



# Article Diffusion of Ethanol in Supercritical Carbon Dioxide—Investigation of scCO<sub>2</sub>-Cosolvent Mixtures Used in Pharmaceutical Applications

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Abstract: Diffusion coefficients, D, for ethanol in supercritical carbon dioxide (scCO<sub>2</sub>) were measured in the temperature range 306.15–331.15 K and along the 10.5 MPa isobar, using the Taylor dispersion technique. The obtained diffusivities ranged from  $1.49 \times 10^{-8}$  to  $2.98 \times 10^{-8}$  m<sup>2</sup> s<sup>-1</sup>, an order of magnitude higher than in usual liquids. The dependence of D on temperature and solvent density was examined. Various correlation models based in the hydrodynamic theory were assessed to estimate the diffusion coefficients, with reasonable results obtained for the Wilke-Chang and Lai-Tan models.

Keywords: supercritical CO2; diffusion coefficients; ethanol; Taylor dispersion

## 1. Introduction

Transport coefficients are essential properties for modeling, designing, and scaling-up rate-controlled processes. Supercritical fluids (SCFs) have the remarkable ability to be applied at the industrial level in mass-transfer operations, phase transition processes, reactive systems, and nanostructured and materials related processes [1]. Carbon dioxide (CO<sub>2</sub>), among SCFs, has been widely used due to its chemical stability, considerable inertness, low critical temperature, relatively non-toxicity, non-flammability, and availability in high purity at relatively low cost [2]. Physical properties of supercritical CO<sub>2</sub>, namely, density, viscosity, and diffusivity, can be controlled by the simple adjustment of the working conditions (temperature and pressure). Response to minor changes in the temperature and pressure of this fluid near the critical region result in high variations in its density and solubility. These features, together with the fact that supercritical CO<sub>2</sub> presents low viscosity and high diffusivity like gases and high density and solvating power like liquids [3] and that it is classified as a safe solvent for the FDA [4], make it a very convenient and resourceful solvent and anti-solvent to be used in the pharmaceutical industry in a wide variety of processes and technologies related to drug formulation such as purification, micronization, and encapsulation of drugs, in contrast to more conventional methods.

Application of scCO<sub>2</sub> through technologies such as rapid expansion of supercritical solutions (RESS), supercritical anti-solvent (SAS) and derivatives, and depressurization of an expanded liquid organic solution (DELOS) has been used to overcome poor physiochemical, pharmacokinetic, and pharmacodynamic properties of drugs that limit their therapeutic effect [5–9] and to produce micro-particles for drug delivery in which the active principle is encapsulated within biocompatible polymers [10–14]. Such formulations, in the form of microparticles, nanoparticles, polymeric membranes, aerogels, microporous foams, solid lipid nanoparticles, and/or liposomes, encapsulate the active principle ideally at high drug loads, transport it to the site of action, and release it in a controlled manner, hence improving the efficacy and safety of the drug [15]. In common, all these methods use a step of mixture of a drug (or a solution of the drug) with  $scCO_2$  as a solvent (or co-solvent), followed by a depressurization step, through a nozzle, according to the principle that the decrease in pressure leads to decrease in density and thus, in the drug solubility, creates a supersaturated solution and further precipitation, producing small particles with uniform



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size distributions. In RESS,  $scCO_2$  is used as the solvent and so is applied for drugs that have a good solubility in them. In SAS, the precipitation occurs by addition of  $scCO_2$  to a liquid solution of the drug, where the solvent is usually an alcohol (ethanol/methanol/propanol), ketone (acetone), or dimethyl sulfoxide. The addition of  $scCO_2$  gives place to a mixture in which the drug is not soluble anymore. In this case, the drug is insoluble or slightly soluble in the supercritical fluid, whereas the liquid solvent and the fluid are highly miscible [16]. In the DELOS process [17], the precipitation occurs by depressurization of a solution the drug plus an organic solvent plus  $scCO_2$  to atmospheric pressure. This depressurization goes along with a decrease of the solution temperature, both contributing to the solution supersaturation and to the precipitation yield. In such process, the drug is soluble in the organic solvent plus  $scCO_2$  mixture.

The major advantage of these technologies is that the size of the particles can be controlled by solely manipulating the  $scCO_2$  temperature and pressure conditions, and the conditions met provide a final product without solvent residues. However, the choice of which process to use for a defined drug and what would be the ideal operative conditions is, in itself, a unique challenge because it requires knowledge of the involved phase equilibria. Behavior of general solutes in SCFs near the critical point is highly non-ideal [18], and the prediction of their behavior based on their properties in aqueous media with traditional models might fail. Moreover, supercritical  $CO_2$  is a non-polar solvent, and thus, it does not dissolve well all compounds, which can limit the applicability of the  $scCO_2$  based technologies. This limitation can be overcome by introducing small amounts of co-solvents and/or surfactants together with  $scCO_2$  (like in SAS and DELOS technologies) [19], but the addition of more components increases the complexity of the system and ultimately requires deeper knowledge of the system properties and further process optimization.

When employing co-solvents to enhance the drug solubility, many times the choice relies on ethanol. The presence of this co-solvent increases the solvent mixture density, the polarity and also the specific interactions like hydrogen bonding. Moreover, ethanol is generally safe and has a relatively high affinity with for supercritical CO<sub>2</sub>, being extensively used for supercritical extraction [20,21].

Fundamental properties in supercritical CO<sub>2</sub>, such as mass transport, have been objects of great interest, and it is possible to find data available far from the critical point, but information under near-critical conditions is lacking in the literature. Thus, detailed and accurate information about diffusion of ethanol in supercritical CO<sub>2</sub>, as co-solvent, is of great importance, in view of its role in the rational design and efficient operation in the process of creating a controlled drug delivery device. This study aims to investigate the diffusion of ethanol in carbon dioxide, at temperature and pressure above the critical point (314.18 K and 7.38 MPa), in a broad range of densities of this fluid covering areas close and far from the critical point, in order to understand the transport phenomena occurring in this mixture.

## 2. Materials and Methods

#### 2.1. Materials

Toluene 99.85% (CAS Number: 110-82-7) was supplied by Acros Organics and ethanol absolute 99.97% (CAS Number: 64-17-5) was supplied by VWR Chemicals Prolabo. All liquids were used as received, with no further purification.  $CO_2$  with purity higher than 99.995% (water content < 40 ppm) was supplied by Air Liquide.

#### 2.2. Equipment and Procedure

The present equipment was built based on the principle of the Taylor dispersion method and is represented in Figure 1. The basis of the method is as follows: when a pulse of a solute is injected into a solvent stream flowing under a laminar regime through a capillary tube of circular cross section, the pulse will broaden due to the combined action of convection along the longitudinal axis and molecular diffusion in the radial direction. A stainless-steel capillary tube of (30.916  $\pm$  0.001) m length and 0.375 mm inner radii was used.

It was coiled on a grooved aluminum cylinder in the form of a helix with 0.36 m diameter, for both support and temperature regulation, and kept at the study temperature  $\pm 0.1$  K using a temperature-regulated water bath (Lauda Eco RE415G). At the start of each run, a pulse of 5 µL of pure solute was injected through a 6-port injection valve (Knauer model A1357) into CO<sub>2</sub> at a constant flow rate of 0.3 cm<sup>3</sup> min<sup>-1</sup>, maintained by a HPLC analytical pump (Jasco PU-4185). Attached to the pump head, there is a custom designed cooling device; temperature is regulated by a Peltier module and thermostated through a circulating water bath set to 260.15 K to ensure  $CO_2$  is in the liquid state and the pump can pressurize liquid  $CO_2$  above its critical pressure. At the pump outlet, a heat exchanger of about 1.5 m long is used for preheating subcooled liquid  $CO_2$  to its supercritical state before the injection valve. Dispersion of the injected samples was monitored at the outlet of the dispersion tube using an FT-IR refractometer (Jasco FT-IR 4600), equipped with a high-pressure demountable cell (Harrick). Response curves, corresponding to the changes in the flow with time were monitored in terms of absorbance/transmittance spectra at wavenumbers corresponding to different vibration modes of the studied molecules. The lower range of Tand p parameters required to perform the diffusion study in supercritical CO<sub>2</sub> is limited by the critical parameters of carbon dioxide:  $T_c = 304.18$ K and  $p_c = 7.38$ MPa [22]. The detector is connected to a computer for digital data acquisition using the Spectra Manager software provided by Jasco. The pressure in the system was established by a back pressure regulator (Jasco BP-4340) and was controlled within  $\pm 0.05$  MPa accuracy with a pressure sensor (Jumo dTrans p30). Data were recorded at increments of  $4 \text{ cm}^{-1}$  and at time intervals of 4 s, for each measurement. Diffusion coefficients are the average of 4 to 6 injections of sample.

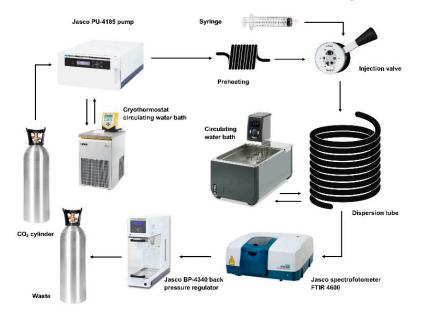


Figure 1. Schematic representation of high-pressure Taylor dispersion set-up.

To determine the diffusion coefficients from the response curve of the absorbance of the solute, we have adopted the same procedure that we apply in with a conventional Taylor refractive index refractometer [23–26], and assuming that small changes in concentration *C* are proportional to variations in absorbance, it is possible to extract the diffusion coefficients by fitting the experimentally measured signal to

$$A(t) = A_0 + A_1 t + A_2 t^2 + R(C(t) - C_0) = A_0 + A_1 t + A_2 t^2 + \Delta A_0 \sqrt{\frac{t_R}{t} \exp\left(-\frac{12D(t - t_R)^2}{R^2 t}\right)}$$
(1)

where the three first terms  $A_0 + A_1t + A_2t^2$  consider the drift and curvature of the baseline due to small concentration and temperature variations;  $t_R$  is retention time of the peak,  $R = (\partial A / \partial C)\lambda$  is the sensitivity of the detector (that depends on the wavenumber upon which

the measurements are carried);  $\Delta A$  is the peak height relative to the baseline. Diffusion coefficients *D* are then obtained by fitting the response curve to the theoretical solution expressed by Equation (1), withdrawing the baseline and offset.

## 3. Results and Discussion

### 3.1. Optimization of Experimental Parameters

Conventional setup for Taylor dispersion experiments generally adopts a refractive index detector (RID) [26–28], but these operate only in low pressure range, generally bellow 0.5 MPa. Performing measurements of diffusion in supercritical fluids requires a detector that can be equipped with high pressure cells [29,30], as it is the case of FT-IR spectrometers. Jasco FT-IR 4600 detector allows to perform measurements simultaneously in an extensive range of wavenumbers, and since the FT-IR spectra of a solute will reflect the vibration modes of that specific molecule, it will work as a digital fingerprint of the injected solute.

This means that, prior to any designed experiment, the IR transmittance spectra for the solute of interest must be analyzed against the infrared spectra for pure supercritical CO<sub>2</sub>. The latter presents three IR transparent regions ranging from 850–1200, 1400–2100, and 2600–3400 cm<sup>-1</sup> [31], and thus meaning that it will be possible to detect to any vibrational modes of the solute molecules that appear in those regions.

Validation and optimization of the Taylor setup for high pressure was done by carrying out measurements of diffusion coefficients of toluene in supercritical CO<sub>2</sub>, and results have been compared against the available literature data [32–36]. An extensive description of all parameters' optimization can be found elsewhere [37]. Transmittance spectra of pure toluene (see Figure 2) shows the lowest transmittance values (that is maximum absorbance) at wavenumbers 1506 cm<sup>-1</sup>, 2925 cm<sup>-1</sup>, and 3036 cm<sup>-1</sup>, which correspond, respectively, to C = C stretching, C-CH<sub>3</sub>, and aromatic C-H stretches. All of these vibration modes appear in the supercritical CO<sub>2</sub> IR transparent regions; therefore, the detected signal corresponds to the dispersion of the pulse of injected toluene in supercritical CO<sub>2</sub>. Additionally, we have selected from the IR transmittance spectra for scCO<sub>2</sub> a wavenumber at which absorbance is minimum, allowing us to control the stability of the baseline during the experiments.

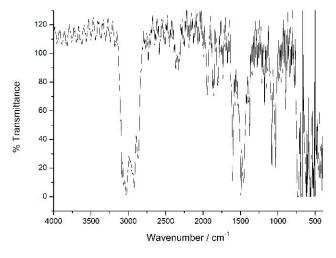


Figure 2. Transmittance in the infrared spectrum of Toluene at 298.15 K and 101.3 kPa.

The typical response curve for the injection of toluene in supercritical carbon dioxide is represented in Figure 3. It is possible to identify three peaks for toluene in supercritical  $CO_2$ , by following the absorbance of the flow at the upper defined wavenumbers. The response curves show no peak tailing effects (their gaussian shape is symmetrical). Moreover, we have one response signal at wavenumber,  $2100 \text{ cm}^{-1}$ , where absorption is minimum. The latter provides reference on the stability of the experiment, giving us the reading of a baseline signal, and it is noticeable that it remains stable during the measurements.

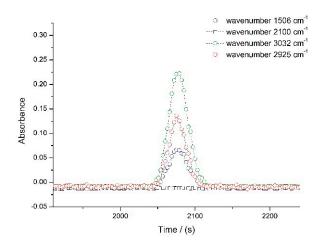


Figure 3. Typical response curves for toluene in supercritical carbon dioxide at different wavenumbers.

Diffusion coefficients for toluene in supercritical carbon dioxide were measured at 306.15 K and at 7.5 MPa, 10.5 MPa, and 12.5 MPa. The obtained diffusion coefficients are an average from 4 to 6 replicate dispersion profiles, and the standard deviation is estimated from the averaged diffusion coefficients over different wavenumbers for each run, over repeated runs. The obtained values are  $D = (2.89 \pm 0.02) \times 10^{-8} \text{ m}^2/\text{s}$ ,  $D = (1.44 \pm 0.03) \times 10^{-8} \text{ m}^2/\text{s}$  and  $D = (1.14 \pm 0.02) \times 10^{-8} \text{ m}^2/\text{s}$ , respectively. As it was expected, observed diffusion coefficients decrease with the increase of pressure at a constant temperature.

Figure 4 shows the measured binary diffusion coefficients for toluene in supercritical carbon dioxide against supercritical carbon dioxide density. Values of density for supercritical carbon dioxide were obtained from NIST [38]. We can see that diffusion coefficients for toluene decrease with increasing density of scCO<sub>2</sub>, because the increase in density brings molecules in closer proximity, and the mean free path available is smaller. Moreover, we found an excellent agreement between our results and the available literature data [32–36,39], with less than 6% difference for the measurements in similar conditions of Sengers et al. [36] and Lai et al. [34].

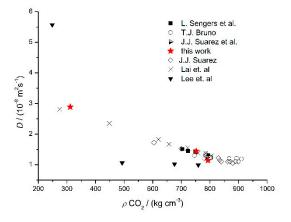


Figure 4. Diffusion coefficient for toluene in scCO<sub>2</sub> and comparison with literature data [32–36,39].

Constrains usually applied to Taylor dispersion method [40] were also verified, namely:

- (i) Laminar regime of the solvent flow, with Reynolds number, *Re* ranging from 55 to 144 for supercritical CO<sub>2</sub> ( $Re = 2a_0\overline{u_0}\rho/\eta$ , where  $a_0$  is the radius of the tube,  $\overline{u_0}$  is the average velocity of the flow,  $\rho$  is the density, and  $\eta$  is the viscosity of the solvent);
- (ii) The peaks presented a Gaussian shape  $(D/\overline{u}L < 0.0024)$  [41];
- (iii) Secondary flow effects associated to coiled columns were negligible with  $De^2Sc < 14$ , where *De* and *Sc* are the Dean and Schmidt numbers, respectively ( $De = Re\omega^{\frac{1}{2}}$ ,  $\omega = Rc/a_0$  and  $Sc = \eta/\rho D$ , where *Rc* is the radius of dispersion coil).

This validates the high-pressure Taylor setup developed here for the measurement of diffusion coefficients in supercritical carbon dioxide.

#### 3.2. Diffusion Coefficients for Ethanol in Supercritical CO<sub>2</sub>

Before the measurements of diffusion coefficients of ethanol in supercritical carbon dioxide, we have selected the working wavenumbers from the ethanol infrared spectrum. Due to the region of high absorbance in supercritical  $CO_2$  spectra, at wavelengths 3500–3800 cm<sup>-1</sup>, superimposed with main stretching frequencies for ethanol (O-H bond), this solute can be identified in an FTIR measurement by its bending frequencies [31]. Thus, we have followed the vibration modes response with time at the positions 1087 cm<sup>-1</sup> (C–C single bond) and 2973 cm<sup>-1</sup> (C–H aromatic bond) not existent in the solvent.

Diffusion coefficients for ethanol in supercritical carbon dioxide, at temperatures ranging from 306.15 to 331.15 K and pressure of 10.5 MPa are presented in Table 1 and were determined from four to six replicate dispersion profiles, together with the calculated density and viscosity [38] for supercritical carbon dioxide in the range of temperatures studied. The obtained diffusion coefficients are an average from 4 to 6 replicate dispersion profiles, and the standard deviation is estimated from the averaged diffusion coefficients over different wavenumbers for each run, over repeated runs.

**Table 1.** Measured diffusion coefficients *D* for ethanol in supercritical CO<sub>2</sub> at pressure *p* =10.5 MPa and calculated density  $\rho$  and viscosity  $\eta$  [38] for supercritical CO<sub>2</sub> at different temperatures from 306.15 to 331.15 K.

T/K	$ ho/kg/m^3$	η/(10 <sup>-5</sup> cP)	$(D \pm S_{\rm D})$ <sup>a</sup> /(10 <sup>-8</sup> m <sup>2</sup> s <sup>-1</sup> )
306.15	752.30	6.37	$1.49\pm0.01$
311.15	690.79	5.51	$1.69\pm0.04$
316.15	604.79	4.52	$1.98\pm0.05$
321.15	489.18	3.49	$2.10\pm0.08$
326.15	393.92	2.85	$2.57\pm0.09$
331.15	338.03	2.57	$2.98\pm0.15$

<sup>a</sup> Standard deviation of the mean. Standard uncertainties are uc(T) = 0.01 K and uc(P) = 0.005 MPa. The expanded uncertainties  $uc(D) \approx 0.05 \times 10^{-8}$  m<sup>2</sup> s<sup>-1</sup> (level of confidence 0.95).

The diffusion coefficient for ethanol in supercritical  $CO_2$ , illustrated in Figure 5, increases with the increase of temperature, as expected. Values for diffusivities of ethanol in  $scCO_2$  are one order of magnitude higher than those in usual liquids (e.g., water) showing that supercritical  $CO_2$  special features, namely, gas-like viscosity and liquid-like density, facilitate mass transference, and this is of high importance considering its application in many pharmaceutical manufacturing processes, for example, in the preparation of drug release systems. Studies performed for this system in a different isobar [42] have shown that the relation is non-linear, and there is an inversion of the slope, corresponding to the region where the mobility (in terms of the inverse of the viscosity) is the maximum for  $CO_2$ . Authors have related this change of slope to the so-called Widom line, corresponding to the transition between liquid-like and gas-like states, which would significantly affect the thermodynamic and transport properties of supercritical carbon dioxide, even in a region that is distant from the critical point. This trend is also observed in our case, and the inversion point occurs before, at around 322.15 K, corresponding to the maximum of mobility at 10.5 MPa (330.15 K for the 12.0 MPa isobar).

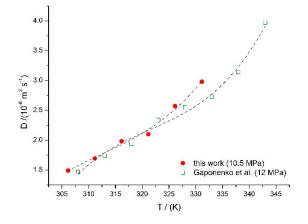
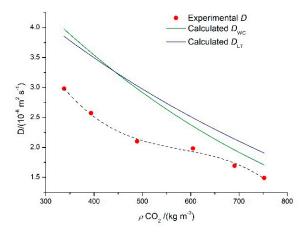


Figure 5. Diffusion coefficient for ethanol in scCO<sub>2</sub> and comparison with literature data [42].

The operating conditions frequently fixed for the measurements of diffusion coefficients are temperature and pressure, which directly influence the solvent density and viscosity. In this way, it is interesting to examine the dependence of the diffusion coefficients D on carbon dioxide density, plotted in Figure 6. The diffusion coefficient for ethanol decreases with the increasing density of supercritical CO<sub>2</sub>, and the reason for this decrease is related to the larger number of molecular collisions and the lessened mean free path available for the molecules.



**Figure 6.** Experimental and calculated diffusion coefficient for ethanol in  $scCO_2$  at pressure p = 10.5 MPa and temperatures from 306.15 to 331.15 K.

Several approaches for the estimate of diffusion coefficients in liquids have been proposed in the literature, and hydrodynamic models, based on the Stokes–Einstein equation [43], have shown to be a simple and useful tool to derive valuable information about the diffusion process. Wilke–Chang (WC) [44], Scheibel (Sch) [45] and Lusis–Ratcliff (LR) [46] are well known models developed for liquid systems and have recently been improved [47] aiming to provide precise estimates of diffusion coefficients in supercritical carbon dioxide. The above-mentioned models, together with the Lai–Tan (LT) [34] model, also based on hydrodynamic theory and validated for solutes diffusing in supercritical carbon dioxide. Equations (2)–(5) for the WC, Sch, LR, and LT models are presented below.

$$D_{WC} = 7.4 \times 10^{-8} \frac{T \sqrt{\phi M_1}}{\eta_1 V_{hn\,2}^{0.6}} \tag{2}$$

$$D_{Sch} = 8.2 \times 10^{-8} \frac{T}{\eta_1 V_{bp,2}^{1/3}} \left[ 1 + \left(\frac{3V_{bp,1}}{V_{bp,2}}\right)^{\frac{2}{3}} \right]$$
(3)

$$D_{LR} = 8.52 \times 10^{-8} \frac{T}{\eta_1 V_{bp,1}^{1/3}} \left[ 1.4 \left( \frac{V_{bp,1}}{V_{bp,2}} \right)^{\frac{1}{3}} + \left( \frac{V_{bp,1}}{V_{bp,2}} \right) \right]$$
(4)

$$D_{LT} = 2.5 \times 10^{-7} \frac{T\sqrt{M_1}}{\left(10\eta_1\right)^{0.688} V_{c,2}^{1/3}}$$
(5)

In the Equations (2)–(5), temperature *T* is in K,  $\eta_1$  is the solvent viscosity in cP;  $\varphi$  is a dimensionless association factor of the solvent,  $M_1$  is the solvent molecular weight in g/mol,  $V_{bp,1}$  and  $V_{bp,2}$  are the solvent and solute molar volumes at their normal boiling points in cm<sup>3</sup>/mol, respectively, and  $V_{c,2}$  is the solute critical volume in cm<sup>3</sup>/mol.

A general idea on the performance of these hydrodynamic models for the prediction of the diffusion coefficients can be obtained when examining the average absolute deviation (*AAD*) which comes defined as

$$AAD (\%) = \frac{100}{n} \sum_{i=1}^{n} \left| \frac{D_{exp} - D_{pred}}{D_{exp}} \right|$$
(6)

where the subscripts "*exp*" and "*pred*" refer to the experimental and calculated diffusion coefficients, and *n* is the number of experimental points, in our case 28. Table 2 shows results for the various correlations tested for the prediction of diffusion coefficients of ethanol in supercritical  $CO_2$ .

**Table 2.** The average absolute deviation (*AAD*) for the hydrodynamic models adopted for the prediction of the diffusion coefficients for ethanol in supercritical carbon dioxide.

	AAD %		
Model ———	Original	Modified	
Wilke–Chang (Equation (2))	13.2 <sup>a</sup>	5.8 <sup>e</sup>	
Scheibel (Equation (3))	16.4 <sup>b</sup>	12.7 <sup>e</sup>	
Lusis–Ratcliff (Equation (4))	15.8 <sup>c</sup>	7.4 <sup>e</sup>	
Lai-Tan (Equation (5))	6.8 <sup>d</sup>		

<sup>a</sup> [44], <sup>b</sup> [45], <sup>c</sup> [46], <sup>d</sup> [34], <sup>e</sup> [47], *n* is 28.

Although WC, Sch, and LS equations were derived from diffusion coefficients in solvents other than  $CO_2$ , they can reasonably predict the diffusion coefficients in supercritical carbon dioxide, with values of *AAD* of 13 to 16%. The improved models can increase the accuracy of prediction, cutting *AAD* % to roughly half than the original equations. The Lai-Tan model shows an average absolute deviation of only 7%, so statistically, we should expect a very precise prediction of the diffusion coefficients. However, this statistical reading should be prudent, and a careful analysis should be carried out when applying these models over a broadened density range of the solvent, especially for supercritical carbon dioxide as in our case.

Values for the calculated diffusion coefficients for ethanol using the modified WC and LT models are presented in Figure 6. They show capacity to calculate relatively well the diffusion coefficients in the high-density range (15% or less deviation) but fail at lower densities of carbon dioxide, presenting deviations that can go up to 30%. All the other models show even higher deviations when used for prediction of individual points in the lower density range of carbon dioxide, with deviations that can range up to 60% from experimental data.

The Wilke–Chang model (Equation (2)) has been proposed in 1955, and so far, it remains one of the most extensively used equations to estimate binary diffusion coefficients,

largely due to its simplicity, since it only requires simple information on the solvent and the solute and operating conditions like temperature. Bearing in mind that water is, by excellence, the most widely used solvent and the principal media to define the solubility of a drug, it is interesting to see that the predictions from the WC model for the diffusion coefficients of ethanol in aqueous solution would result in similar deviations (around 15%) towards experimental results [48], notwithstanding the different properties of water and scCO<sub>2</sub>. In fact, the one order of magnitude difference between the diffusion coefficients for ethanol in water (lower diffusivity) and in scCO<sub>2</sub> (higher diffusivity) is the result of the latter characteristics of both liquid and gas because CO<sub>2</sub> in its supercritical state exhibits viscosity and compressibility like a gas but density like a liquid, consequently facilitating mass transfer processes, an important feature when designing a drug delivery system. In general, the WC model shows to be a reasonably good model considering the needs of information on diffusivities of solutes in different media, not always available in the literature.

On the other hand, the deviations attained using the Lai–Tan model, a model validated by using a database for solutes diffusing in supercritical CO<sub>2</sub>, become even more significative when looking for an accurate prediction for a specific system in supercritical conditions, as it is the case with the data needed to model the nano devices for drug release systems using SAS technology. The authors of the Lai–Tan model believe that their approach fails in the supercritical region at lower densities due to the significant amount of clustering around the solutes, which results in an overestimation of the diffusion coefficients [34]; thus, the model still requires some improvement. The fact is, in the near critical region, which is in conditions close to the supercritical  $CO_2$  critical point, is where diffusion coefficients information is absent and where the theoretical models fail. Complexity in performing experiments together with the higher uncertainty of the data, caused by sharper fluctuations in density associated with the critical phase transition is the main issue. Improvement of experimental methods for the measurement of supercritical fluids, to be capable of more precise measures, is the first step to help overcome this lacune and provide information on mass transport data to build more accurate models. In effect, difficulty in predicting accurately the diffusion coefficients from the available theoretical models emphasizes the importance to achieve experimental data in the near critical region, even if measurements in critical conditions are difficult to perform. This does not only provide more accuracy for the development of supercritical based technologies for drug release production in the pharmaceutical industry but ultimately will help to progressively improve the actual prevision models to a point were experimental and estimation coincide.

#### 4. Conclusions

Molecular diffusion coefficients for ethanol in supercritical CO<sub>2</sub> were measured by the Taylor dispersion technique in the temperature range of 306.15 to 331.15 K and along the 10.5 MPa isobar. The obtained values ranged from  $1.49 \times 10^{-8}$  to  $2.98 \times 10^{-8}$  m2 s<sup>-1</sup>. *D* increased non-linearly with temperature and decreased with the increase of carbon dioxide density, and results were consistent with similar studies in the literature. Various correlation models were assessed to estimate the diffusion coefficients, with the best results obtained for the Wilke–Chang and Lai–Tan models but still with 15 to 30 % deviations, reinforcing the need to provide accurate experimental data on the diffusion coefficients, so both the pharmaceutical industry and the scientific community can better develop prevision models.

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