We also use a range of values for the autoregressive coefficient in the first regime: 0.5 (mild persistence), 0.9 (high persistence) and 1.1 (explosive).

Bordo and Jeanne (2002), in a three period model, assumed that monetary policy can affect the transition probabilities. Zampolli (2006) argues that

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<sup>2</sup>Several authors have provided rationales for the “disconnect puzzle” described in Obstfeld and Rogoff (2001). For example, De Grauwe and Grimaldi (2006) assume heterogeneous agents with different beliefs about the behavior of the exchange rate, which results in persistent deviations from equilibrium and non-linear behavior.

assuming exogenous transition probabilities is not unreasonable given the high degree of uncertainty about the stochastic properties of an asset price and their relationship with monetary policy. We follow this author and in our computations we assume that the transition probabilities are exogenous and observed by policymakers. We therefore abstract from the issue of imperfect information at this stage. In this context, the policymaker is uncertain only about the exchange rate regime in the next period.

In our analysis, only the parameters in the policy rules and the autoregressive coefficient of the risk premium may vary with the state. Other parameters do not adjust to changes in the state of the economy or to changes in policy rules. To the extent that the other parameters in the model do not only reflect preferences and technology, deep structural parameters, guaranteed to be invariant to policy rules, but also reflect behavioral rules, as in wage and price-setting, for example, our analysis may be subject to the Lucas critique. However, while this may be an issue in principle, we do not believe it is serious in practice.

Clarida et al. (2001) show that in an open economy it is important to distinguish between domestic inflation and consumer price inflation, as measured by the Consumer Price Index. These authors conclude that for an economy with perfect exchange-rate pass-through the central bank should target domestic inflation and let the exchange rate float. To take this into account we work with both measures of inflation. Eq. (4) defines CPI inflation,  $\pi$ , as a function of domestic inflation and the change in the real exchange rate (which captures the effects of a rise in the domestic-currency prices of imported foreign goods,  $\pi_t^f$ ),<sup>3</sup> where  $\omega$  is the share of imported goods in CPI. Through this effect the exchange rate can affect the CPI directly, and it allows monetary policy to

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<sup>3</sup>As described in Svensson (2000),  $\pi_t^f$  is given by  $\pi_t^f = p_t^f - p_{t-1}^f = \pi_t^* + s_t - s_{t-1} = \pi_t + q_t - q_{t-1}$ , where  $p_t^f = p_t^* + s_t$  is the domestic-currency price of imported foreign goods and  $\pi_t^*$  is foreign inflation.

affect CPI inflation with a shorter lag than through the aggregate demand channel. The effect of the exchange rate on the CPI depends on the weight of the domestic-currency inflation of imported foreign goods. Svensson (2000) sets  $\omega = 0.3$ . We use this openness degree as our benchmark, but later we consider alternative values.

As in Svensson (2000) we assume that foreign output and foreign inflation follow stationary AR(1) processes as described in Eq. (8) and Eq. (9), and we set  $\rho_{y^*} = \rho_{\pi^*} = 0.8$ , while the foreign interest rate is assumed to follow a Taylor rule — 10 — with  $\rho_{i^*} = 1.5$ ,  $\rho'_{i^*} = 0.5$ .

## 2.2 Policy rules and welfare

A Markov-switching rational expectations model requires adequate solution methods. Svensson and Williams (2005, henceforth SW) and Farmer et al. (2006, henceforth FWZ) propose two such methods. SW's method uses an iterative procedure similar to the one used to solve simple optimal linear quadratic regulator problems. FWZ rightly argue that SW's method does not tell us whether the solution is unique. FWZ propose a modification of Sims (2001) method to deal with the case of Markov-switching rational expectations while maintaining the ability to analyze the uniqueness of the solution. In this paper we employ SW's method to compute the optimal loss, and base our numerical optimization of simple rules on FWZ's method, selecting only rules that correspond to unique and stable solutions. The application of the SW and FWZ methods to our model is described in the Appendix.

Simple rules have been widely discussed among academics in monetary policy analysis. Several arguments have been used in its defense. On one hand, it has been argued that simple rules perform nearly as well as optimal rules (see, for example, Rudebusch and Svensson (1999)). On the other hand, it has been argued that simple rules are very robust to several types of uncertainty

(see, for example, Levin et al. (1999)). We therefore use simple rules to see how they compare to the optimal policy rule and how robust they are in dealing with exchange rate uncertainty. The different rules are summarized in Table 1.

We compute the optimal parameters for Taylor-type (denoted TR in Table 1) and inflation-forecast based (IFB) policy rules. In the Taylor-type policy rule the interest rate reacts to deviations of output and inflation from the target (assumed to be zero). Additionally, we look at the Taylor-type policy rule with an exchange rate term (denoted TR+q). As a benchmark, we also look at the performance of the Taylor rule as defined in Taylor (1993), denoted TRo. In our computations we assume that the policymaker reacts to CPI inflation. In section 4 we report results using domestic inflation instead of CPI inflation in our set of policy rules.

In the inflation-forecast based policy rule the interest rate responds to deviations of expected inflation from the target. We also consider an inflation-forecast based rule with an exchange rate term (IFB+q) — see Levin et al. (2003) for a discussion of the rationale and robustness of inflation-forecast based rules.

As in Zampolli (2006), we compute both time-invariant policy rules (denoted by an I) and regime-switching policy rules. The inclusion of time-invariant policy rules, where the switching nature of the exchange rate misalignments is not taken into consideration, is based on the argument that they could be a good option if the policymaker cannot observe the regime — see Zampolli (2006). Also, many of the rules are optimized over a restricted range of parameter values (and these are denoted by an R).

Several papers — see, for example, Kirsanova et al. (2006), and references therein — have discussed whether monetary policy should target domestic inflation or consumer price inflation. We start by considering a loss function that includes CPI inflation, the output gap and the change in the interest rate.

Later we assume a loss function that includes domestic inflation instead of CPI inflation. Therefore, the values of the parameters in policy rules are chosen so as to minimize the following loss function (also used by, e.g., Rudebusch and Svensson, 1999):

$$\text{Loss Function} = V(\pi_t) + V(y_t) + 0.5V(i_t - i_{t-1}), \quad (12)$$

where  $V(x)$  represents the unconditional variance of variable  $x$ , i.e., the policy rule aims at minimizing a weighted sum of the unconditional variances of output, CPI inflation and the change in the interest rate.

### 3 Monetary policy under exchange rate uncertainty

As mentioned in the introductory section, evidence from simulated open-economy models with exchange rate uncertainty on whether monetary policy should react to the exchange rate is mixed. Leitemo and Söderström (2005) analyze the impact of exchange rate uncertainty for the conduct of monetary policy and conclude that policy rules without an exchange rate term, namely a Taylor rule, are optimal at stabilizing a small open economy. However, Wollmershäuser (2006) and Zampolli (2006), in models that allow for uncertainty in the exchange rate, show that a reaction to the exchange rate is welfare enhancing. Wollmershäuser (2006) uses a model with uncertainty on the exchange rate model and concludes that monetary policy rules that include an exchange rate term are more robust.

Zampolli (2006) introduces a regime-switching exchange rate in a simple backward looking model. In his analysis policymakers are uncertain about the nature of the shock that hits the real exchange rate. Policymakers therefore have to assign probabilities to a transitory shock and to a very persistent or bubble shock. Zampolli (2006) then investigates how that type of uncertainty affects the optimal reaction of policy instruments and how that reaction depends on the transition probabilities that characterize the shock. He concludes that

an invariant Taylor rule performs significantly worse than the optimal policy when the probability of continuing in the bubble regime is high and the probability of continuing in the other regime is low. Zampolli also concludes that a time invariant Taylor rule that includes an exchange rate term performs noticeably better than a time invariant Taylor rule without an exchange rate term. A drawback of Zampolli's analysis is the absence of forward-looking behavior which prevents the model from capturing the essential role of expectations in monetary policy and in asset markets. Therefore, we extend Zampolli's analysis by considering an open-economy forward-looking model of the type described above.

Following Zampolli's strategy, we started by computing, as a benchmark, the value of the optimal loss when policymakers face no uncertainty about the nature of the shock on the real exchange rate, that is, they know it to be white noise. Results for this case and for optimized policy rules are presented in Table 2. In the case of optimized policy rules we restricted our attention to determinate solutions, as in Levin et al. (2003).

We then simulated the model and computed the optimal policy for different values of the transition probabilities and for different values of the autoregressive coefficient on the real exchange rate shock. We assumed the shock on the real exchange rate to be mildly persistent, very persistent or to be of the bubble type. The values for the transition probabilities and the autoregressive coefficients and the corresponding value of the central bank's loss are presented in Tables 3 to 6.<sup>4</sup>

The results in Table 3 show that introducing uncertainty in the behavior of the non-fundamental shock that affects the real exchange rate increases, as expected, the welfare loss. The welfare loss increase is higher when the

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<sup>4</sup>Tables 7 to 18 report the results for the variance of the output gap, inflation, exchange rate and interest rate for all policy rules and for the different degrees of persistence.

persistence of the non-fundamental shock is higher. It also increases with the probability of being in the regime where the non-fundamental shock to the real exchange rate is persistent, i.e., the loss increases with  $p_{11}$  and decreases with  $p_{22}$ . The effect on welfare is nonlinear: the effect is magnified as persistence increases towards (and beyond) unity. In fact, the values in Table 3 that stand out are those associated with high persistence ( $\rho_1^q = 1.1$ ) and high duration of the “bubble” period ( $p_{11} = 0.75$ ); the loss increases between 22% and 34% compared to the case with white noise deviations and without regime-switching in the exchange rate.

The Taylor and inflation–forecast based rules, described above and summarized in Table 1, perform much worse than the optimal policy. From the results presented in Tables 4, 5 and 6 we can see that the difference exceeds 30% of the optimal loss. We can also conclude that the optimized Taylor rule is always better than the corresponding inflation-forecast based rule, by a margin of at least 20%. The original Taylor rule is worse than an optimized Taylor rule by at least 7%. But it is usually better than an inflation-forecast based rule, except in our worst possible scenario:  $\rho_1^q = 1.1, p_{11} = 0.75, p_{22} = 0.25$ .

Optimized Taylor rules have coefficients that vary widely with the parameters of the model and tend to be extremely large, sometimes even exceeding 2000. However, restricting the coefficients not to exceed 5, so as not to be too far from the original coefficients and from the coefficients employed in other studies, does not affect the loss very much: the difference is below 0.7% (see Tables 4 and 5). The optimized parameters of IFB rules are always between 1.5 and 2.5 for  $E_t\pi_{t+1}$ , and between 0 and 0.3 for  $q_t$ .

Reacting to the exchange rate does not yield large dividends in the case of the Taylor rule: the difference is less than 0.8%. The optimized Taylor rule without an exchange rate term seems to be robust in the context of regime-switching in the exchange rate. These results, presented in Table 4,



appear to reinforce the findings of Leitemo and Söderström (2005). Taylor (2001) argues that the indirect response to the exchange rate through the output gap and inflation terms in the policy rule severely reduces the benefits from reacting directly to the exchange rate. This indirect effect may be at work in our model.

However, in the case of an inflation-based forecast rule (results in Table 6), the benefit from reacting to the exchange rate is never below 7% and may even go beyond 20%. Again, significant benefits from reacting to the exchange rate arise when the shock and the bubble-regime are very persistent:  $\rho_1^q = 1.1, p_{11} = 0.75$ . Welfare gains from the reaction to the exchange rate result from a more stable output, inflation and policy instrument. Batini et al. (2003) find similar results for the time-invariant case.

In order to evaluate the benefits from switching the policy rule coefficients according to the exchange rate regime we compare the performance of time invariant rules to regime-switching rules. The results for the case of the inflation-based forecast rule, presented in Table 6, show that an optimized time invariant rule leads to an increase in welfare loss of less than 0.2%, i.e., taking into account the switching nature of the economy does not bring significant benefits, both when the policy rule includes an exchange rate term and when it does not.

In the case of the Taylor rule, comparing the results in Tables 4 and 5, we conclude that the use of an optimized time invariant rule leads to an increase in welfare loss below 0.5%, in general. However, the difference goes up to 6% in our worst scenario ( $\rho_1^q = 1.1, p_{11} = 0.75, p_{22} = 0.25$ ). It appears that taking into account the switching nature of the economy is important only in extreme cases. The same applies to the case where a restricted, optimized, time-invariant Taylor rule is used, though the difference in welfare loss is slightly bigger. These results seem to corroborate the findings of Zampolli (2006) in the context of a

backward-looking model.

In order to check the sensitivity and the robustness of the results, in the next section we present our computations with a higher degree of openness and with a loss function and policy rules that include domestic inflation instead of the CPI inflation.

## 4 Sensitivity and robustness analysis

The exchange rate parameters in the IS, Phillips curve and CPI equations are crucial for the working of the transmission mechanism through the exchange rate channel. These parameters determine the exposure of the economy to exchange rate shocks. Therefore, we start our sensitivity analysis by checking the robustness of the baseline results to an increase in the degree of openness. For that purpose we use parameter values similar to those estimated for Scandinavian economies. In these countries, the import/GDP ratio is around 0.4, which is the new value for the coefficient  $\omega$  in CPI equation, Eq. (4). The new coefficient for the real exchange rate in the aggregate demand equation,  $\alpha_3$ , is 0.1. The Phillips curve pass-through parameter,  $\beta_3$ , is equal to 0.1. These parameters are based on the estimates of Lubik and Schorfheide (2007) and Hunt (2006).

The results obtained for the new parameters are very similar to the results obtained for the baseline parameters. The only fact to notice from the new computations is the difficulty of finding a unique stable solution for the IFB rule when it does not include an exchange rate term.

In our computations we considered a loss function that is a weighted sum of the unconditional variances of output, interest rate and CPI inflation. The inclusion of CPI inflation in the policymaker's objective function combines both the domestic inflation and the exchange rate, see Eq. (4). Benigno and Benigno (2003), De Paoli (2006) and Leith and Wren-Lewis (2007) show

that social welfare functions for open economies include the terms of trade gap. However, Kirsanova et al. (2006) note that including an exchange rate term explicitly, or implicitly through the CPI inflation, in the welfare function remains unorthodox.<sup>5</sup> Additionally, Clarida et al. (2001), Galí and Monacelli (2005), among other authors, show that there may be an isomorphism between welfare functions in closed and open economies. These authors derived social welfare functions for open economies directly from the consumer’s utility function and concluded that the policymaker’s objective function for an open economy can be written as a quadratic function in output and domestic inflation. In order to check the robustness of our results to the form of the policymakers’s loss function we conduct our computations considering a loss function that is a weighted sum of the unconditional variances of output, interest rate and domestic inflation. The policy rule parameters are then chosen such that they minimize the following loss function:

$$Loss\ Function = V(\pi_t^d) + V(y_t) + 0.5V(i_t - i_{t-1}). \quad (13)$$

From the computations for the new loss function we conclude that our baseline results are robust, as they do not seem to depend on whether domestic or CPI inflation is included in the policymaker’s objective function.

Svensson (2000) considers two versions of the Taylor rule, one in which the policy instrument responds to CPI inflation and another in which it reacts to domestic inflation. Galí and Monacelli (2005) define a policy rule in which the interest rule responds to deviations of domestic inflation and/or the output gap from the target, on the basis that a rule of that type can avoid indeterminacy problems. Following these authors, substitute domestic inflation for CPI inflation in the policy rules described in Table 1, both for the new calibration and for the

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<sup>5</sup>Although Kirsanova et al. (2006) give an example where the inclusion of terms of trade or real exchange rate gap may be justified. These authors also emphasize that the derivations of social welfare functions from consumers’ utility depend on the structure of the model.

new loss function. In general, we conclude that reacting to domestic inflation is worse than reacting to CPI inflation. Adolfson (2007), in a model with imperfect exchange rate pass-through, also concludes that reacting to CPI inflation is better than reacting to domestic inflation. As argued in Taylor (2001) this result may be explained by the indirect reaction to the exchange rate when the interest rate reacts to CPI inflation.

To conclude, the baseline results remain fairly robust when we consider a higher degree of openness and when we consider domestic inflation in the policymaker's objective function and in the Taylor and IFB policy rules. The only result to be stressed is the difficulty of finding a unique stable solution for the IFB rule, in the very open economy case, when it does not include an exchange rate term. Levin et al. (2003) show that the inclusion of an output gap term and a lagged interest rate term makes the inflation-forecast based rule more robust and reduces the region of indeterminacy.

## 5 Conclusion

Evidence from simulated open-economy models with exchange rate uncertainty on whether monetary policy should react to the exchange rate is mixed. We study this issue in a Markov-switching model. In our model the exchange rate may be in one of two states: in one regime it randomly oscillates around its equilibrium; in the other regime the deviations from equilibrium are persistent. The welfare loss increases with the persistence of the non-fundamental shock and with the probability of being in the regime where the misalignment in the exchange rate is persistent. We assume that the transition probabilities are exogenous and observed by policymakers, and that the current state is known to policymakers. Despite the difficulties of anticipating the effects of monetary policy on financial markets, future research should look at models

with unobserved and endogenous transition probabilities along the lines of Davig and Leeper (2006).

In our model, simple policy rules perform much worse than the optimal policy. Optimized Taylor rules are always better than the corresponding inflation-forecast based rule. The optimized Taylor rule without an exchange rate term seems to be robust in the context of exchange rate uncertainty. However, significant welfare gains from adding an exchange rate term to the inflation-based forecast rule arise when the shock and the bubble-regime are very persistent.

Finally, we evaluate the benefits from taking into account the switching nature of the economy by comparing the performance of time invariant rules to regime switching rules. We conclude that taking into account the regime-switching in the exchange rate, both for the Taylor rule and for the inflation-based forecast rule, does not bring significant benefits. However, when the shock and the bubble-regime are very persistent an optimized time invariant Taylor rule can increase the welfare loss significantly.

Our results for a forward-looking model seem to corroborate the results that Zampolli (2006) obtained in the context of a backward-looking model. Taking into account the switching nature of the economy is important only in extreme cases. Computations for a higher degree of openness and for domestic inflation in the policymaker's objective function and in the Taylor and IFB policy rules show the robustness of the baseline results.

# Appendix

We employed the Svensson-Williams method to find the optimal policy in a Markov-switching model of the form:

$$\begin{bmatrix} X_{t+1} \\ H_{s_t} E_t x_{t+1} \end{bmatrix} = A_{s_t} \begin{bmatrix} X_t \\ x_t \end{bmatrix} + B_{s_t} i_t + \begin{bmatrix} C_{s_t} \\ 0 \end{bmatrix} e_{t+1}, \quad (14)$$

where  $H_{s_t}$ ,  $A_{s_t}$ ,  $B_{s_t}$ ,  $C_{s_t}$  are Markov-switching matrices,  $i_t$  is the control variable (in our model, the nominal interest rate) and  $s_t$  is the state.

In our model, we defined:

$$X_t = (\varepsilon_t^s, \varepsilon_t^d, \varepsilon_t^q, y_t^*, \pi_t^*, i_t^*, y_{t-1}^*, i_{t-1}^*, y_{t-1}, q_{t-1}, \pi_{t-1}^d)', \quad (15)$$

$$x_t = (y_t, \pi_t^d, q_t, \pi_t)', \quad (16)$$

$$e_t = (e_t^s, e_t^d, e_t^q, e_t^{y^*}, e_t^{\pi^*}, e_t^{i^*})', \quad (17)$$

$$H_{s_t} = \begin{bmatrix} 1 & 0 & 0 & \alpha_1 \\ 0 & (1 - \beta_1)\beta & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}, \quad (18)$$

$$A_{st} = \begin{bmatrix} \rho^s & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \rho^d & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \rho_{st}^a & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \rho_{y^*} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \rho_{\pi^*} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \rho'_{i^*} \rho_{y^*} & \rho_{i^*} \rho_{\pi^*} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 & -\alpha_2 & 0 & 0 & 0 & 0 & 1 & 0 & -\alpha_3 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -\beta_2 & \beta_3 & -\beta_1 & 0 & 1 & -\beta_3 & 0 \\ 0 & 0 & -1 & 0 & \rho_{\pi^*} & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \omega & 0 & 0 & -1 & -\omega & 1 \end{bmatrix}, \quad (19)$$

$$B_{st} = (0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, \alpha_1, 0, 1, 0)', \quad (20)$$

$$C_{st} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & \rho'_{i^*} & \rho_{i^*} & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}. \quad (21)$$

The Farmer-Waggoner-Zha method was used to solve, with an arbitrary policy rule, a Markov-switching model of the form:

$$\begin{bmatrix} a_1(s_t) \\ a_2 \end{bmatrix} x_t = \begin{bmatrix} b_1(s_t) \\ b_2 \end{bmatrix} x_{t-1} + \begin{bmatrix} \Psi(s_t) \\ 0 \end{bmatrix} e_t + \begin{bmatrix} 0 \\ \Pi \end{bmatrix} \eta_t, \quad (22)$$

where  $e_t$  are exogenous i.i.d. variables,  $\eta_t$  is the vector of expectational errors and the vector  $x_t$  includes expected values.

In our model, we defined:

$$x_t = (\varepsilon_t^s, \varepsilon_t^d, \varepsilon_t^q, y_t^*, \pi_t^*, i_t^*, i_t, i_{t-1}, y_t, \pi_t^d, q_t, p i_t, E_t y_{t+1}, E_t \pi_{t+1}^d, E_t q_{t+1}, E_t \pi_{t+1})', \quad (23)$$

$$e_t = (e_t^s, e_t^d, e_t^q, e_t^{y^*}, e_t^{\pi^*}, e_t^{i^*})', \quad (24)$$

$$\eta_t = (\eta_t^y, \eta_t^{\pi^d}, \eta_t^q, \eta_t^\pi)'. \quad (25)$$

$$a_1(s_t) = \begin{bmatrix} 0 & -1 & 0 & 0 & 0 & 0 & \alpha_1 & 0 & 1 & 0 & -\alpha_3 & 0 & -1 & 0 & 0 & -\alpha_1 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & -\beta_3 & 0 & 0 & -(1-\beta_1)\beta & 0 & 0 \\ 0 & 0 & -1 & 0 & \rho_{\pi^*} & -1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & -1 & -1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & -\omega & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -\rho_{i^*} & -\rho_{i^*} & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \quad (26)$$

$$a_2 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \quad (27)$$



$$b_1(s_t) = \begin{bmatrix} 0 & -1 & 0 & 0 & 0 & 0 & \alpha_1 & 0 & 1 & 0 & -\alpha_3 & 0 & -1 & 0 & 0 & -\alpha_1 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & -\beta_3 & 0 & 0 & -(1-\beta_1)\beta & 0 & 0 \\ 0 & 0 & -1 & 0 & \rho_{\pi^*} & -1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & -1 & -1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & -\omega & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -\rho'_{i^*} & -\rho_{i^*} & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & -\delta_{s_t}^y & -\delta_{s_t}^{\pi^d} & -\delta_{s_t}^q & -\delta_{s_t}^{\pi} & 0 & -\delta_{s_t}^{\varepsilon^d} & 0 & -\delta_{s_t}^{\varepsilon} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \quad (28)$$

$$b_2 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix}, \quad (29)$$

$$\Psi(s_t) = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \quad (30)$$

$$\Pi = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}. \quad (31)$$

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# Tables

Table 1: Simple policy rules

| Rule    | Formula   |
|---------|---|
| TRo     | $i_t = 1.5\pi_t + 0.5y_t$   |
| TR+q    | $i_t = \delta_{s_t}^\pi \pi_t + \delta_{s_t}^y y_t + \delta_{s_t}^q q_t$  |
| TR      | $i_t = \delta_{s_t}^\pi \pi_t + \delta_{s_t}^y y_t$   |
| TR+q R  | $i_t = \delta_{s_t}^\pi \pi_t + \delta_{s_t}^y y_t + \delta_{s_t}^q q_t, \delta_{s_t}^\pi, \delta_{s_t}^y \in [0, 5], \delta_{s_t}^q \in [-1, 1]$ |
| TR R    | $i_t = \delta_{s_t}^\pi \pi_t + \delta_{s_t}^y y_t, \delta_{s_t}^\pi, \delta_{s_t}^y \in [0, 5]$  |
| TR+q RI | $i_t = \delta^\pi \pi_t + \delta^y y_t + \delta^q q_t, \delta^\pi, \delta^y \in [0, 5], \delta^q \in [-1, 1]$                                     |
| TR RI   | $i_t = \delta^\pi \pi_t + \delta^y y_t, \delta^\pi, \delta^y \in [0, 5]$  |
| TR+q I  | $i_t = \delta^\pi \pi_t + \delta^y y_t + \delta^q q_t$  |
| TR I    | $i_t = \delta^\pi \pi_t + \delta^y y_t$   |
| IFB+q   | $i_t = \delta_{s_t}^e E_t \pi_{t+1} + \delta_{s_t}^q q_t$   |
| IFB     | $i_t = \delta_{s_t}^e E_t \pi_{t+1}$  |
| IFB+q I | $i_t = \delta^e E_t \pi_{t+1} + \delta^q q_t$   |
| IFB I   | $i_t = \delta^e E_t \pi_{t+1}$  |

Table 2: Loss with one regime

| Policy          | $\rho_1^q = \rho_2^q$ |        |        |
|-----------------|-----------------------|--------|--------|
|                 | 0.0                   | 0.5    | 0.9    |
| Optimal         | 14.352                | 14.536 | 17.123 |
| TR+q            | 19.117                | 19.533 | 24.750 |
| TR              | 19.142                | 19.543 | 24.785 |
| TR+q R          | 19.233                | 19.648 | 24.775 |
| TR R            | 19.253                | 19.657 | 24.877 |
| TR <sub>o</sub> | 20.721                | 21.098 | 27.933 |
| IFB+q           | 28.423                | 28.509 | 32.227 |
| IFB             | 30.534                | 30.770 | 37.636 |



Table 3: Loss: Optimal policy and the original Taylor rule

|            |          | Optimal  |        |        | TRo      |        |        |
|------------|----------|----------|--------|--------|----------|--------|--------|
|            |          | $p_{22}$ |        |        | $p_{22}$ |        |        |
| $\rho_1^q$ | $p_{11}$ | 0.25     | 0.50   | 0.75   | 0.25     | 0.50   | 0.75   |
| 0.5        | 0.25     | 14.405   | 14.394 | 14.379 | 20.831   | 20.808 | 20.776 |
| 0.5        | 0.50     | 14.426   | 14.414 | 14.394 | 20.873   | 20.848 | 20.810 |
| 0.5        | 0.75     | 14.464   | 14.451 | 14.427 | 20.950   | 20.930 | 20.892 |
| 0.9        | 0.25     | 14.500   | 14.470 | 14.426 | 21.038   | 20.968 | 20.876 |
| 0.9        | 0.50     | 14.633   | 14.586 | 14.509 | 21.301   | 21.209 | 21.067 |
| 0.9        | 0.75     | 15.041   | 14.965 | 14.813 | 22.169   | 22.080 | 21.885 |
| 1.1        | 0.25     | 14.584   | 14.538 | 14.468 | 21.266   | 21.127 | 20.966 |
| 1.1        | 0.50     | 14.963   | 14.863 | 14.693 | 22.103   | 21.791 | 21.428 |
| 1.1        | 0.75     | 19.155   | 18.627 | 17.563 | 31.541   | 27.840 | 25.581 |

Table 4: Loss: optimized Taylor rule

|            |          | TR+q     |        |        | TR       |        |        |
|------------|----------|----------|--------|--------|----------|--------|--------|
|            |          | $p_{22}$ |        |        | $p_{22}$ |        |        |
| $\rho_1^q$ | $p_{11}$ | 0.25     | 0.50   | 0.75   | 0.25     | 0.50   | 0.75   |
| 0.5        | 0.25     | 19.239   | 19.214 | 19.179 | 19.260   | 19.236 | 19.203 |
| 0.5        | 0.50     | 19.286   | 19.261 | 19.220 | 19.306   | 19.282 | 19.242 |
| 0.5        | 0.75     | 19.373   | 19.354 | 19.314 | 19.390   | 19.371 | 19.334 |
| 0.9        | 0.25     | 19.481   | 19.405 | 19.302 | 19.501   | 19.428 | 19.327 |
| 0.9        | 0.50     | 19.770   | 19.677 | 19.525 | 19.790   | 19.698 | 19.547 |
| 0.9        | 0.75     | 20.621   | 20.561 | 20.406 | 20.632   | 20.574 | 20.420 |
| 1.1        | 0.25     | 19.753   | 19.599 | 19.414 | 19.771   | 19.623 | 19.439 |
| 1.1        | 0.50     | 20.604   | 20.320 | 19.936 | 20.629   | 20.325 | 19.958 |
| 1.1        | 0.75     | 27.304   | 25.284 | 23.828 | 27.309   | 25.313 | 23.864 |

  

|            |          | TR+q R   |        |        | TR R     |        |        |
|------------|----------|----------|--------|--------|----------|--------|--------|
|            |          | $p_{22}$ |        |        | $p_{22}$ |        |        |
| $\rho_1^q$ | $p_{11}$ | 0.25     | 0.50   | 0.75   | 0.25     | 0.50   | 0.75   |
| 0.5        | 0.25     | 19.357   | 19.331 | 19.295 | 19.375   | 19.350 | 19.315 |
| 0.5        | 0.50     | 19.404   | 19.377 | 19.335 | 19.421   | 19.395 | 19.354 |
| 0.5        | 0.75     | 19.489   | 19.469 | 19.427 | 19.504   | 19.484 | 19.444 |
| 0.9        | 0.25     | 19.592   | 19.515 | 19.413 | 19.612   | 19.535 | 19.433 |
| 0.9        | 0.50     | 19.872   | 19.779 | 19.628 | 19.892   | 19.798 | 19.647 |
| 0.9        | 0.75     | 20.725   | 20.663 | 20.488 | 20.743   | 20.676 | 20.502 |
| 1.1        | 0.25     | 19.850   | 19.699 | 19.519 | 19.874   | 19.721 | 19.539 |
| 1.1        | 0.50     | 20.708   | 20.401 | 20.025 | 20.733   | 20.421 | 20.043 |
| 1.1        | 0.75     | 27.427   | 25.388 | 23.892 | 27.460   | 25.426 | 23.959 |

Table 5: Loss: invariant optimized Taylor rule

|            |          | TR+q I   |        |        | TR I     |        |        |
|------------|----------|----------|--------|--------|----------|--------|--------|
|            |          | $p_{22}$ |        |        | $p_{22}$ |        |        |
| $\rho_1^q$ | $p_{11}$ | 0.25     | 0.50   | 0.75   | 0.25     | 0.50   | 0.75   |
| 0.5        | 0.25     | 19.241   | 19.216 | 19.180 | 19.260   | 19.237 | 19.203 |
| 0.5        | 0.50     | 19.289   | 19.264 | 19.221 | 19.307   | 19.283 | 19.243 |
| 0.5        | 0.75     | 19.375   | 19.356 | 19.315 | 19.391   | 19.373 | 19.334 |
| 0.9        | 0.25     | 19.490   | 19.412 | 19.306 | 19.505   | 19.430 | 19.328 |
| 0.9        | 0.50     | 19.788   | 19.691 | 19.532 | 19.799   | 19.705 | 19.551 |
| 0.9        | 0.75     | 20.693   | 20.620 | 20.427 | 20.694   | 20.622 | 20.431 |
| 1.1        | 0.25     | 19.770   | 19.611 | 19.420 | 19.784   | 19.629 | 19.442 |
| 1.1        | 0.50     | 20.698   | 20.362 | 19.955 | 20.703   | 20.370 | 19.968 |
| 1.1        | 0.75     | 28.807   | 25.935 | 24.001 | 28.886   | 25.986 | 24.034 |
|            |          | TR+q RI  |        |        | TR RI    |        |        |
|            |          | $p_{22}$ |        |        | $p_{22}$ |        |        |
| $\rho_1^q$ | $p_{11}$ | 0.25     | 0.50   | 0.75   | 0.25     | 0.50   | 0.75   |
| 0.5        | 0.25     | 19.359   | 19.332 | 19.296 | 19.375   | 19.350 | 19.315 |
| 0.5        | 0.50     | 19.406   | 19.379 | 19.336 | 19.421   | 19.396 | 19.354 |
| 0.5        | 0.75     | 19.491   | 19.470 | 19.428 | 19.504   | 19.485 | 19.444 |
| 0.9        | 0.25     | 19.600   | 19.521 | 19.416 | 19.614   | 19.537 | 19.434 |
| 0.9        | 0.50     | 19.889   | 19.791 | 19.634 | 19.898   | 19.803 | 19.649 |
| 0.9        | 0.75     | 20.775   | 20.698 | 20.506 | 20.775   | 20.699 | 20.509 |
| 1.1        | 0.25     | 19.867   | 19.709 | 19.523 | 19.879   | 19.725 | 19.541 |
| 1.1        | 0.50     | 20.768   | 20.437 | 20.039 | 20.771   | 20.443 | 20.050 |
| 1.1        | 0.75     | 28.817   | 25.949 | 24.029 | 28.960   | 26.025 | 24.074 |

Table 6: Loss: inflation forecast based rule

|            |          | IFB+q    |        |        | IFB      |        |        |
|------------|----------|----------|--------|--------|----------|--------|--------|
|            |          | $p_{22}$ |        |        | $p_{22}$ |        |        |
| $\rho_1^q$ | $p_{11}$ | 0.25     | 0.50   | 0.75   | 0.25     | 0.50   | 0.75   |
| 0.5        | 0.25     | 28.422   | 28.418 | 28.418 | 30.586   | 30.573 | 30.559 |
| 0.5        | 0.50     | 28.428   | 28.425 | 28.424 | 30.610   | 30.597 | 30.579 |
| 0.5        | 0.75     | 28.451   | 28.448 | 28.446 | 30.661   | 30.651 | 30.632 |
| 0.9        | 0.25     | 28.519   | 28.485 | 28.454 | 30.799   | 30.733 | 30.654 |
| 0.9        | 0.50     | 28.629   | 28.584 | 28.529 | 31.031   | 30.937 | 30.808 |
| 0.9        | 0.75     | 29.121   | 29.060 | 28.940 | 31.868   | 31.729 | 31.495 |
| 1.1        | 0.25     | 28.652   | 28.571 | 28.496 | 31.083   | 30.920 | 30.751 |
| 1.1        | 0.50     | 29.079   | 28.894 | 28.704 | 31.934   | 31.536 | 31.141 |
| 1.1        | 0.75     | 34.528   | 32.421 | 30.971 | 41.639   | 37.125 | 34.543 |

  

|            |          | IFB+q I  |        |        | IFB I    |        |        |
|------------|----------|----------|--------|--------|----------|--------|--------|
|            |          | $p_{22}$ |        |        | $p_{22}$ |        |        |
| $\rho_1^q$ | $p_{11}$ | 0.25     | 0.50   | 0.75   | 0.25     | 0.50   | 0.75   |
| 0.5        | 0.25     | 28.422   | 28.418 | 28.418 | 30.586   | 30.573 | 30.559 |
| 0.5        | 0.50     | 28.428   | 28.425 | 28.424 | 30.610   | 30.597 | 30.579 |
| 0.5        | 0.75     | 28.451   | 28.448 | 28.446 | 30.661   | 30.651 | 30.632 |
| 0.9        | 0.25     | 28.520   | 28.486 | 28.454 | 30.799   | 30.733 | 30.655 |
| 0.9        | 0.50     | 28.629   | 28.584 | 28.530 | 31.031   | 30.937 | 30.808 |
| 0.9        | 0.75     | 29.123   | 29.063 | 28.942 | 31.868   | 31.729 | 31.496 |
| 1.1        | 0.25     | 28.654   | 28.572 | 28.496 | 31.084   | 30.921 | 30.752 |
| 1.1        | 0.50     | 29.079   | 28.894 | 28.705 | 31.936   | 31.537 | 31.141 |
| 1.1        | 0.75     | 34.576   | 32.472 | 31.008 | 41.712   | 37.162 | 34.562 |

Table 7: Variance of the exchange rate - 1

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | Optimal | TR+q   | TR     | IFB+q  | IFB    | TRo    | TR+q R |
|----------|----------|------------|---------|--------|--------|--------|--------|--------|--------|
| 0.25     | 0.25     | 0.5        | 44.263  | 46.725 | 45.423 | 44.597 | 56.045 | 43.301 | 46.255 |
| 0.25     | 0.5      | 0.5        | 44.143  | 46.657 | 45.31  | 44.421 | 55.79  | 43.156 | 46.172 |
| 0.25     | 0.75     | 0.5        | 43.983  | 46.565 | 45.163 | 44.182 | 55.446 | 42.964 | 46.047 |
| 0.5      | 0.25     | 0.5        | 44.522  | 46.924 | 45.652 | 44.92  | 56.547 | 43.6   | 46.465 |
| 0.5      | 0.5      | 0.5        | 44.374  | 46.815 | 45.506 | 44.712 | 56.239 | 43.418 | 46.344 |
| 0.5      | 0.75     | 0.5        | 44.152  | 46.663 | 45.295 | 44.393 | 55.774 | 43.148 | 46.17  |
| 0.75     | 0.25     | 0.5        | 45.058  | 47.287 | 46.129 | 45.547 | 57.529 | 44.212 | 46.895 |
| 0.75     | 0.5      | 0.5        | 44.895  | 47.178 | 45.957 | 45.324 | 57.2   | 44.003 | 46.752 |
| 0.75     | 0.75     | 0.5        | 44.594  | 46.936 | 45.649 | 44.911 | 56.594 | 43.627 | 46.481 |
| 0.25     | 0.25     | 0.9        | 45.23   | 47.623 | 46.431 | 45.99  | 58.254 | 44.652 | 47.263 |
| 0.25     | 0.5      | 0.9        | 44.866  | 47.298 | 45.986 | 45.399 | 57.351 | 44.088 | 46.864 |
| 0.25     | 0.75     | 0.9        | 44.404  | 46.874 | 45.49  | 44.7   | 56.285 | 43.444 | 46.398 |
| 0.5      | 0.25     | 0.9        | 47.182  | 49.355 | 48.319 | 48.264 | 61.863 | 47.023 | 49.066 |
| 0.5      | 0.5      | 0.9        | 46.503  | 48.512 | 47.359 | 47.14  | 60.157 | 45.869 | 48.171 |
| 0.5      | 0.75     | 0.9        | 45.513  | 47.507 | 46.227 | 45.734 | 58.003 | 44.467 | 47.086 |
| 0.75     | 0.25     | 0.9        | 56.875  | 57.495 | 57.402 | 58.652 | 76.441 | 57.776 | 57.587 |
| 0.75     | 0.5      | 0.9        | 55.237  | 54.9   | 54.356 | 55.389 | 72.107 | 54.417 | 54.67  |
| 0.75     | 0.75     | 0.9        | 52.23   | 50.999 | 50.341 | 50.873 | 65.956 | 49.79  | 50.693 |
| 0.25     | 0.25     | 1.1        | 46.12   | 49.013 | 47.834 | 47.745 | 61.068 | 46.474 | 48.744 |
| 0.25     | 0.5      | 1.1        | 45.532  | 48.056 | 46.754 | 46.417 | 59.018 | 45.131 | 47.691 |
| 0.25     | 0.75     | 1.1        | 44.791  | 47.196 | 45.789 | 45.143 | 57.031 | 43.884 | 46.735 |
| 0.5      | 0.25     | 1.1        | 52.247  | 56.288 | 55.391 | 56.39  | 74.257 | 55.592 | 55.981 |
| 0.5      | 0.5      | 1.1        | 50.603  | 52.048 | 51.07  | 51.619 | 67.225 | 50.584 | 51.811 |
| 0.5      | 0.75     | 1.1        | 48.166  | 48.768 | 47.689 | 47.606 | 61.13  | 46.413 | 48.436 |
| 0.75     | 0.25     | 1.1        | 207.04  | 210.14 | 211.03 | 226.71 | 277.5  | 225.5  | 209.36 |
| 0.75     | 0.5      | 1.1        | 188.17  | 115.68 | 116.73 | 126.74 | 159.42 | 125.11 | 115.34 |
| 0.75     | 0.75     | 1.1        | 151.52  | 70.244 | 71.464 | 77.02  | 99.965 | 75.595 | 70.084 |

Table 8: Variance of the exchange rate - 2

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | TR R   | TR+q RI | TR RI  | TR+q I | TR I   | IFB+q I | IFB I  |
|----------|----------|------------|--------|---------|--------|--------|--------|---------|--------|
| 0.25     | 0.25     | 0.5        | 45.081 | 46.252  | 45.081 | 46.659 | 45.404 | 44.597  | 56.045 |
| 0.25     | 0.5      | 0.5        | 44.967 | 46.165  | 44.964 | 46.607 | 45.295 | 44.421  | 55.79  |
| 0.25     | 0.75     | 0.5        | 44.825 | 46.045  | 44.812 | 46.564 | 45.157 | 44.181  | 55.446 |
| 0.5      | 0.25     | 0.5        | 45.324 | 46.466  | 45.321 | 46.853 | 45.635 | 44.919  | 56.547 |
| 0.5      | 0.5      | 0.5        | 45.172 | 46.349  | 45.171 | 46.81  | 45.494 | 44.711  | 56.239 |
| 0.5      | 0.75     | 0.5        | 44.96  | 46.165  | 44.952 | 46.64  | 45.289 | 44.393  | 55.774 |
| 0.75     | 0.25     | 0.5        | 45.822 | 46.894  | 45.821 | 47.252 | 46.108 | 45.547  | 57.529 |
| 0.75     | 0.5      | 0.5        | 45.644 | 46.753  | 45.643 | 47.179 | 45.943 | 45.323  | 57.2   |
| 0.75     | 0.75     | 0.5        | 45.328 | 46.482  | 45.326 | 46.901 | 45.648 | 44.91   | 56.593 |
| 0.25     | 0.25     | 0.9        | 46.154 | 47.256  | 46.151 | 47.579 | 46.413 | 45.994  | 58.257 |
| 0.25     | 0.5      | 0.9        | 45.687 | 46.864  | 45.685 | 47.239 | 45.978 | 45.401  | 57.353 |
| 0.25     | 0.75     | 0.9        | 45.172 | 46.404  | 45.165 | 46.874 | 45.49  | 44.7    | 56.286 |
| 0.5      | 0.25     | 0.9        | 48.124 | 49.052  | 48.115 | 49.347 | 48.307 | 48.267  | 61.867 |
| 0.5      | 0.5      | 0.9        | 47.126 | 48.171  | 47.121 | 48.534 | 47.362 | 47.139  | 60.159 |
| 0.5      | 0.75     | 0.9        | 45.947 | 47.093  | 45.947 | 47.52  | 46.225 | 45.733  | 58.004 |
| 0.75     | 0.25     | 0.9        | 57.418 | 57.501  | 57.37  | 57.663 | 57.281 | 58.642  | 76.44  |
| 0.75     | 0.5      | 0.9        | 54.353 | 54.64   | 54.34  | 54.868 | 54.335 | 55.369  | 72.106 |
| 0.75     | 0.75     | 0.9        | 50.222 | 50.726  | 50.239 | 50.993 | 50.359 | 50.849  | 65.955 |
| 0.25     | 0.25     | 1.1        | 47.644 | 48.744  | 47.636 | 49.012 | 47.827 | 47.761  | 61.081 |
| 0.25     | 0.5      | 1.1        | 46.511 | 47.703  | 46.506 | 48.09  | 46.762 | 46.425  | 59.026 |
| 0.25     | 0.75     | 1.1        | 45.49  | 46.745  | 45.489 | 47.182 | 45.805 | 45.145  | 57.035 |
| 0.5      | 0.25     | 1.1        | 55.403 | 55.957  | 55.361 | 56.029 | 55.262 | 56.396  | 74.278 |
| 0.5      | 0.5      | 1.1        | 51.004 | 51.815  | 50.992 | 52.01  | 51.047 | 51.617  | 67.235 |
| 0.5      | 0.75     | 1.1        | 47.44  | 48.45   | 47.446 | 48.785 | 47.647 | 47.602  | 61.135 |
| 0.75     | 0.25     | 1.1        | 212.44 | 204.28  | 210.55 | 204.46 | 208.83 | 227.02  | 278.16 |
| 0.75     | 0.5      | 1.1        | 117.68 | 113.75  | 117.45 | 113.85 | 116.8  | 126.91  | 159.74 |
| 0.75     | 0.75     | 1.1        | 71.928 | 69.819  | 72.216 | 69.97  | 72.023 | 77.009  | 100.12 |

Table 9: Variance of  $\pi^d - 1$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | Optimal | TR+q   | TR     | IFB+q  | IFB    | TRo    | TR+q R |
|----------|----------|------------|---------|--------|--------|--------|--------|--------|--------|
| 0.25     | 0.25     | 0.5        | 7.6157  | 8.6583 | 8.7011 | 10.763 | 11.407 | 10.25  | 8.7532 |
| 0.25     | 0.5      | 0.5        | 7.6154  | 8.6525 | 8.6972 | 10.77  | 11.411 | 10.25  | 8.7456 |
| 0.25     | 0.75     | 0.5        | 7.615   | 8.6438 | 8.6899 | 10.785 | 11.417 | 10.25  | 8.7348 |
| 0.5      | 0.25     | 0.5        | 7.6164  | 8.6738 | 8.7145 | 10.75  | 11.402 | 10.251 | 8.7678 |
| 0.5      | 0.5      | 0.5        | 7.616   | 8.6702 | 8.7104 | 10.758 | 11.406 | 10.251 | 8.7603 |
| 0.5      | 0.75     | 0.5        | 7.6154  | 8.6575 | 8.7026 | 10.775 | 11.413 | 10.25  | 8.7476 |
| 0.75     | 0.25     | 0.5        | 7.6177  | 8.7015 | 8.7385 | 10.734 | 11.395 | 10.252 | 8.7945 |
| 0.75     | 0.5      | 0.5        | 7.6172  | 8.6975 | 8.7358 | 10.741 | 11.398 | 10.252 | 8.7903 |
| 0.75     | 0.75     | 0.5        | 7.6165  | 8.6874 | 8.7288 | 10.758 | 11.406 | 10.251 | 8.7758 |
| 0.25     | 0.25     | 0.9        | 7.6181  | 8.7449 | 8.7762 | 10.751 | 11.439 | 10.253 | 8.8325 |
| 0.25     | 0.5      | 0.9        | 7.6172  | 8.7264 | 8.7663 | 10.753 | 11.432 | 10.252 | 8.8108 |
| 0.25     | 0.75     | 0.9        | 7.6161  | 8.6913 | 8.7375 | 10.769 | 11.428 | 10.251 | 8.7765 |
| 0.5      | 0.25     | 0.9        | 7.6227  | 8.8419 | 8.877  | 10.722 | 11.452 | 10.258 | 8.9201 |
| 0.5      | 0.5      | 0.9        | 7.6211  | 8.8171 | 8.8557 | 10.727 | 11.439 | 10.255 | 8.8945 |
| 0.5      | 0.75     | 0.9        | 7.6187  | 8.7699 | 8.8121 | 10.749 | 11.429 | 10.252 | 8.8463 |
| 0.75     | 0.25     | 0.9        | 7.6407  | 9.0913 | 9.0768 | 10.713 | 11.516 | 10.295 | 9.1639 |
| 0.75     | 0.5      | 0.9        | 7.6375  | 9.0695 | 9.0834 | 10.716 | 11.479 | 10.282 | 9.1588 |
| 0.75     | 0.75     | 0.9        | 7.6315  | 9.064  | 9.0896 | 10.733 | 11.438 | 10.267 | 9.1161 |
| 0.25     | 0.25     | 1.1        | 7.6203  | 8.8497 | 8.8714 | 10.757 | 11.505 | 10.256 | 8.9263 |
| 0.25     | 0.5      | 1.1        | 7.6189  | 8.7975 | 8.8446 | 10.75  | 11.47  | 10.253 | 8.876  |
| 0.25     | 0.75     | 1.1        | 7.617   | 8.7361 | 8.7822 | 10.762 | 11.444 | 10.251 | 8.8153 |
| 0.5      | 0.25     | 1.1        | 7.6337  | 9.0889 | 9.0964 | 10.715 | 11.616 | 10.28  | 9.184  |
| 0.5      | 0.5      | 1.1        | 7.6301  | 9.0483 | 9.0367 | 10.716 | 11.521 | 10.267 | 9.0979 |
| 0.5      | 0.75     | 1.1        | 7.6245  | 8.9199 | 8.9183 | 10.738 | 11.457 | 10.257 | 8.9787 |
| 0.75     | 0.25     | 1.1        | 7.8494  | 9.8478 | 9.8925 | 10.777 | 12.623 | 11.239 | 10.14  |
| 0.75     | 0.5      | 1.1        | 7.8223  | 10.159 | 10.464 | 10.771 | 11.806 | 10.649 | 10.268 |
| 0.75     | 0.75     | 1.1        | 7.7696  | 10.095 | 10.071 | 10.766 | 11.45  | 10.379 | 10.135 |

Table 10: Variance of  $\pi^d - 2$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | TR R   | TR+q RI | TR RI  | TR+q I | TR I   | IFB+q I | IFB I  |
|----------|----------|------------|--------|---------|--------|--------|--------|---------|--------|
| 0.25     | 0.25     | 0.5        | 8.779  | 8.7541  | 8.7789 | 8.6565 | 8.7156 | 10.763  | 11.407 |
| 0.25     | 0.5      | 0.5        | 8.7702 | 8.7463  | 8.7722 | 8.6519 | 8.7082 | 10.77   | 11.411 |
| 0.25     | 0.75     | 0.5        | 8.753  | 8.7352  | 8.7618 | 8.6448 | 8.6941 | 10.785  | 11.417 |
| 0.5      | 0.25     | 0.5        | 8.7915 | 8.769   | 8.7931 | 8.6725 | 8.7278 | 10.75   | 11.402 |
| 0.5      | 0.5      | 0.5        | 8.7858 | 8.7613  | 8.7858 | 8.6701 | 8.7204 | 10.758  | 11.406 |
| 0.5      | 0.75     | 0.5        | 8.7688 | 8.748   | 8.774  | 8.6585 | 8.707  | 10.775  | 11.413 |
| 0.75     | 0.25     | 0.5        | 8.8172 | 8.798   | 8.8168 | 8.6998 | 8.7541 | 10.735  | 11.395 |
| 0.75     | 0.5      | 0.5        | 8.8118 | 8.7894  | 8.8124 | 8.6991 | 8.7467 | 10.741  | 11.398 |
| 0.75     | 0.75     | 0.5        | 8.8    | 8.7777  | 8.8015 | 8.6875 | 8.7324 | 10.758  | 11.406 |
| 0.25     | 0.25     | 0.9        | 8.8604 | 8.8373  | 8.8606 | 8.7496 | 8.7996 | 10.752  | 11.439 |
| 0.25     | 0.5      | 0.9        | 8.8368 | 8.8128  | 8.8373 | 8.7275 | 8.7718 | 10.753  | 11.432 |
| 0.25     | 0.75     | 0.9        | 8.7997 | 8.7791  | 8.8043 | 8.6974 | 8.736  | 10.768  | 11.428 |
| 0.5      | 0.25     | 0.9        | 8.9451 | 8.9319  | 8.9487 | 8.8597 | 8.8806 | 10.723  | 11.452 |
| 0.5      | 0.5      | 0.9        | 8.9189 | 8.9008  | 8.9218 | 8.8341 | 8.8495 | 10.727  | 11.439 |
| 0.5      | 0.75     | 0.9        | 8.8727 | 8.8502  | 8.8738 | 8.7749 | 8.8147 | 10.749  | 11.429 |
| 0.75     | 0.25     | 0.9        | 9.1745 | 9.2009  | 9.2023 | 9.1538 | 9.1644 | 10.713  | 11.516 |
| 0.75     | 0.5      | 0.9        | 9.1714 | 9.1796  | 9.1838 | 9.1297 | 9.151  | 10.717  | 11.479 |
| 0.75     | 0.75     | 0.9        | 9.1274 | 9.1204  | 9.1295 | 9.0767 | 9.0961 | 10.736  | 11.438 |
| 0.25     | 0.25     | 1.1        | 8.9526 | 8.9346  | 8.9563 | 8.8621 | 8.8904 | 10.759  | 11.506 |
| 0.25     | 0.5      | 1.1        | 8.9037 | 8.8813  | 8.9064 | 8.8169 | 8.8358 | 10.751  | 11.471 |
| 0.25     | 0.75     | 1.1        | 8.8436 | 8.8185  | 8.8445 | 8.7405 | 8.7705 | 10.762  | 11.444 |
| 0.5      | 0.25     | 1.1        | 9.2038 | 9.2284  | 9.2389 | 9.1938 | 9.2121 | 10.715  | 11.617 |
| 0.5      | 0.5      | 1.1        | 9.1206 | 9.1174  | 9.1337 | 9.0758 | 9.1037 | 10.716  | 11.522 |
| 0.5      | 0.75     | 1.1        | 9.0036 | 8.9864  | 9.007  | 8.9316 | 8.9661 | 10.738  | 11.457 |
| 0.75     | 0.25     | 1.1        | 10.059 | 11.516  | 11.462 | 11.593 | 11.628 | 10.777  | 12.597 |
| 0.75     | 0.5      | 1.1        | 10.21  | 10.755  | 10.651 | 10.792 | 10.761 | 10.785  | 11.79  |
| 0.75     | 0.75     | 1.1        | 10.08  | 10.209  | 10.149 | 10.24  | 10.182 | 10.793  | 11.44  |



Table 11: Variance of  $y - 1$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | Optimal | TR+q   | TR     | IFB+q  | IFB    | TRo    | TR+q R |
|----------|----------|------------|---------|--------|--------|--------|--------|--------|--------|
| 0.25     | 0.25     | 0.5        | 7.3605  | 8.0302 | 8.0691 | 10.18  | 10.199 | 8.1065 | 8.0881 |
| 0.25     | 0.5      | 0.5        | 7.3589  | 8.0288 | 8.0677 | 10.177 | 10.192 | 8.1039 | 8.0897 |
| 0.25     | 0.75     | 0.5        | 7.3566  | 8.0281 | 8.0676 | 10.166 | 10.182 | 8.1002 | 8.0934 |
| 0.5      | 0.25     | 0.5        | 7.3636  | 8.0254 | 8.0651 | 10.188 | 10.212 | 8.1113 | 8.0828 |
| 0.5      | 0.5      | 0.5        | 7.3617  | 8.0216 | 8.0638 | 10.184 | 10.204 | 8.1086 | 8.0844 |
| 0.5      | 0.75     | 0.5        | 7.3587  | 8.0234 | 8.0625 | 10.173 | 10.19  | 8.1041 | 8.0876 |
| 0.75     | 0.25     | 0.5        | 7.3691  | 8.0212 | 8.0586 | 10.194 | 10.234 | 8.12   | 8.0745 |
| 0.75     | 0.5      | 0.5        | 7.3672  | 8.0174 | 8.0568 | 10.192 | 10.226 | 8.1178 | 8.0727 |
| 0.75     | 0.75     | 0.5        | 7.3636  | 8.0148 | 8.0547 | 10.183 | 10.21  | 8.1132 | 8.0771 |
| 0.25     | 0.25     | 0.9        | 7.3741  | 7.9906 | 8.0418 | 10.199 | 10.215 | 8.1297 | 8.0473 |
| 0.25     | 0.5      | 0.9        | 7.3696  | 7.988  | 8.0313 | 10.201 | 10.204 | 8.122  | 8.0529 |
| 0.25     | 0.75     | 0.9        | 7.3631  | 8.001  | 8.04   | 10.188 | 10.189 | 8.1115 | 8.0681 |
| 0.5      | 0.25     | 0.9        | 7.3936  | 7.9587 | 7.9913 | 10.213 | 10.27  | 8.1588 | 8.0173 |
| 0.5      | 0.5      | 0.9        | 7.3865  | 7.9583 | 7.9936 | 10.214 | 10.249 | 8.1487 | 8.0203 |
| 0.5      | 0.75     | 0.9        | 7.3751  | 7.9672 | 8.0058 | 10.201 | 10.218 | 8.1322 | 8.0363 |
| 0.75     | 0.25     | 0.9        | 7.4587  | 7.9656 | 7.9855 | 10.176 | 10.47  | 8.25   | 7.9895 |
| 0.75     | 0.5      | 0.9        | 7.4466  | 7.945  | 7.9688 | 10.194 | 10.419 | 8.24   | 7.9616 |
| 0.75     | 0.75     | 0.9        | 7.4229  | 7.8825 | 7.8969 | 10.212 | 10.34  | 8.2158 | 7.9542 |
| 0.25     | 0.25     | 1.1        | 7.3861  | 7.9315 | 7.9963 | 10.215 | 10.217 | 8.1556 | 7.9921 |
| 0.25     | 0.5      | 1.1        | 7.3791  | 7.9499 | 7.9847 | 10.217 | 10.206 | 8.1401 | 8.0144 |
| 0.25     | 0.75     | 1.1        | 7.369   | 7.9724 | 8.0135 | 10.201 | 10.191 | 8.1216 | 8.0432 |
| 0.5      | 0.25     | 1.1        | 7.4426  | 7.8971 | 7.9518 | 10.225 | 10.372 | 8.2477 | 7.9258 |
| 0.5      | 0.5      | 1.1        | 7.4271  | 7.8578 | 7.9537 | 10.232 | 10.314 | 8.2123 | 7.9338 |
| 0.5      | 0.75     | 1.1        | 7.402   | 7.9001 | 7.9751 | 10.221 | 10.252 | 8.1703 | 7.9744 |
| 0.75     | 0.25     | 1.1        | 8.1493  | 8.4969 | 8.3885 | 10.076 | 12.448 | 9.152  | 8.3701 |
| 0.75     | 0.5      | 1.1        | 8.0602  | 7.9925 | 7.5688 | 10.127 | 11.367 | 8.7933 | 7.9977 |
| 0.75     | 0.75     | 1.1        | 7.8829  | 7.8024 | 7.6659 | 10.237 | 10.753 | 8.5607 | 7.8268 |

Table 12: Variance of  $y - 2$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | TR R   | TR+q RI | TR RI  | TR+q I | TR I   | IFB+q I | IFB I  |
|----------|----------|------------|--------|---------|--------|--------|--------|---------|--------|
| 0.25     | 0.25     | 0.5        | 8.1404 | 8.0872  | 8.1406 | 8.0356 | 8.0534 | 10.18   | 10.199 |
| 0.25     | 0.5      | 0.5        | 8.1452 | 8.0892  | 8.1431 | 8.0318 | 8.056  | 10.177  | 10.192 |
| 0.25     | 0.75     | 0.5        | 8.1572 | 8.093   | 8.1477 | 8.0268 | 8.0631 | 10.166  | 10.182 |
| 0.5      | 0.25     | 0.5        | 8.1358 | 8.0814  | 8.134  | 8.0306 | 8.0506 | 10.188  | 10.212 |
| 0.5      | 0.5      | 0.5        | 8.1369 | 8.0827  | 8.1368 | 8.0218 | 8.0527 | 10.184  | 10.204 |
| 0.5      | 0.75     | 0.5        | 8.1471 | 8.087   | 8.1414 | 8.0223 | 8.0576 | 10.173  | 10.191 |
| 0.75     | 0.25     | 0.5        | 8.1242 | 8.0703  | 8.1246 | 8.0244 | 8.0418 | 10.194  | 10.234 |
| 0.75     | 0.5      | 0.5        | 8.1258 | 8.0733  | 8.1251 | 8.0148 | 8.0447 | 10.192  | 10.226 |
| 0.75     | 0.75     | 0.5        | 8.1299 | 8.0744  | 8.1282 | 8.0156 | 8.0497 | 10.183  | 10.21  |
| 0.25     | 0.25     | 0.9        | 8.0933 | 8.0429  | 8.0935 | 7.988  | 8.012  | 10.199  | 10.215 |
| 0.25     | 0.5      | 0.9        | 8.1049 | 8.0505  | 8.1045 | 7.9899 | 8.0251 | 10.201  | 10.204 |
| 0.25     | 0.75     | 0.9        | 8.1264 | 8.0644  | 8.1212 | 7.9926 | 8.0414 | 10.188  | 10.189 |
| 0.5      | 0.25     | 0.9        | 8.0557 | 8.006   | 8.0525 | 7.9392 | 7.9884 | 10.213  | 10.27  |
| 0.5      | 0.5      | 0.9        | 8.0658 | 8.0126  | 8.0623 | 7.9358 | 7.9995 | 10.214  | 10.249 |
| 0.5      | 0.75     | 0.9        | 8.0855 | 8.0299  | 8.0837 | 7.9581 | 8.0019 | 10.201  | 10.218 |
| 0.75     | 0.25     | 0.9        | 7.9925 | 7.9484  | 7.9559 | 7.8726 | 7.8883 | 10.176  | 10.47  |
| 0.75     | 0.5      | 0.9        | 7.9709 | 7.9391  | 7.9562 | 7.8651 | 7.8811 | 10.192  | 10.419 |
| 0.75     | 0.75     | 0.9        | 7.9723 | 7.9407  | 7.968  | 7.8589 | 7.8864 | 10.207  | 10.34  |
| 0.25     | 0.25     | 1.1        | 8.0391 | 7.9851  | 8.0362 | 7.9198 | 7.9684 | 10.213  | 10.217 |
| 0.25     | 0.5      | 1.1        | 8.0645 | 8.0081  | 8.0617 | 7.9258 | 7.994  | 10.216  | 10.207 |
| 0.25     | 0.75     | 1.1        | 8.0965 | 8.0385  | 8.0953 | 7.967  | 8.0248 | 10.202  | 10.191 |
| 0.5      | 0.25     | 1.1        | 7.948  | 7.8765  | 7.9039 | 7.7906 | 7.824  | 10.225  | 10.373 |
| 0.5      | 0.5      | 1.1        | 7.9658 | 7.9124  | 7.9513 | 7.8274 | 7.8642 | 10.232  | 10.315 |
| 0.5      | 0.75     | 1.1        | 8.0155 | 7.9609  | 8.0099 | 7.879  | 7.9213 | 10.22   | 10.252 |
| 0.75     | 0.25     | 1.1        | 8.283  | 7.4809  | 7.2296 | 7.3573 | 7.0552 | 10.08   | 12.524 |
| 0.75     | 0.5      | 1.1        | 7.8862 | 7.6211  | 7.4576 | 7.5363 | 7.3295 | 10.121  | 11.406 |
| 0.75     | 0.75     | 1.1        | 7.6775 | 7.7331  | 7.5636 | 7.6381 | 7.4911 | 10.215  | 10.771 |

Table 13: Variance of  $\pi - 1$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | Optimal | TR+q   | TR     | IFB+q  | IFB    | TRo    | TR+q R |
|----------|----------|------------|---------|--------|--------|--------|--------|--------|--------|
| 0.25     | 0.25     | 0.5        | 6.7138  | 7.9531 | 7.94   | 11.577 | 12.904 | 9.6091 | 8.0766 |
| 0.25     | 0.5      | 0.5        | 6.7052  | 7.9432 | 7.9303 | 11.572 | 12.886 | 9.601  | 8.0636 |
| 0.25     | 0.75     | 0.5        | 6.6921  | 7.9282 | 7.9144 | 11.571 | 12.863 | 9.5898 | 8.0441 |
| 0.5      | 0.25     | 0.5        | 6.7317  | 7.9796 | 7.9654 | 11.585 | 12.935 | 9.624  | 8.1029 |
| 0.5      | 0.5      | 0.5        | 6.7215  | 7.9719 | 7.9552 | 11.58  | 12.917 | 9.6155 | 8.0894 |
| 0.5      | 0.75     | 0.5        | 6.7045  | 7.9506 | 7.9371 | 11.578 | 12.889 | 9.6017 | 8.0667 |
| 0.75     | 0.25     | 0.5        | 6.7623  | 8.0246 | 8.0112 | 11.608 | 12.994 | 9.6518 | 8.1499 |
| 0.75     | 0.5      | 0.5        | 6.7522  | 8.0185 | 8.0036 | 11.605 | 12.98  | 9.6446 | 8.1418 |
| 0.75     | 0.75     | 0.5        | 6.7318  | 8.0004 | 7.9864 | 11.601 | 12.953 | 9.6301 | 8.1168 |
| 0.25     | 0.25     | 0.9        | 6.7926  | 8.0969 | 8.0776 | 11.668 | 13.118 | 9.6792 | 8.2174 |
| 0.25     | 0.5      | 0.9        | 6.7683  | 8.0655 | 8.0475 | 11.635 | 13.048 | 9.6551 | 8.178  |
| 0.25     | 0.75     | 0.9        | 6.7317  | 8.006  | 7.9926 | 11.605 | 12.962 | 9.6232 | 8.1173 |
| 0.5      | 0.25     | 0.9        | 6.9021  | 8.2656 | 8.2539 | 11.772 | 13.349 | 9.7727 | 8.3781 |
| 0.5      | 0.5      | 0.9        | 6.8642  | 8.2207 | 8.2082 | 11.731 | 13.257 | 9.7396 | 8.3297 |
| 0.5      | 0.75     | 0.9        | 6.8     | 8.1364 | 8.1229 | 11.678 | 13.124 | 9.6878 | 8.2404 |
| 0.75     | 0.25     | 0.9        | 7.2299  | 8.7392 | 8.7099 | 12.248 | 14.058 | 10.096 | 8.8486 |
| 0.75     | 0.5      | 0.9        | 7.1693  | 8.7032 | 8.691  | 12.185 | 13.957 | 10.055 | 8.821  |
| 0.75     | 0.75     | 0.9        | 7.0457  | 8.6336 | 8.632  | 12.061 | 13.764 | 9.9698 | 8.7169 |
| 0.25     | 0.25     | 1.1        | 6.8629  | 8.2727 | 8.2454 | 11.787 | 13.381 | 9.7568 | 8.3838 |
| 0.25     | 0.5      | 1.1        | 6.8248  | 8.1852 | 8.176  | 11.712 | 13.225 | 9.709  | 8.2941 |
| 0.25     | 0.75     | 1.1        | 6.7672  | 8.0801 | 8.0654 | 11.643 | 13.056 | 9.6529 | 8.185  |
| 0.5      | 0.25     | 1.1        | 7.1737  | 8.7678 | 8.7268 | 12.192 | 14.167 | 10.058 | 8.8813 |
| 0.5      | 0.5      | 1.1        | 7.0915  | 8.6236 | 8.5709 | 12.018 | 13.817 | 9.9421 | 8.7036 |
| 0.5      | 0.75     | 1.1        | 6.9523  | 8.3859 | 8.3272 | 11.839 | 13.447 | 9.8083 | 8.4739 |
| 0.75     | 0.25     | 1.1        | 10.5    | 12.63  | 12.724 | 17.522 | 21.363 | 13.901 | 12.947 |
| 0.75     | 0.5      | 1.1        | 10.081  | 11.563 | 11.995 | 15.444 | 18.184 | 12.246 | 11.688 |
| 0.75     | 0.75     | 1.1        | 9.2335  | 10.628 | 10.701 | 13.98  | 16.307 | 11.264 | 10.682 |

Table 14: Variance of  $\pi - 2$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | TR R   | TR+q RI | TR RI  | TR+q I | TR I   | IFB+q I | IFB I  |
|----------|----------|------------|--------|---------|--------|--------|--------|---------|--------|
| 0.25     | 0.25     | 0.5        | 8.0492 | 8.0772  | 8.0489 | 7.9471 | 7.957  | 11.577  | 12.904 |
| 0.25     | 0.5      | 0.5        | 8.0332 | 8.0639  | 8.0354 | 7.9395 | 7.9432 | 11.573  | 12.886 |
| 0.25     | 0.75     | 0.5        | 8.0054 | 8.0443  | 8.0154 | 7.9292 | 7.9194 | 11.571  | 12.863 |
| 0.5      | 0.25     | 0.5        | 8.0742 | 8.1039  | 8.076  | 7.974  | 7.9809 | 11.585  | 12.935 |
| 0.5      | 0.5      | 0.5        | 8.0616 | 8.0906  | 8.0615 | 7.9713 | 7.9668 | 11.58   | 12.917 |
| 0.5      | 0.75     | 0.5        | 8.0322 | 8.067   | 8.0381 | 7.9502 | 7.9423 | 11.578  | 12.889 |
| 0.75     | 0.25     | 0.5        | 8.1234 | 8.1537  | 8.1228 | 8.02   | 8.0295 | 11.608  | 12.994 |
| 0.75     | 0.5      | 0.5        | 8.1123 | 8.1405  | 8.1128 | 8.0202 | 8.0162 | 11.605  | 12.98  |
| 0.75     | 0.75     | 0.5        | 8.0884 | 8.1192  | 8.0901 | 7.9985 | 7.9901 | 11.601  | 12.953 |
| 0.25     | 0.25     | 0.9        | 8.1943 | 8.221   | 8.1938 | 8.0983 | 8.1014 | 11.669  | 13.118 |
| 0.25     | 0.5      | 0.9        | 8.1499 | 8.1795  | 8.1499 | 8.0627 | 8.0533 | 11.635  | 13.048 |
| 0.25     | 0.75     | 0.9        | 8.0838 | 8.1204  | 8.089  | 8.0127 | 7.9905 | 11.604  | 12.962 |
| 0.5      | 0.25     | 0.9        | 8.3587 | 8.3874  | 8.3609 | 8.2822 | 8.2555 | 11.772  | 13.349 |
| 0.5      | 0.5      | 0.9        | 8.3055 | 8.3351  | 8.3075 | 8.2396 | 8.1986 | 11.731  | 13.257 |
| 0.5      | 0.75     | 0.9        | 8.2147 | 8.2453  | 8.2155 | 8.1426 | 8.1253 | 11.678  | 13.124 |
| 0.75     | 0.25     | 0.9        | 8.8484 | 8.8715  | 8.8669 | 8.791  | 8.7856 | 12.25   | 14.058 |
| 0.75     | 0.5      | 0.9        | 8.8188 | 8.8351  | 8.825  | 8.7516 | 8.7512 | 12.187  | 13.957 |
| 0.75     | 0.75     | 0.9        | 8.7078 | 8.7239  | 8.7086 | 8.6478 | 8.6374 | 12.062  | 13.764 |
| 0.25     | 0.25     | 1.1        | 8.3581 | 8.3897  | 8.3606 | 8.2839 | 8.259  | 11.79   | 13.383 |
| 0.25     | 0.5      | 1.1        | 8.2671 | 8.2989  | 8.2692 | 8.2082 | 8.164  | 11.713  | 13.226 |
| 0.25     | 0.75     | 1.1        | 8.1565 | 8.1889  | 8.1572 | 8.0842 | 8.0506 | 11.643  | 13.056 |
| 0.5      | 0.25     | 1.1        | 8.8706 | 8.9129  | 8.8972 | 8.846  | 8.8329 | 12.192  | 14.169 |
| 0.5      | 0.5      | 1.1        | 8.6879 | 8.719   | 8.6972 | 8.6459 | 8.6314 | 12.018  | 13.817 |
| 0.5      | 0.75     | 1.1        | 8.4534 | 8.4839  | 8.4563 | 8.4    | 8.3828 | 11.839  | 13.448 |
| 0.75     | 0.25     | 1.1        | 12.988 | 13.813  | 13.97  | 13.924 | 14.141 | 17.577  | 21.394 |
| 0.75     | 0.5      | 1.1        | 11.749 | 11.969  | 12.024 | 12.012 | 12.12  | 15.488  | 18.195 |
| 0.75     | 0.75     | 1.1        | 10.768 | 10.735  | 10.819 | 10.758 | 10.818 | 14      | 16.311 |

Table 15: Variance of  $i - 1$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | Optimal | TR+q   | TR     | IFB+q  | IFB    | TRo    | TR+q R |
|----------|----------|------------|---------|--------|--------|--------|--------|--------|--------|
| 0.25     | 0.25     | 0.5        | 2.0443  | 11.144 | 11.115 | 21.285 | 22.959 | 12.154 | 11.374 |
| 0.25     | 0.5      | 0.5        | 2.0437  | 11.126 | 11.096 | 21.287 | 22.96  | 12.142 | 11.357 |
| 0.25     | 0.75     | 0.5        | 2.0429  | 11.101 | 11.068 | 21.296 | 22.963 | 12.125 | 11.331 |
| 0.5      | 0.25     | 0.5        | 2.0458  | 11.183 | 11.154 | 21.273 | 22.942 | 12.177 | 11.409 |
| 0.5      | 0.5      | 0.5        | 2.045   | 11.165 | 11.134 | 21.276 | 22.946 | 12.164 | 11.39  |
| 0.5      | 0.75     | 0.5        | 2.0438  | 11.132 | 11.1   | 21.287 | 22.953 | 12.143 | 11.359 |
| 0.75     | 0.25     | 0.5        | 2.0489  | 11.252 | 11.224 | 21.264 | 22.911 | 12.221 | 11.472 |
| 0.75     | 0.5      | 0.5        | 2.048   | 11.237 | 11.207 | 21.266 | 22.917 | 12.21  | 11.458 |
| 0.75     | 0.75     | 0.5        | 2.0464  | 11.204 | 11.174 | 21.275 | 22.93  | 12.187 | 11.424 |
| 0.25     | 0.25     | 0.9        | 2.0493  | 11.336 | 11.322 | 21.283 | 23.014 | 12.262 | 11.544 |
| 0.25     | 0.5      | 0.9        | 2.0475  | 11.281 | 11.255 | 21.273 | 22.995 | 12.224 | 11.491 |
| 0.25     | 0.75     | 0.9        | 2.0451  | 11.198 | 11.168 | 21.278 | 22.977 | 12.175 | 11.416 |
| 0.5      | 0.25     | 0.9        | 2.0609  | 11.566 | 11.55  | 21.265 | 22.929 | 12.411 | 11.75  |
| 0.5      | 0.5      | 0.9        | 2.0571  | 11.49  | 11.469 | 21.255 | 22.927 | 12.357 | 11.68  |
| 0.5      | 0.75     | 0.9        | 2.0516  | 11.364 | 11.338 | 21.261 | 22.934 | 12.275 | 11.564 |
| 0.75     | 0.25     | 0.9        | 2.1208  | 12.199 | 12.201 | 21.356 | 22.76  | 12.962 | 12.355 |
| 0.75     | 0.5      | 0.9        | 2.1109  | 12.144 | 12.135 | 21.323 | 22.776 | 12.881 | 12.297 |
| 0.75     | 0.75     | 0.9        | 2.0928  | 11.989 | 11.983 | 21.288 | 22.819 | 12.728 | 12.139 |
| 0.25     | 0.25     | 1.1        | 2.054   | 11.565 | 11.558 | 21.296 | 23.126 | 12.382 | 11.74  |
| 0.25     | 0.5      | 1.1        | 2.051   | 11.436 | 11.418 | 21.27  | 23.049 | 12.306 | 11.627 |
| 0.25     | 0.75     | 1.1        | 2.0472  | 11.286 | 11.26  | 21.268 | 22.995 | 12.22  | 11.492 |
| 0.5      | 0.25     | 1.1        | 2.0908  | 12.233 | 12.218 | 21.311 | 22.933 | 12.874 | 12.357 |
| 0.5      | 0.5      | 1.1        | 2.0813  | 11.98  | 11.963 | 21.268 | 22.901 | 12.679 | 12.121 |
| 0.5      | 0.75     | 1.1        | 2.0673  | 11.662 | 11.631 | 21.254 | 22.904 | 12.462 | 11.834 |
| 0.75     | 0.25     | 1.1        | 3.002   | 15.414 | 15.492 | 21.699 | 24.751 | 20.001 | 15.52  |
| 0.75     | 0.5      | 1.1        | 2.8913  | 14.716 | 14.923 | 21.585 | 23.597 | 16.741 | 14.822 |
| 0.75     | 0.75     | 1.1        | 2.6759  | 14.029 | 14.151 | 21.431 | 23.062 | 14.888 | 14.107 |

Table 16: Variance of  $i - 2$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | TR R   | TR+q RI | TR RI  | TR+q I | TR I   | IFB+q I | IFB I  |
|----------|----------|------------|--------|---------|--------|--------|--------|---------|--------|
| 0.25     | 0.25     | 0.5        | 11.329 | 11.376  | 11.33  | 11.142 | 11.121 | 21.285  | 22.959 |
| 0.25     | 0.5      | 0.5        | 11.309 | 11.357  | 11.31  | 11.125 | 11.101 | 21.287  | 22.96  |
| 0.25     | 0.75     | 0.5        | 11.28  | 11.332  | 11.283 | 11.102 | 11.07  | 21.296  | 22.963 |
| 0.5      | 0.25     | 0.5        | 11.365 | 11.411  | 11.366 | 11.182 | 11.159 | 21.273  | 22.942 |
| 0.5      | 0.5      | 0.5        | 11.345 | 11.392  | 11.346 | 11.167 | 11.139 | 21.276  | 22.946 |
| 0.5      | 0.75     | 0.5        | 11.31  | 11.36   | 11.312 | 11.131 | 11.103 | 21.287  | 22.953 |
| 0.75     | 0.25     | 0.5        | 11.432 | 11.475  | 11.432 | 11.252 | 11.231 | 21.264  | 22.911 |
| 0.75     | 0.5      | 0.5        | 11.415 | 11.459  | 11.416 | 11.241 | 11.213 | 21.266  | 22.917 |
| 0.75     | 0.75     | 0.5        | 11.38  | 11.426  | 11.381 | 11.204 | 11.174 | 21.276  | 22.93  |
| 0.25     | 0.25     | 0.9        | 11.51  | 11.551  | 11.512 | 11.343 | 11.324 | 21.284  | 23.014 |
| 0.25     | 0.5      | 0.9        | 11.451 | 11.495  | 11.452 | 11.285 | 11.258 | 21.273  | 22.995 |
| 0.25     | 0.75     | 0.9        | 11.369 | 11.418  | 11.371 | 11.201 | 11.169 | 21.278  | 22.977 |
| 0.5      | 0.25     | 0.9        | 11.726 | 11.768  | 11.734 | 11.59  | 11.561 | 21.265  | 22.929 |
| 0.5      | 0.5      | 0.9        | 11.648 | 11.692  | 11.655 | 11.511 | 11.475 | 21.255  | 22.926 |
| 0.5      | 0.75     | 0.9        | 11.525 | 11.57   | 11.527 | 11.374 | 11.344 | 21.261  | 22.934 |
| 0.75     | 0.25     | 0.9        | 12.366 | 12.428  | 12.422 | 12.308 | 12.293 | 21.358  | 22.76  |
| 0.75     | 0.5      | 0.9        | 12.295 | 12.345  | 12.332 | 12.22  | 12.203 | 21.329  | 22.776 |
| 0.75     | 0.75     | 0.9        | 12.129 | 12.159  | 12.138 | 12.021 | 12     | 21.297  | 22.819 |
| 0.25     | 0.25     | 1.1        | 11.713 | 11.753  | 11.72  | 11.583 | 11.558 | 21.3    | 23.127 |
| 0.25     | 0.5      | 1.1        | 11.591 | 11.635  | 11.596 | 11.454 | 11.419 | 21.27   | 23.049 |
| 0.25     | 0.75     | 1.1        | 11.449 | 11.496  | 11.451 | 11.292 | 11.256 | 21.268  | 22.995 |
| 0.5      | 0.25     | 1.1        | 12.353 | 12.431  | 12.413 | 12.333 | 12.317 | 21.311  | 22.931 |
| 0.5      | 0.5      | 1.1        | 12.103 | 12.161  | 12.133 | 12.035 | 12.012 | 21.269  | 22.901 |
| 0.5      | 0.75     | 1.1        | 11.803 | 11.848  | 11.811 | 11.687 | 11.66  | 21.255  | 22.904 |
| 0.75     | 0.25     | 1.1        | 15.702 | 17.739  | 18.327 | 17.767 | 18.176 | 21.717  | 24.716 |
| 0.75     | 0.5      | 1.1        | 14.988 | 15.723  | 16.032 | 15.744 | 15.994 | 21.637  | 23.589 |
| 0.75     | 0.75     | 1.1        | 14.278 | 14.294  | 14.473 | 14.296 | 14.441 | 21.508  | 23.061 |

Table 17: Variance of  $i - i_{-1} - 1$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | Optimal | TR+q   | TR     | IFB+q  | IFB    | TRo    | TR+q R |
|----------|----------|------------|---------|--------|--------|--------|--------|--------|--------|
| 0.25     | 0.25     | 0.5        | 0.66116 | 6.5116 | 6.5014 | 13.329 | 14.965 | 6.2309 | 6.3843 |
| 0.25     | 0.5      | 0.5        | 0.66062 | 6.4842 | 6.4768 | 13.338 | 14.99  | 6.2053 | 6.3552 |
| 0.25     | 0.75     | 0.5        | 0.65984 | 6.4461 | 6.4417 | 13.362 | 15.027 | 6.1713 | 6.3154 |
| 0.5      | 0.25     | 0.5        | 0.66241 | 6.5629 | 6.5513 | 13.31  | 14.927 | 6.2747 | 6.4355 |
| 0.5      | 0.5      | 0.5        | 0.66174 | 6.5356 | 6.5261 | 13.32  | 14.954 | 6.2489 | 6.4068 |
| 0.5      | 0.75     | 0.5        | 0.66067 | 6.4917 | 6.4856 | 13.346 | 14.999 | 6.2089 | 6.3611 |
| 0.75     | 0.25     | 0.5        | 0.66475 | 6.6541 | 6.6396 | 13.296 | 14.867 | 6.3558 | 6.5284 |
| 0.75     | 0.5      | 0.5        | 0.66404 | 6.6356 | 6.6222 | 13.303 | 14.891 | 6.3362 | 6.508  |
| 0.75     | 0.75     | 0.5        | 0.66265 | 6.5971 | 6.5854 | 13.324 | 14.939 | 6.2979 | 6.4668 |
| 0.25     | 0.25     | 0.9        | 0.66578 | 6.7864 | 6.7626 | 13.303 | 14.931 | 6.4592 | 6.6537 |
| 0.25     | 0.5      | 0.9        | 0.66424 | 6.703  | 6.6984 | 13.3   | 14.961 | 6.3812 | 6.5682 |
| 0.25     | 0.75     | 0.9        | 0.66205 | 6.5907 | 6.5879 | 13.324 | 15.008 | 6.2823 | 6.4549 |
| 0.5      | 0.25     | 0.9        | 0.67411 | 7.0906 | 7.0903 | 13.286 | 14.824 | 6.7385 | 6.9536 |
| 0.5      | 0.5      | 0.9        | 0.67134 | 6.9961 | 6.9919 | 13.279 | 14.862 | 6.6411 | 6.858  |
| 0.5      | 0.75     | 0.9        | 0.66697 | 6.8424 | 6.8364 | 13.301 | 14.931 | 6.4947 | 6.7027 |
| 0.75     | 0.25     | 0.9        | 0.70407 | 7.8317 | 7.8726 | 13.393 | 14.68  | 7.6457 | 7.7743 |
| 0.75     | 0.5      | 0.9        | 0.69879 | 7.8258 | 7.829  | 13.361 | 14.705 | 7.5694 | 7.7607 |
| 0.75     | 0.75     | 0.9        | 0.68857 | 7.7792 | 7.7822 | 13.334 | 14.783 | 7.3999 | 7.6341 |
| 0.25     | 0.25     | 1.1        | 0.66998 | 7.0974 | 7.0593 | 13.3   | 14.97  | 6.7079 | 6.949  |
| 0.25     | 0.5      | 1.1        | 0.66752 | 6.927  | 6.925  | 13.285 | 14.978 | 6.5562 | 6.7809 |
| 0.25     | 0.75     | 1.1        | 0.66405 | 6.7232 | 6.7204 | 13.305 | 15.009 | 6.3827 | 6.5808 |
| 0.5      | 0.25     | 1.1        | 0.69417 | 7.8791 | 7.9015 | 13.323 | 14.79  | 7.5961 | 7.8019 |
| 0.5      | 0.5      | 1.1        | 0.68788 | 7.6781 | 7.6002 | 13.287 | 14.812 | 7.2723 | 7.5267 |
| 0.5      | 0.75     | 1.1        | 0.67787 | 7.3008 | 7.3107 | 13.288 | 14.883 | 6.8979 | 7.1527 |
| 0.75     | 0.25     | 1.1        | 1.011   | 12.354 | 12.393 | 13.86  | 15.657 | 16.975 | 12.219 |
| 0.75     | 0.5      | 1.1        | 0.97144 | 11.457 | 11.499 | 13.699 | 15.147 | 13.601 | 11.403 |
| 0.75     | 0.75     | 1.1        | 0.89295 | 10.794 | 10.993 | 13.509 | 14.966 | 11.511 | 10.765 |

Table 18: Variance of  $i - i_{-1} - 2$ 

| $p_{11}$ | $p_{22}$ | $\rho_1^q$ | TR R   | TR+q RI | TR RI  | TR+q I | TR I   | IFB+q I | IFB I  |
|----------|----------|------------|--------|---------|--------|--------|--------|---------|--------|
| 0.25     | 0.25     | 0.5        | 6.3708 | 6.3882  | 6.3715 | 6.5166 | 6.4999 | 13.329  | 14.965 |
| 0.25     | 0.5      | 0.5        | 6.3423 | 6.3583  | 6.3428 | 6.4889 | 6.4752 | 13.338  | 14.99  |
| 0.25     | 0.75     | 0.5        | 6.3039 | 6.3173  | 6.3033 | 6.4488 | 6.4415 | 13.362  | 15.027 |
| 0.5      | 0.25     | 0.5        | 6.4214 | 6.4404  | 6.4224 | 6.5691 | 6.5511 | 13.31   | 14.927 |
| 0.5      | 0.5      | 0.5        | 6.3929 | 6.411   | 6.3943 | 6.5409 | 6.5268 | 13.32   | 14.954 |
| 0.5      | 0.75     | 0.5        | 6.3484 | 6.3635  | 6.3485 | 6.4969 | 6.486  | 13.346  | 14.999 |
| 0.75     | 0.25     | 0.5        | 6.5117 | 6.5333  | 6.5136 | 6.662  | 6.6392 | 13.296  | 14.867 |
| 0.75     | 0.5      | 0.5        | 6.4917 | 6.5128  | 6.4935 | 6.6425 | 6.6236 | 13.303  | 14.891 |
| 0.75     | 0.75     | 0.5        | 6.4513 | 6.4695  | 6.4519 | 6.6026 | 6.5885 | 13.324  | 14.94  |
| 0.25     | 0.25     | 0.9        | 6.6485 | 6.6724  | 6.6534 | 6.8069 | 6.7836 | 13.305  | 14.931 |
| 0.25     | 0.5      | 0.9        | 6.5606 | 6.5817  | 6.5651 | 6.7191 | 6.7041 | 13.3    | 14.961 |
| 0.25     | 0.75     | 0.9        | 6.4455 | 6.4613  | 6.4473 | 6.6011 | 6.5921 | 13.324  | 15.007 |
| 0.5      | 0.25     | 0.9        | 6.9548 | 6.9917  | 6.9701 | 7.1331 | 7.1097 | 13.286  | 14.823 |
| 0.5      | 0.5      | 0.9        | 6.8525 | 6.8864  | 6.8659 | 7.0318 | 7.0144 | 13.279  | 14.861 |
| 0.5      | 0.75     | 0.9        | 6.6927 | 6.7166  | 6.6988 | 6.8635 | 6.8465 | 13.301  | 14.931 |
| 0.75     | 0.25     | 0.9        | 7.8031 | 7.9095  | 7.904  | 8.0589 | 8.0406 | 13.394  | 14.68  |
| 0.75     | 0.5      | 0.9        | 7.7723 | 7.8481  | 7.8358 | 8.0056 | 7.9791 | 13.367  | 14.705 |
| 0.75     | 0.75     | 0.9        | 7.6437 | 7.6831  | 7.6639 | 7.8396 | 7.8135 | 13.346  | 14.784 |
| 0.25     | 0.25     | 1.1        | 6.9529 | 6.9835  | 6.9653 | 7.1324 | 7.1137 | 13.305  | 14.968 |
| 0.25     | 0.5      | 1.1        | 6.7782 | 6.8042  | 6.7879 | 6.9536 | 6.9415 | 13.285  | 14.977 |
| 0.25     | 0.75     | 1.1        | 6.5728 | 6.5911  | 6.5775 | 6.738  | 6.7327 | 13.304  | 15.009 |
| 0.5      | 0.25     | 1.1        | 7.8279 | 7.9565  | 7.9388 | 8.1237 | 8.0924 | 13.323  | 14.787 |
| 0.5      | 0.5      | 1.1        | 7.5342 | 7.6103  | 7.5886 | 7.7771 | 7.7492 | 13.288  | 14.81  |
| 0.5      | 0.75     | 1.1        | 7.149  | 7.1889  | 7.1676 | 7.3515 | 7.3277 | 13.29   | 14.882 |
| 0.75     | 0.25     | 1.1        | 12.378 | 15.046  | 15.521 | 15.052 | 15.379 | 13.836  | 15.588 |
| 0.75     | 0.5      | 1.1        | 11.581 | 12.717  | 13.086 | 12.774 | 13.072 | 13.727  | 15.12  |
| 0.75     | 0.75     | 1.1        | 11.026 | 11.121  | 11.382 | 11.21  | 11.45  | 13.586  | 14.961 |



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