Removal of Chloride in the Kraft Chemical Recovery Cycle of Pulp Mills Using the Ion-Exchange Process

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High levels of chloride in the kraft recovery cycle of pulp mills can cause serious problems, particularly in recovery boiler operation. The treatment of ash collected from the electrostatic precipitator (ESP) for chloride removal was investigated experimentally using the ion-exchange process based on an amphoteric resin (BIORAD AG 11 A8). Saturation and regeneration experiments in a fixed bed were carried out for different flow rates. Experimental adsorption results obtained in the saturation step were well predicted with a mathematical model that takes into account dispersed plug flow for the bulk liquid, external mass-transfer resistance, intraparticle mass transfer by pore diffusion, and instantaneous equilibrium of adsorption at the pore/wall interface. The equilibrium was modeled using an extended Langmuir–Freundlich isotherm for three components (Cl\(^{-}\), SO\(_4^{2-}\), and CO\(_3^{2-}\)) based on single-component equilibrium data. The resin performance was tested during cyclic operation, in which a chloride removal efficiency of higher than 89% was achieved, along with a sulfate recovery of 67–74%.

1. Introduction

A high concentration level of chloride in the recovery cycle of kraft pulp mills is known to cause serious problems in recovery boiler operation. The boiler burns black liquor, which is a heterogeneous aqueous solution of various organic and inorganic substances.\(^1\) The inorganic material consists mainly of residual effective alkalis, sulfide, sulfate, carbonate, chloride, thiosulfate, and oxalate.\(^2\) The exact composition of the black liquor depends on the wood species, the pulp yield, and the alkali charge used. The sources and amounts of Cl entering a mill vary from one mill to another depending on the type of wood, the degree of closure, and the location of the mill (inland or coastal). For inland mills, the wood is the main source of input for Cl, and its concentration in strong black liquor (BLS) is typically 0.1–0.8% of the liquor dry solid. However, for coastal mills transporting their logs on seawater, the Cl content can be as high as 3–5%, and in closed processes, it can rise even higher.\(^2,3\) Studies have shown that the chloride concentration is one of the most significant factors affecting the melting properties of the ash in the boiler.\(^3,4\) Some of these ash particles are dragged with the gas stream and form deposits on tube surfaces in the upper furnace of the recovery boiler, and if such deposits are not periodically removed, they can plug the flue gas passages. Thus, excessive deposit accumulation decreases the boiler capacity and causes severe losses of production. Also, the risk of occurrence of a corrosive environment that can damage tubes increases drastically. The current level of chloride in the recovery cycle of some mills requires that boilers be shut down for water washing as frequently as every 3 months. If this level is maintained at a minimal value in the BLS, the operating availability of the recovery boiler can be extended beyond 6 months without cleaning and without noticeable signs of fouling or plugging.

A few processes such as leaching,\(^5\) evaporation/crystallization,\(^6\) electrodialysis,\(^7\) and ion exchange\(^8,9\) have been applied to reduce the chloride level in ash captured in the electrostatic precipitator (ESP) before it is recycled to the liquor cycle. This stream is rather enriched in chloride and is easier to handle than other alternatives, such as the green and white liquor, which are particularly corrosive at the air/liquor interface where the leakage of air causes an increase in the concentration of thiosulfates.\(^10\) However, it is possible to remove chloride by evaporating the white liquor\(^11\) or by cooling the green liquor to temperatures below 20 °C followed by evaporation and subsequent precipitation of NaCl.\(^12\) The first process was developed by Ahlstrom but has not used, whereas the second was practiced in the closed cycle mill at Great Lakes Forest Products Limited, resulting in several operational problems, such as corrosion problems in the evaporators.\(^13\)

In some kraft mills, it is common practice to simply purge part of the total ash collected in the precipitator, but this causes a significant loss of sodium sulfate and sodium carbonate. This sodium must be replaced, so there is an additional cost for makeup chemicals. A preliminary economic analysis reported by Ferreira et al.\(^14\) for different ash treatment alternatives (purging, leaching, evaporation/crystallization, and ion exchange), indicated that, in terms of maintenance costs, purging is indeed the most expensive alternative, mainly because of the sulfate makeup. Ion exchange was found to be an attractive process for efficient chloride removal as it is one of the less expensive alternatives.

The selective removal of chloride from ESP using the Recofo ion-exchange technology employs fine particles,
short column heights, and high flow rates. In the work reported by Jemaa et al., the ashes are dissolved in warm water (40–50 °C), and then the previously filtered solution is percolated through a fixed bed packed with an amphoteric resin that exhibits greater affinity for sodium chloride than for other compounds such as sodium sulfate. Thus, during this operation (upstroke step), the NaCl is adsorbed by the resin, and the purified solution (Na2SO4/Na2CO3) is collected and recycled to the kraft recovery cycle. Sodium chloride is released by the resin during the downstroke step, in which water is passed through the bed. The system alternates automatically between the upstroke and downstroke every 2 min. The work presented here deals with a similar ion-exchange system in which the operation steps are carried out with longer cycle times, approximately 12 min, and the size of the resin (ion retardation resin AG 11 A8) particles used is higher than the standard fine mesh size utilized in the Recoflo systems. In this study, the attention is focused on the dynamics of the process based on saturation and regeneration fixed-bed experiments. Saturation was modeled using an extended Langmuir–Freundlich isotherm for three components based on single-component equilibrium data. Several cyclic experiments were also carried out, to evaluate the resin performance.

2. Material and Methods

Equilibrium isotherms were determined by batch experiments at a temperature of 45 °C using a Unitronic (Selecta) shaker and a thermostatic bath. In these experiments, a known mass (2 g) of resin Bio-Rad AG 11 A8 was poured into volumetric flasks with 20 mL of initial solution with concentrations of NaCl, Na2SO4, and Na2CO3 ranging from 32 to 1300 mmol/L, from 20 to 1500 mmol/L, and from 60 to 140 mmol/L, respectively. The flasks were then placed in the shaker for 48 h (time required to reach equilibrium). After equilibrium was reached, the solution was separated from the resin and the concentrations of Cl−, SO42−, and CO32− were determined by titration and ion chromatography techniques. The physical properties of the resin used are listed in Table 1.

Fixed-bed experiments (saturation and regeneration) were carried out in a jacketed column (26 × 500 mm, Pharmacy), with the flow controlled by a peristaltic pump (Ismatec-BVP). The experimental conditions for these runs are summarized in Table 2. During the saturation step, an aqueous solution prepared from industrial ESP ash was passed through the column, and fractions of the treated feed, at the column outlet, were collected at regular intervals of time for analysis. In the regeneration step, distilled water was percolated through the column, and fractions of the eluted solution were also collected. The ESP ash was obtained from a Portuguese pulp mills using Eucalyptus globulus (hardwood) with larger chloride concentration levels in the recovery cycle. To prepare the feed solution, the ashes were dissolved in water to yield a concentration of about 30–40% of dissolved solids and then filtered under vacuum using a Buchner funnel to remove the suspended solids. The concentration ranges of the principal species present in the samples of ESP ash and measured using analytical techniques as described above are reported in Table 3. The temperature of 45 °C for the experiments was chosen on the basis of the thermal balance after the necessary dilution of the hot ash stream collected from the electrostatic precipitator with industrial water.

Cyclic operation experiments were performed under conditions identical to those used for the fixed-bed experiments with the exception of some operating conditions, as described below, which were changed to approach the industrial-scale conditions. Thus, the saturation and regeneration steps were carried out at a flow rate of 37 mL/min, at 45 and 20 °C, respectively. Fresh water collected from the mill was used for the preparation of the ash solution (±3% dissolved solids) and for the regeneration of the bed. The cycle times were defined on the basis of a previous experiment run under the same conditions. The results of this last experiment were also used to define the collecting time intervals of sulfate-rich solution and of chloride purge, aiming at minimizing sulfate and sodium losses without compromising the chloride removal efficiency. The saturation/regeneration cycles and sulfate recovery/chloride purge were shifted automatically using a timer and electrical valves in a specially designed laboratory apparatus (see Figure 2), according to the times depicted in Figure 1.

The chloride and sulfate concentrations were periodically determined by titration techniques in the sulfate recovery and chloride purge solutions, at the end of a

### Table 1. Physical Properties of the AG 11 A8 Resin

<table>
<thead>
<tr>
<th>property</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>wet density, ρw (g of wet resin/L of resin)</td>
<td>1027</td>
</tr>
<tr>
<td>apparent density, ρa (g of dry resin/L of resin)</td>
<td>681</td>
</tr>
<tr>
<td>particle porosity, pP</td>
<td>0.46</td>
</tr>
<tr>
<td>moisture content (%)</td>
<td>33</td>
</tr>
<tr>
<td>average particle size (mm)</td>
<td>0.23</td>
</tr>
</tbody>
</table>

### Table 2. Experimental Conditions for Fixed-Bed Experiments

<table>
<thead>
<tr>
<th>run</th>
<th>CCl (g/L)</th>
<th>CS (g/L)</th>
<th>CCO (g/L)</th>
<th>feed pH</th>
</tr>
</thead>
<tbody>
<tr>
<td>1a</td>
<td>24.00</td>
<td>156.10</td>
<td>2.40</td>
<td>8.1</td>
</tr>
<tr>
<td>2a</td>
<td>25.50</td>
<td>146.0</td>
<td>7.30</td>
<td></td>
</tr>
</tbody>
</table>

* Bed properties: x = 0.45, L (cm) = 22 (runs 1a/b) and 26 (runs 2a/b). Flow conditions: U (cm/min) = 15.3, u (cm/min) = 3.06, and t (min) = 3.24 for runs 1a/b; U (cm/min) = 40.0, u (cm/min) = 7.77, and t (min) = 1.51 for runs 2a/b.

### Table 3. Composition of ESP Ashes

<table>
<thead>
<tr>
<th>chemical species</th>
<th>weight % in ESP ash</th>
</tr>
</thead>
<tbody>
<tr>
<td>sulfate</td>
<td>32–37</td>
</tr>
<tr>
<td>sodium</td>
<td>30–40</td>
</tr>
<tr>
<td>carbonate</td>
<td>16–18</td>
</tr>
<tr>
<td>chloride</td>
<td>5–7</td>
</tr>
<tr>
<td>potassium</td>
<td>4</td>
</tr>
</tbody>
</table>
Mass balance inside particles
\[
\rho, \frac{\partial q(u, z, \theta)}{\partial \theta} + \epsilon_p \frac{\partial X_{pl}(u, z, \theta)}{\partial \theta} = \frac{\partial^2 X_{pl}(u, z, \theta)}{\partial u^2} + \frac{2}{u^*} \frac{\partial X_{pl}(u, z, \theta)}{\partial u^*}
\]

Multicomponent equilibrium adsorption at the pore/wall interface described by the extended Langmuir–Freundlich model
\[
q_i = \frac{a_i (C_{El} X_{pi}/\eta)^n_i}{1 + \sum_{j=1}^{3} b_j (C_{El} X_{pi}/\eta)^n_j}
\]

where \(a_i\), \(b_i\), and \(n_i\) are given by the individual Langmuir–Freundlich isotherm (eq 1) and \(\eta_i\) represents the interaction terms to quantify the competitive adsorption in multicomponent systems.\(^{15}\)

This system of equations is subject to the following initial and boundary conditions:

**Initial conditions**
\[
\theta = 0 \quad X_i(z^*, 0) = X_{i0} \quad \text{and} \quad X_{pl}(u^*, z^*, 0) = X_{i0}
\]

**Boundary conditions**
\[
u^* = 0 \quad \left. \frac{\partial X_{pl}(u^*, z^*, \theta)}{\partial u^*} \right|_{u^* = 0} = 0
\]
\[
u^* = 1 \quad N_{Di}[X_i(z^*, \theta) - X_{pl}(1, z^*, \theta)] = 3 - \epsilon N_{Di} \left. \frac{\partial X_{pl}(u^*, z^*, \theta)}{\partial u^*} \right|_{u^* = 1}
\]

The above equations are written in terms of dimensionless variables: \(X_i = C_i/C_{El}\), \(X_{pl} = C_{pl}/C_{El}\) are the dimensionless concentrations of species \(i\) in the bulk liquid phase and in the liquid inside particle pores, respectively; \(\theta = t/\tau\) is a reduced time, where \(\tau\) is the bed space time; \(z^* = zL\) is the reduced axial coordinate, where \(L\) is the fixed-bed length; and \(u^* = r/R\) is the reduced particle radial coordinate, where \(R\) is the adsorbent particle radius. The dimensionless groups are the Péclet number
\[
Pe = \frac{uL}{\epsilon D_{ax}}
\]
where \(D_{ax}\) is the axial dispersion coefficient; the number of mass-transfer units transported by pore diffusion for species \(i\)
\[
N_{Di} = \frac{\tau \epsilon_{pi} D_{pi}}{R^2}
\]
where \(D_{pi} = D_{mi}/\tau_p\) is the species \(i\) effective diffusivity and \(\tau_p\) is the tortuosity factor; and the number of film mass-transfer units for species \(i\)
\[
N_{fi} = \frac{3(1 - \epsilon)k_{fi} \tau}{\epsilon R}
\]
where \(k_{fi}\) is the film mass-transfer coefficient for species \(i\).
Figure 3. Equilibrium isotherms at 45 °C for Bio-Rad resin in NaCl and Na₂SO₄ solutions.

Numerical solution of eqs 2-7 was performed by discretizing eq 3 in the radial direction using orthogonal collocation in Nₑ finite elements with cubic Hermite polynomials as basis functions. This led to a new boundary value problem of Nₑ+1 (where Nₑ is the number of components) parabolic PDEs in the independent variables zₑ and θ that were numerically integrated with the PDECOL package.16

To evaluate Nₑ, the bed porosity ε was experimentally determined, and the film mass-transfer coefficient, kᵢ, was estimated using the empirical correlation, valid for low Reynolds numbers (Re < 50)

\[ \frac{Sh}{Sc^{1/3}Re} = 0.91Re^{-0.51} \]

with

\[ Sh = \frac{k_i d_p}{D_m} \]

\[ Re = \frac{ud_p \rho}{[\mu 6(1 - \epsilon)] \sigma} \]

and

\[ Sc = \frac{\mu}{\rho D_m} \]

The molecular diffusivities of Cl⁻, SO₄²⁻, and CO₃²⁻ were estimated by the Nernst equation17

\[ D_{mi} = 2.661 \times 10^{-7} \lambda_i/|z_i| \]

where \( \lambda_i \) and \( z_i \) are the equivalent ionic conductivity and the charge for species \( i \), respectively. The values of \( D_{mi} \) obtained were also used to calculate the parameter \( \Lambda_{Di} \), in which, for the evaluation of the effective diffusivity \( D_S \) (\( = D_{mi}/\epsilon_p \)), the tortuosity factor was predicted as being 2.17, according to the random-pore model of Wakao and Smith,18 \( \epsilon_p = 1/\epsilon_{fp} \).

4. Results and Discussion

4.1. Analysis of Isotherm Data. Results of single-solute adsorption equilibrium data for aqueous NaCl, Na₂SO₄, and Na₂CO₃ solutions being adsorbed onto resin are shown in Figures 3 and 4. According to the manufacturer, the resin is a styrene divinylbenzene cross-linked rigid polymer lattice with attached quaternary ammonium groups (strong basic anion-exchange groups) and also having a linear, relatively flexible acrylic acid polymer based on carboxylic groups (weak acidic cation-exchange groups). Thus, the resin is of amphoteric type (containing both cation-exchange and anion-exchange groups), i.e., when brought into contact with aqueous salt solutions, the ions are adsorbed without exchange.19 In fact, the small pH change observed in the samples collected from the batch experiments, when compared with the initial and final (equilibrium) conditions, is not caused by any ion-exchange reaction. Hence, an approach based on models used to describe adsorption processes should be suitable for predicting the equilibrium distribution of solutes between the solid and liquid phases. Thus, the experimental points (qₑ, Cₑ) of the adsorption equilibrium data for each studied component were fitted by the Langmuir–Freundlich equation. The values found for the parameters are as follows: \( a_1 = 1.10 \times 10^{-3} \), \( b_2 = 2.20 \times 10^{-4} \), and \( n_3 = 1.20 \) for chloride; \( a_1 = 4.67 \times 10^{-6} \), \( b_2 = 4.38 \times 10^{-6} \), and \( n_3 = 2.10 \) for sulfate; and \( a_1 = 1.76 \times 10^{-4} \), \( b_2 = 9.77 \times 10^{-5} \), and \( n_3 = 1.35 \) for carbonate. The single-component equilibrium data illustrated in Figures 3 and 4 show that the adsorptive capacity of the resin depends on the species, the chloride ion being the most adsorbed, as expected.

4.2. Analysis of Saturation and Regeneration Curves. Adsorption and desorption breakthrough curves corresponding to the saturation and regeneration steps, respectively, in the fixed bed are shown in Figures 5 and 6. It should be noted that the industrial ash streams treated in the two experiments were collected in different periods of the mill operation. The ash sample used in run 2 is quite similar to that used in run 1 in terms of chloride and sulfate concentrations, but it contains a higher amount of carbonate. Table 4 shows also the values used for the model parameters in the simulation of the saturation experiments. A reasonable agreement is observed between experimental and calculated concentration curves for species \( i \) (see Figure 5a,b), with the adjustable parameters being the Pelet number, \( Pe \), and the interaction factors, \( \eta_i \). The values found for \( \eta_i \) are \( \eta_{Cl} = 0.3 \), \( \eta_{SO_4} = 4 \), and \( \eta_{CO_3} = 4 \).

Figure 5a,b illustrates the effect of the flow rate on the adsorption (saturation) breakthrough curves. As expected, at low flow rates, a longer contact between the phases is promoted, and this leads to larger break-
through times. This effect can also be seen in Figure 6a,b. Decreasing the flow rate results in a longer time needed to regenerate the bed. Moreover, a longer time is needed to remove the chloride from the fixed bed than the other species; this is because chloride has a higher affinity for the adsorbent. At high flow rates, the regeneration of the bed is faster, and the chloride concentration exhibits a higher maximum peak. The behavior of the regeneration curves can be better explained by the influence of the regeneration on the adsorption equilibrium of the species on the adsorbent. However, for the resin studied, it is still unclear how this equilibrium is affected when the bed is regenerated with water. One might expect that the rapid displacement of the chloride ion from the bed by fresh water should be accompanied by the breakage of bonds or by significant structural changes of the resin sites as reported by Rice and Foo.  

4.3. Saturation Simulation. Effect of Axial Dispersion. The effects of axial dispersion on the saturation curves are illustrated in Figure 7. The axial dispersion measured by the Peclet number, Pe, is a function of the hydrodynamic conditions in the bed and of the resin packing. Mixing within the bed increases when the Peclet number decreases. As a consequence, the spreading of the concentration profiles inside the bed increases, and breakthrough occurs earlier, as can be seen in Figure 7; the effect is especially visible for the chloride curve, as chloride is more extensively adsorbed than sulfate and carbonate.

4.4. Saturation Simulation. Effect of Chloride Concentration in the Feed. The effect of the chloride concentration in the feed is shown in Figure 8 for three different Cl⁻ levels within the typical concentration range for the chloride species in the ESP ash. It should be noted that the breakthrough time is only slightly lower when the chloride concentration is increased.
affected, whereas the chloride concentration histories result in increasingly sharp curves as the chloride feed concentration increases. This is probably due to the influence of the differences in the adsorption equilibrium for the three components at higher chloride concentrations in the mixture and the lower tendency toward spreading of the concentration waves during the dynamics of the saturation process.

4.5. Cyclic Operation. Effect on the Adsorption Capacity of the Resin. The effect of cyclic operation on the adsorption capacity (aging) was evaluated by performing a cyclic experiment of saturation followed by regeneration steps at conditions equivalent to those used in industry. The results are shown in Figure 9. Although the possible number of cycles performed at the laboratory scale is limited when compared to a full-scale operation, this set of cycles was valuable for assessing the resin behavior in the first days of operation and for collecting data on process conditions for a possible scale-up of the technical solution.

During the cyclic operation experiment, the resin was exposed to 362 cycles, each of 12 min total time (saturation + regeneration), corresponding to approximately 3 days of continuous labor. The chloride removal efficiency along the experiments was always greater than 89%, corresponding to an average resin capacity of 0.6 mmol of Cl⁻ per gram. The variation in the resin capacity was associated with the varying composition of the ash solution fed to the column. Finally, it was possible to determine an average sulfate loss of 26%, with a maximum loss of 33%.

4.6. Flowsheet and Process Economics. A plant was designed to demonstrate the scale-up viability on the basis of experimental data obtained in this work. Figure 10 shows a schematic flowsheet of the process with results corresponding to the overall material balance that was calculated on the basis of the following assumptions: (i) an incoming flow rate of 3 tons of precipitator ash per hour and (ii) a 90% removal of chloride by the system, accompanied by a 70% recovery of sodium sulfate. The plant basically consists of an ion-exchange column containing a certain amount of amphoteric resin, a filter, two dissolving tanks, and two tanks for feed and product solutions. The only utility used for this process is water for dissolving the ash at a temperature of 45 °C. A nearly saturated solution with approximately 300 g of solids/kg of water is produced. The ash solution is fed to a filter where insoluble solids are removed. After this step, the filtered solution is pumped up through the resin bed to remove sodium chloride. The purified solution (SO₄²⁻/CO₃²⁻) is collected and recycled back to recovery. The resin is regenerated with water, producing a NaCl-rich stream that is sent to the general wastewater treatment plant.

A preliminary economic analysis was performed to compare the operating costs of purging of ash with two methods for chloride removal: ion exchange and evaporation/crystallization. Considering a Portuguese pulp mill that discards one-third of the total amount of ash (5 tons/h) generated from electrostatic precipitator for controlling the chloride levels in the recovery cycle, this causes a loss of about 10354 tons/year of sodium sulfate with a cost estimated at approximately $1,140,000/year. In comparison, the use of the ion-exchange system to treat 3 tons/h of ash would cause a loss of 5591 tons/year of Na₂SO₄, corresponding to a savings of over...
Also, in this step, a SO$_4^{2-}$ can be efficiently removed during the saturation process.

Conclusions

Excessive accumulation of chloride in the kraft recovery cycle of pulp mills is a serious concern. In this work, we have studied an ion-exchange process based on an amphoteric resin that selectively removes chloride from the ash generated by the recovery boiler. Saturation and regeneration experiments were performed under two different flow rates. Because the resin used presents a greater affinity for Cl, the chloride breakthrough curve arises at a longer time than those for the other components (sulfate and carbonate), and chloride can be efficiently removed during the saturation process. Also, in this step, a SO$_4^{2-}$/CO$_3^{2-}$-rich stream is recovered that would be available to be returned to the recovery cycle. It is shown that the use of water as the regenerant leads to the rapid and complete elution of species from the resin.

A mathematical model considering dispersed plug flow for the bulk liquid, external mass-transfer resistance, intraparticle mass transfer by pore diffusion, and instantaneous equilibrium of adsorption at the pore/wall interface was presented to simulate the fixed-bed saturations. The model yields results that are in reasonable agreement with experimental data, and it was successfully tested in simulations of the process dynamics for different values of axial dispersion and chloride feed concentration.

The resin performance was not affected during cyclic operation, in which the chloride removal efficiency was always larger than 89% while the sulfate recovery varied between 67 and 74%. On the basis of these results, obtained at the laboratory scale, which can be easily extrapolated to larger scales, one can conclude that the studied process can provide a true industrial alternative to the problem of the selective removal of chloride in the ash captured from the electrostatic precipitator (ESP) of the recovery boiler of pulp mills.

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Nomenclature

\begin{itemize}
  \item $C$ = solute concentration in the fluid phase, mmol/L
  \item $D_a$ = axial dispersion coefficient, cm$^2$/s
  \item $D_m$ = intraparticle diffusion coefficient, cm$^2$/s
  \item $D_m$ = molecular diffusivity, cm$^2$/s
  \item $k_f$ = film mass-transfer coefficient, cm/s
  \item $L$ = bed height, cm
  \item $N_p$ = number of mass-transfer units transferred by pore diffusion
  \item $N_f$ = number of film mass-transfer units
  \item $P_e$ = axial Peclet number
  \item $q$ = adsorbed solute concentration in equilibrium with the liquid concentration, mmol/g of wet resin
  \item $r$ = radial coordinate, cm
  \item $R_p$ = particle radius, cm
  \item $t$ = time, s
  \item $u$ = bed superficial velocity, cm/s
  \item $u^*$ = normalized radial coordinate ($r/R$)
  \item $U$ = volumetric flow rate, cm$^3$/min
  \item $X$ = dimensionless solute concentration in the bulk liquid phase ($C/C_E$)
  \item $X_p$ = dimensionless solute concentration in the liquid inside the pores ($C_p/C_E$)
  \item $z$ = bed axial coordinate, cm
  \item $z^*$ = normalized axial coordinate ($z/L$)
\end{itemize}

Greek Letters

\begin{itemize}
  \item $\epsilon$ = bed porosity
  \item $\epsilon_p$ = particle porosity
  \item $\rho_w$ = wet density of the adsorbent, g/cm$^3$
  \item $\theta$ = normalized time ($t/r$)
  \item $\tau$ = space time, s
\end{itemize}

Subscript

\begin{itemize}
  \item $f$ = feed conditions
\end{itemize}

Literature Cited


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